

تقدم لجنة EiCoM الاكاديمية

دفتر لمادة:

# حراريات وموائع

جزيل الشكر للطالبة:

**صفاء**



## \* Ch.1 :- Introduction and overview :-

### \* 1.1 :- Thermal - fluid sciences

Thermo  
dynamics

Heat  
Transfer

Fluid Mechanics

\* 1.2 :- Thermodynamics :- Defined as the sciences of energy  
 ↳ 1<sup>st</sup> law of Thermodynamics (conservation of energy)  
 ↳ 2<sup>nd</sup> law of Thermodynamics (Direction of Heat transfer)

### \* 1.3 :- Heat Transfer :- methods of Heat transfer

Conduction

(in solid)

Convection

(in fluid)

liquid or gas

Radiation

(In space)

\* 1.4 :- Fluid Mechanics :- Defined as the science that deals with behavior of fluid at rest (Fluid statics) or motion (Fluid dynamics).

### \* 1.5 :- Dimensions and units :-

→ Any physical quantity can be characterized by dimension.

→ The magnitudes assigned to the dimensions are called units.



→ Primary dimensions

- Mass (m)
- Length (L)
- Time (t)
- Temperature (T) (Θ)

→ Secondary dimensions or (derived dimensions)

- velocity (V)
- energy (E)
- volume (V)
- density (ρ)
- Force (F)

\* Units

- SI (International system)
- English system (USCS)

\* Dimensions

SI

English System

Mass

kg

pound (lb)  
mass  
or (Libra)

Length

meter (m)

foot (ft)

Time

second (s)

second (s)

Temperature

kelvin (K)

Fahrenheit (°F)

or Degree celcius (°C)

\* Note : 1 ft → 0.3048 m / 1 lb → 0.45359 kg

## Derives units-

\* velocity (V) =  $\frac{\text{length}}{\text{time}}$

SI  
s  $\frac{m}{s}$

English  
 $\frac{ft}{s}$

\* force = mass \* acc

SI  
F s  $kg \cdot \frac{m}{s^2}$  s (N) (newton)

English  
lbm  $\frac{ft}{s^2}$

\* Work = Force \* distance  
(W)

SI  
s  $kg \cdot \frac{m}{s^2} \cdot m$   
s (N.m)  
s Joule (J)

BTU

\* Power s  $\frac{\text{work}}{\text{time}}$  s  $\frac{N \cdot m}{s}$  (watt)

## \* 2.1 :- system and control volume:-

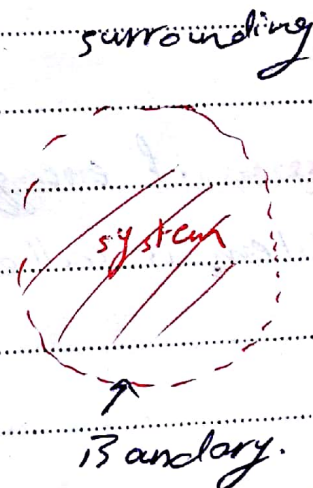
- **system** :- A system is defined as a quantity of matter or a region in a space chosen for study.

- **Surrounding** :- is defined as the mass or region outside the system.

- **Boundary** :- is defined as the real or imaginary surface that separates the system from its surrounding.

⇒ Boundary

- real
- imaginary
- fixed
- movable





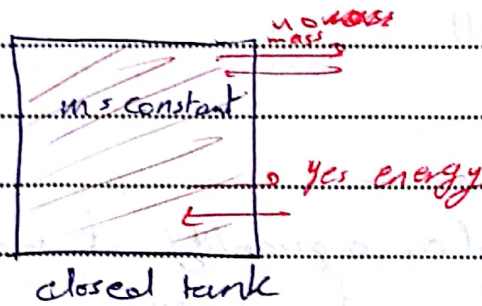
## \* Types of systems :-

- [1] closed system (control mass)
- [2] open system (control volume)

\* **closed system** - a system where no mass transfer or cross the boundary while energy in forms of heat and work can transfer.

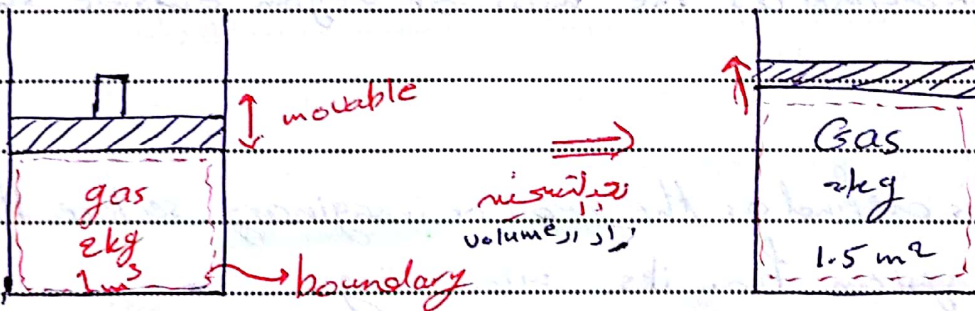
\* Example :-

[1]



(closed system)

[2]



Piston  
cylinder

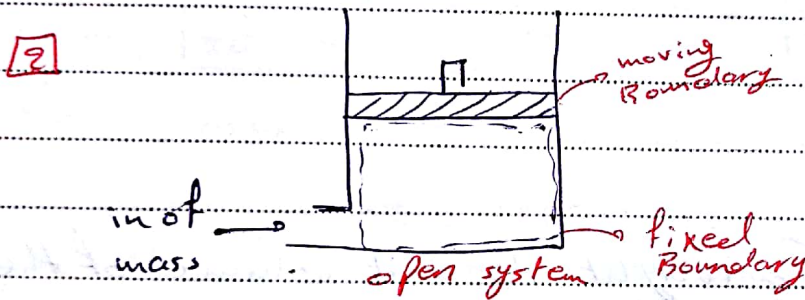
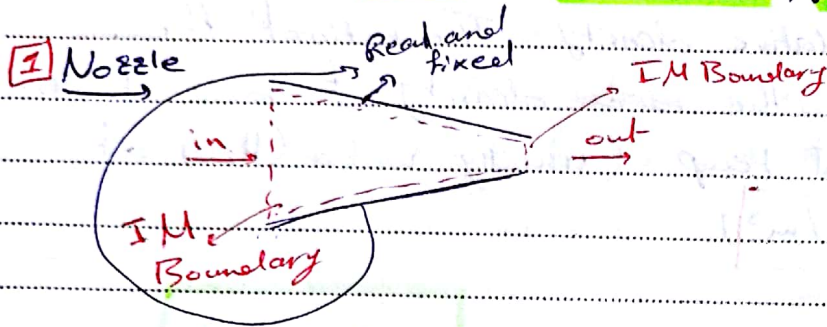
\* **special case** :- if energy is not allowed to cross the boundary, then the system is called "**isolated system**".



**\* open system :-** "control volume" or control surface

→ a system where mass and energy transfer  $\nabla$  or cross the bounding.

**\* Example :-** [1] Nozzle, compressor, pump, turbine.



**\* 2.2:- Properties of system :-**

→ Any characteristic of a system is called a property (Temp, Pressure, volume, density, mass, enthalpy (energy))

=> Properties

- **Intensive** ~ independent of mass (Temp, density, pressure)
- **Extensive** ~ depend on mass or size (mass, volume, energy)

► Subject :

\* Extensive properties per unit mass are called "specific properties"

→ Ex:- specific volume  $v = \frac{V}{m} = \frac{\text{m}^3}{\text{kg}} = \frac{1}{\rho \text{ (density)}}$

\* 2.3 :- Density and specific Gravity (S.G) :-

⇒ specific gravity ~~and~~ relative density :- The ratio of the density of a substance to the ~~data~~ density of some standard substance at a specified temp (usually water (H<sub>2</sub>O) at 4°C)

$$\rho_{\text{H}_2\text{O}} = 1000 \text{ kg/m}^3$$

→ S.G =  $\frac{\rho_{\text{sub}}}{\rho_{\text{H}_2\text{O}}}$  = unit less, Example :- S.G<sub>Hg</sub> = 13.6

$$\rho_{\text{H}_2\text{O}} = 1 \text{ kg/m}^3$$

\* specific weight ( $\gamma$ ) :- The weight per unit volume of the substance,  $\gamma = \rho \cdot g$

→ gravitational acceleration =  $9.8 \text{ m/s}^2$

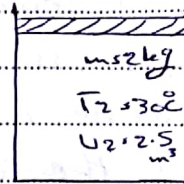
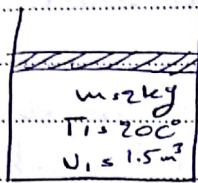
$$\gamma = \frac{\text{kg}}{\text{m}^3} \cdot \frac{\text{m}}{\text{s}^2} = (\text{N/m}^3)$$

\* 2.4 :- State and Equilibrium :-

\* State :- system not undergoing any change of properties.



Ex



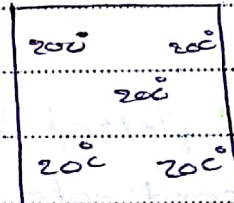
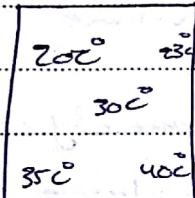
closed system

state 1

state 2

\* **Equilibrium** - a state of balance; there are no unbalanced potentials or driving forces with the system.

Ex



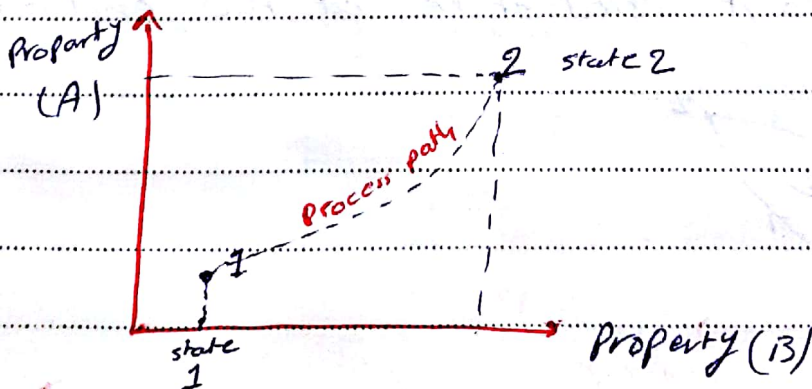
non equilibrium

Equilibrium

\* **Example of equilibrium** - Thermal equil, Mechanical equil, chemical equil.

\* **2.5 :- Processes and cycles :-**

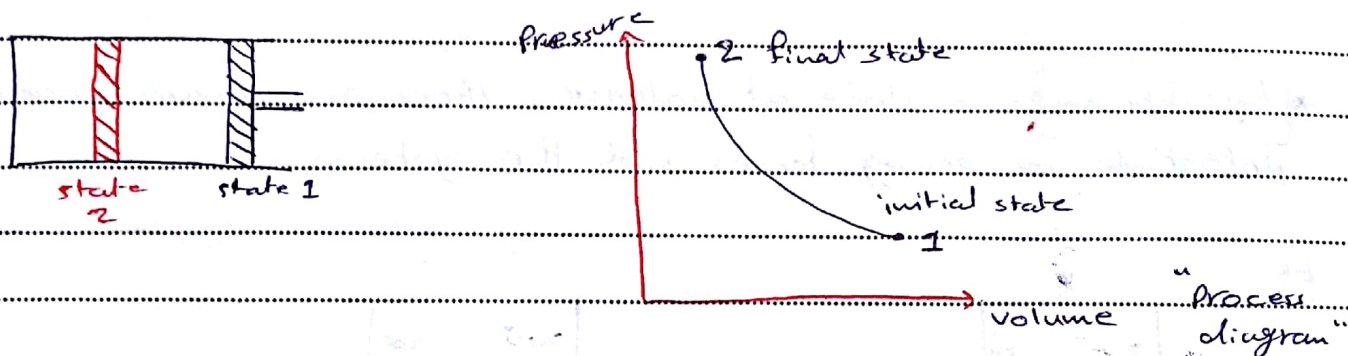
- **Process** - Any change that a system undergoes from one equilibrium state to another state.





→ **Process path** :- A series of states through which a system pass during a process.

→ to describe a process completely, one should specify the initial and final states of process as well as the path it follows, and the interactions with the surrounding.



\* **Process diagram** :- Plotted by employing thermodynamics properties as coordinates, like pressure, volume, temperature.

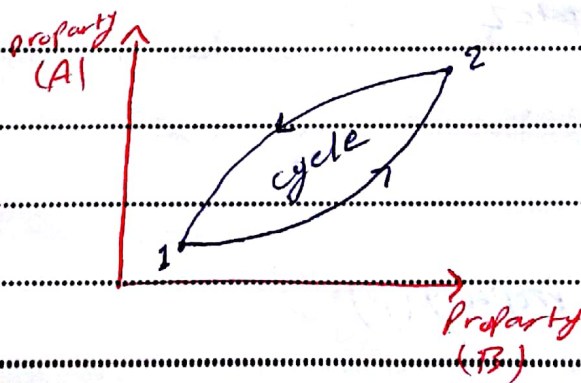
\* During a process, a specific system property may remain constant (iso).

1. **iso thermal process** :- Temp remain constant.

2. **iso baric process** :- Pressure remain constant.

3. **iso metric process** :- Volume remain constant.

\* **cycle** :- system returns to its initial state at the end of the process.



► Subject : \_\_\_\_\_

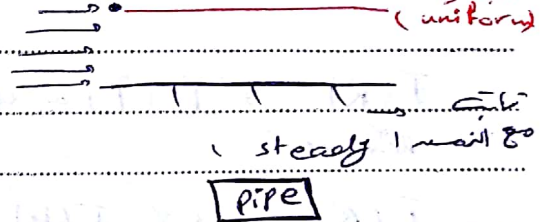
\* example :- otto cycle / Diesel cycle / Refrigeration cycle.

\* The steady - flow process :-

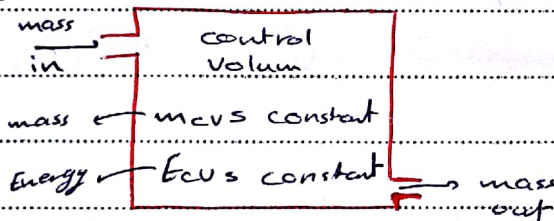
- steady :- No change with time (opposite unsteady, transient)

- uniform :- No change with location over a specific region.

Ex [1] :- flow

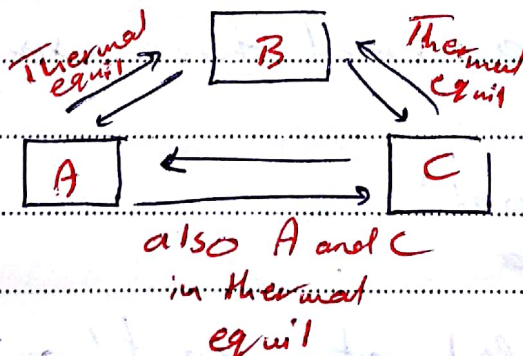


\* Ex [2] :-



\* 2-6 :- Temperature and The zeroth law of Thermodynamics :-

=> zeroth law :- if two bodies are in thermal equilibrium with a third body, they are also in thermal equilibrium with each other.





## \* Temperature scales :-

SI unit	English
celsius scale	fahrenheit scale
kelvin scale	Rankine scale
<u>absolute temp.</u>	

$$\rightarrow T(K) = T(^{\circ}C) + 273.15$$

$$\rightarrow T(R) = T(^{\circ}F) + 459.67$$

Rankine

$$\rightarrow T(R) = 1.8 T(K)$$

$$\rightarrow T(^{\circ}F) = 1.8 T(^{\circ}C) + 32$$

\* Note :-  $\Delta T(K) = \Delta T(^{\circ}C)$

$$\Delta T(R) = \Delta T(^{\circ}F)$$

## \* Temperature Devices :-

- [1] Thermometer.
- [2] RTD
- [3] Thermistor
- [4] Thermo couple

## \* 2.7 :- Pressure :-

\* pressure defined as :- a normal force exerted by a fluid per unit area.

$$\rightarrow p = \frac{F}{A} = \frac{N}{m^2} \quad (\text{Pascal})$$

Pa

Pressure units :- (Pascal (Pa), atm, kg f/cm<sup>2</sup>, bar) SI units



► Subject :

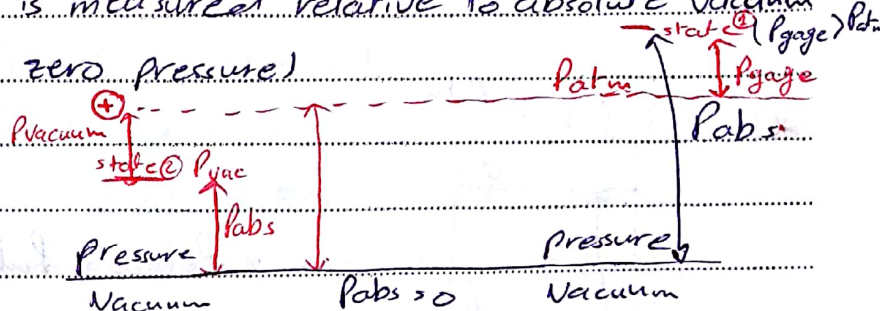
Standard per square in

◦ In english units (lbf/in<sup>2</sup>, (psi))

1 bar  $\longrightarrow$  100 kPa

1 atm  $\longrightarrow$  101.325 kPa

\* Absolute Pressure : it is measured relative to absolute vacuum pressure (i.e. absolute zero pressure)

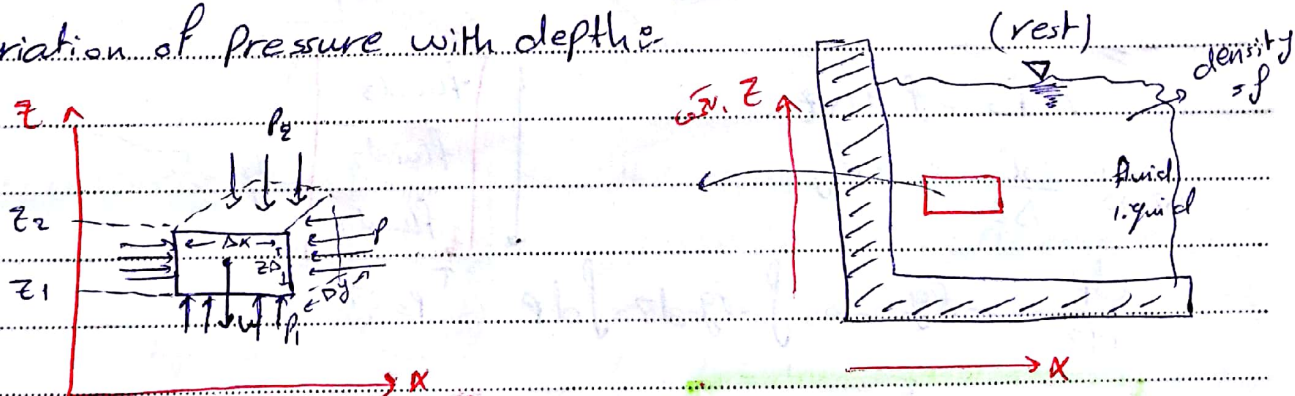


\*  $P_{\text{gauge}} = P_{\text{abs}} - P_{\text{atm}}$

\*  $P_{\text{vac}} = P_{\text{atm}} - P_{\text{abs}}$  (negative sign)

\* Pressure measuring devices are calibrated to read zero in atmosphere.

\* Variation of pressure with depth



Subject :

Volume & density

$$\uparrow \sum F_z = 0$$

$$-P_2 (\Delta x \cdot \Delta y) + P_1 (\Delta x \cdot \Delta y) - W = 0$$

$$-P_2 (\Delta x \cdot \Delta y) + P_1 (\Delta x \cdot \Delta y) - (\Delta x \cdot \Delta y \cdot \Delta z) \cdot \rho \cdot g = 0$$

$W = \text{mass} \cdot g$

$W = m \cdot g$

$$= \rho (\Delta x \cdot \Delta y \cdot \Delta z) \cdot g$$

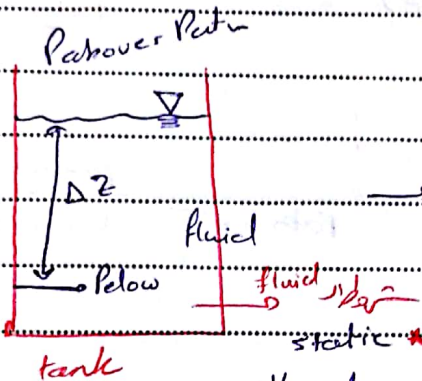
3D (vol)

$$-P_2 + P_1 - \rho \Delta z g = 0 \rightarrow$$

$$P_2 - P_1 = \rho \Delta z g = \Delta P$$

direction

\*



$$\rightarrow P_{\text{below}} = P_{\text{atm}} + \rho g |\Delta z|$$

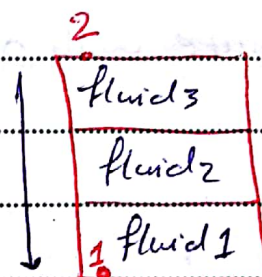
without variable density (constant density)

\* The pressure of a fluid at rest increases with depth (increasing linearly)

→ for variation of density with elevation

$$\Delta P_s = \rho g \Delta z$$

$$\lim_{\Delta z \rightarrow 0} \frac{\Delta P}{\Delta z} = -\rho g$$

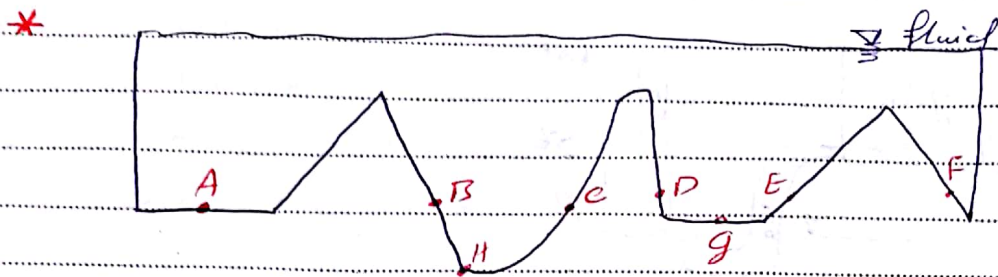


$$\frac{dP}{dz} = -\rho g \rightarrow \int -\rho g dz = \int dP$$

$$\Delta P_s = \int \rho g \cdot dz$$



Subject :



$$P_A = P_B = P_C = P_D = P_E = P_F \neq P_G \neq P_H$$

\* Note : pressure in a fluid at rest is independent of the shape or cross-sectional area of the container, it changes with vertical direction, constant in other direction.

\* 2.8 : Pressure measurement devices :-

1] The Barometer :- is used to measure the atmospheric pressure (barometric pressure).

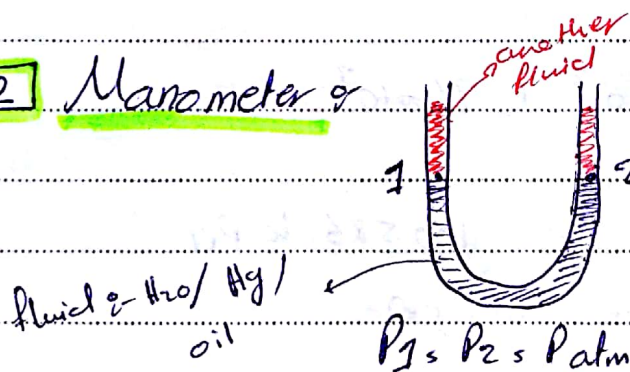
$$1 \text{ atm} \rightarrow 760 \text{ mm Hg}$$

$$1 \text{ torr} \rightarrow 760 \text{ mm Hg}$$

$$P_{\text{atm}} = \rho_{\text{Hg}} g \cdot \Delta z$$

$$\Delta z_{\text{water}} = 10.3 \text{ m}$$

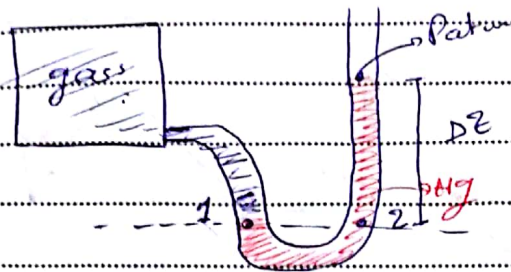
2] Manometer :-



The manometer is used to measure small pressure difference and consists of a glass or plastic with U-tube containing one or more fluids, like Hg, H<sub>2</sub>O, oil, etc -



\* Example 2



$P_1 = P_2$

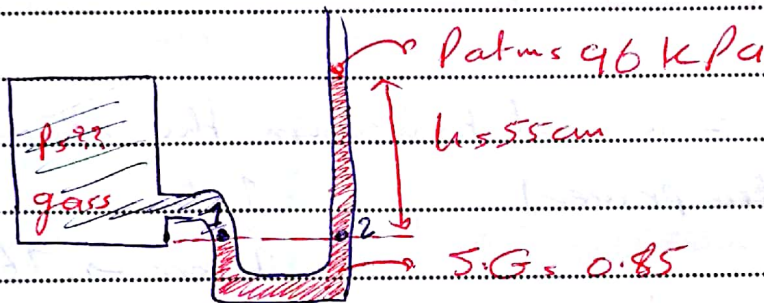
$P_1 = P_{\text{gage of gas}}$

$P_2 = \rho_{\text{MHg}} \cdot g \cdot \Delta z$

$P_{\text{gage gas}} = \rho_{\text{MHg}} \cdot g \cdot \Delta z$

$P_{\text{abs gas}} = P_{\text{atm}} + P_{\text{gage}}$

\* Ex 2



→ Determine the absolute pressure in tank?

→  $P_1 = P_2$

$P_1 = \text{Pressure tank}$

$P_2 = \rho \cdot g \cdot h + P_{\text{atm}}$

$$P_2 = 0.85 \times 1000 \times 9.81 \times 55 \times 10^{-2} + 96 \times 10^3$$

$$P_2 = 4.586 \times 10^3 + 96 \times 10^3$$

$$= 100.586 \times 10^3 \text{ Pa} \quad \text{or} \quad 100.586 \text{ kPa}$$

$$P_1 = P_2 = 100.586 \text{ kPa} \rightarrow \text{atm } 5.10$$

atm 11.2 is gage or 12)

Subject :

② و ④ بنوعه نقطه في الفتحه من 4

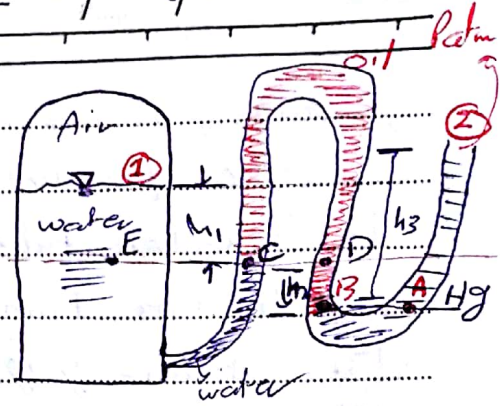
Note : داي غسبه اكله بنوعه  
النتاج في الفتحه discontinuity

\*Ex: water tank pressurized by air

$$P_{atm} = 85.6 \text{ kPa}, h_1 = 0.1 \text{ m}$$

$$h_2 = 0.2 \text{ m}, h_3 = 0.35 \text{ m}, \rho_{H_2O} = 1000 \text{ kg/m}^3$$

$$\rho_{oil} = 850 \text{ kg/m}^3, \rho_{Hg} = 13600 \text{ kg/m}^3$$



→ Determine the air pressure in the tank?

sol:  $P_A = P_B$  — (1)

$$P_C = P_D = P_E$$
 — (2)

$$P_A = P_2 + \rho_{Hg} g h_3$$
 — (3)

$$P_E = P_1 + \rho_{H_2O} g h_1$$
 — (4)

$$P_B = P_D + \rho_{oil} g h_2$$
 — (5)

→ sub eq (3) and eq (5) in eq (1):

$$P_A = P_B$$

$$P_2 + \rho_{Hg} g h_3 = P_D + \rho_{oil} g h_2$$
 — eq (6)

→ sub eq (4) in eq (6)

$$P_2 + \rho_{Hg} g h_3 = P_1 + \rho_{H_2O} g h_1 + \rho_{oil} g h_2$$

$P_{atm} =$

$$P_1 = P_2 + \rho_{Hg} g h_3 - \rho_{H_2O} g h_1 - \rho_{oil} g h_2$$

$$= 85.6 \times 10^3 + 13600 \times 9.81 \times 0.35 - 1000 \times 9.81 \times 0.1 - 850 \times 9.81 \times 0.2$$

$$P_1 = 129.6 \times 10^3 \text{ Pa or } 129.6 \text{ kPa}$$

absolute



→ other pressure measurements devices:-

- 1] Bourdon tube (gauge)
- 2] Pressure transducers
- 3] Strain-gages pressure transducers
- 4] Piezoelectric transducers

## \* Ch. 3 :- Energy transfer and Energy Analysis :-

### \* 3.1 :- Introduction :-

→ Conservation of energy :- Energy can't be created or destroyed during a process, it can only change from one form to another

### \* 3.2 :- Forms of Energy :-

\* Thermal, kinetic, potentials, nuclear, electrical, chemical, mechanical, magnetic

→ The sum of these forms (E) "Total Energy" (kJ)

$$e = \frac{E}{m} \quad \left( \frac{\text{kJ}}{\text{kg}} \right)$$

✓  
Energy Per unit mass

$$* \text{Kinetic Energy (K.E)} = \frac{mV^2}{2} \quad \text{or} \quad k.e = \frac{V^2}{2} \quad \left( \frac{\text{kJ}}{\text{kg}} \right)$$

► Subject :

\* Potential energy (P.E) =  $mgZ$  <sub>elevation</sub> or  $P.E = g.Z$

① \* The total Energy of a system is divided into two groups:-

① Macroscopic form of Energy:- These form are considered with respect to some outside reference frame such as kinetic and potential Energys

② Microscopic form of Energy:- These form are related to the molecular structure of the system and the degree of the molecular activity, and they are independent of outside reference frames

- The sum of all the microscopic forms of energy is called the internal energy of a system ( $U$ )

$$\rightarrow E = U + K.E + K.P \quad (kJ)$$

Per unit mass,

$$\rightarrow e = u + k.e + k.p \quad \left( \frac{kJ}{kg} \right)$$

→ The most closed systems are stationary system →

~~K.P~~  $K.E, P.E$  remain constant.  ~~$\Delta P.E$~~

$$\rightarrow \Delta P.E = 0,$$

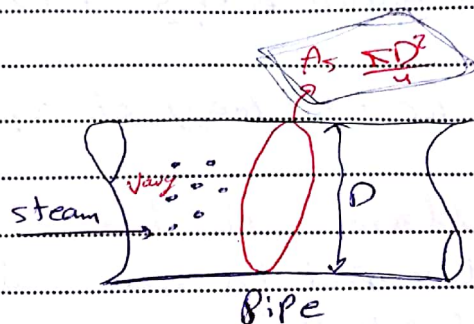
$$\rightarrow \Delta K.E = 0$$

$$\boxed{\Delta E = \Delta U}$$



open system (control volume)

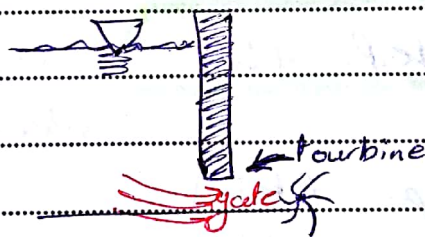
Mass flow rate  
 $\dot{m} = \rho \dot{V}$   
 $\text{kg/s} = \text{m}^3/\text{s} \times \rho$   
 $\text{in} = \rho \dot{V}$



Energy flow rate  $(\dot{E}) = \dot{m} e$  Energy per unit mass  
 $(\text{kJ/s}) \quad (\text{Watt})$

\* Mechanical Energy: The form of energy that can be converted to mechanical work completely and directly by an ideal mechanical devices, such as ideal turbine.

kinetic and potential energies are familiar form of mechanical energy.



\* The mechanical energy of a fluid can be expressed on a unit mass:

$$e_{\text{mech}} = \underbrace{\frac{V^2}{2}}_{\text{kinetic}} + \underbrace{gZ}_{\text{potential}} + \underbrace{\frac{P}{\rho}}_{\text{Pressure energy}}$$

Pressure  $= \frac{N}{m^2} = \frac{N \cdot m}{m^3} = \frac{J}{m^3}$  / Pressure density  $= \frac{J}{m^3} / \frac{kg}{m^3}$

Subject :

$$\dot{E} = \dot{m} \dot{e}_{\text{mech}} = \dot{m} \left( \frac{p}{\rho} + \frac{V^2}{2} + gz \right)$$

\* The mechanical energy changed of a fluid during incompressible ( $P = \text{constant}$ )

$$\Delta e_{\text{mech}} = \frac{P_2 - P_1}{\rho} + \frac{V_2^2 - V_1^2}{2} + g(z_2 - z_1) \quad (\text{kJ/kg})$$

$$\text{rate of energy} = \dot{E} = \dot{m} \Delta e_{\text{mech}} = \dot{m} \left( \frac{\Delta P}{\rho} + \frac{\Delta V^2}{2} + g \Delta z \right) \quad (\text{kW})$$

### \* 3.3 :- Energy Transfer by Heat :-

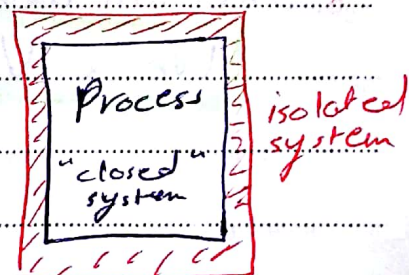
\* **Heat** :- The form of energy that is transfer between two systems or (system and it's surrounding) depends on temperature difference. ( $Q$ )

\* Heat per unit mass ( $q$ )  $\rightarrow q = \frac{Q}{m}$  (kJ/kg), rate of Heat transfer ( $\dot{Q}$ ) (kJ/s).

إجمالي انتقال الحرارة بالسرعة الزمنية  
 $Q = \int_{t_1}^{t_2} \dot{Q} dt$ , where  $\dot{Q}$  remains constant during process.

$$Q = \dot{Q} \Delta t$$

\* **Adiabatic process** :- A process during which there is not heat transfer between the system and surrounding.





### \* 3.4 :- Energy Transfer by work :-

\* Work is the energy transfer associated with a force acting through a distance. (Ex:- rising piston, rotating shaft)

→ work per unit mass ( $w$ )

$$w = \frac{W}{m} \left( \frac{\text{kJ}}{\text{kg}} \right)$$

→ power  $\dot{w} = \frac{W}{t}$  (kW)

chrg per unit time  $\xrightarrow{t_1} \dot{w} = \frac{W}{t}$  if it is constant  $\boxed{W = \dot{w} \Delta t}$

\* Heat and Work are directional quantities (Magnitude and direction)

→ Heat transfer to a system and work done by a system are positive

→ Heat transfer from a system and work done on a system are negative.

\* Electrical work ( $W_e$ ) :-

$$\boxed{W_e = VQ}$$

$V$  :- Potential diff & voltage

$Q$  :- electrical charge.

Subject: \_\_\_\_\_

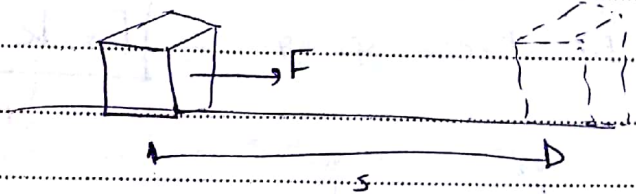
electrical power  $w_e$ :-  $w_e = UI$  (kwatt)  
change with time  $w_e = \int E V dt$

if  $I$  is constant  $\rightarrow w_e = UI \Delta t$  (kJ)

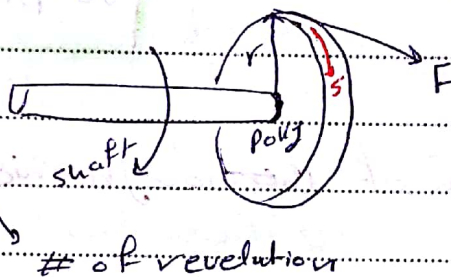
\* 3.5 :- Mechanical forms of work:-  
work (force acting through a distance)

$W = F \cdot S$   $\rightarrow$  if  $(F)$  is constant

if  $F$  is variable  $W = \int F ds$



\* Shaft work:-



$T = F \cdot r$  Torque.  $S = 2\pi r n$  revolution distance # of revolution

$W = F \cdot S$

$W_{\text{shaft}} = \frac{F}{r} \cdot 2\pi r n = T 2\pi n$  (kJ)

power of shaft  $\rightarrow w_{\text{shaft}} = 2\pi n T$  (kw)

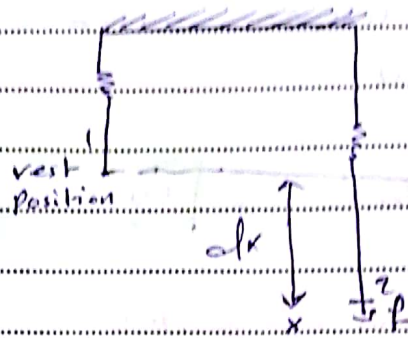
revolution per unit time (Angular speed) velocity



► Subject :

### \* Spring Work :

$$dw_{\text{spring}} = F \cdot dx$$

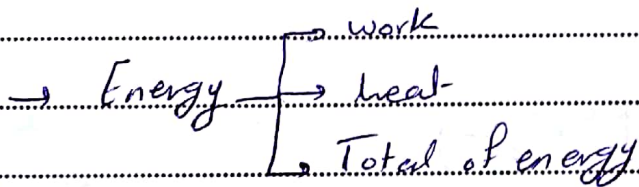


→ for linear spring →  $F = kx$  → distance

stiffness of spring (N/m)

$$\int_{w_1}^{w_2} dw = \int_{x_1}^{x_2} kx dx \rightarrow W_{\text{spring}} = \frac{1}{2} k x^2 \Big|_{x_1}^{x_2}$$
$$W_{\text{spring}} = \frac{1}{2} k (x_2^2 - x_1^2) \text{ (kJ)}$$

### \* 3.6 :- The first law of Thermodynamics :- (conservation of energy)



$$\text{Energy balance :- } \left( \text{Total energy entering the system} \right) - \left( \text{Total energy leaving the system} \right) = \left( \text{change in the total energy of the system} \right)$$

↳ net of energy transfer by Heat, work, mass of energy

↳ internal energy, potential energy, kinetic energy

$$E_{\text{in}} - E_{\text{out}} = \Delta E_{\text{system}}$$

► Subject :

\* change Energy change of the system  $\Delta E_{sys}$

$$\Delta E_{sys} = E_{\text{final state}} - E_{\text{initial state}}$$

$$\Delta E_{sys} = \Delta U + \Delta K.E + \Delta P.E$$

$$\Delta U = m(u_f - u_i) \quad \Delta K.E = \frac{m}{2}(v_f^2 - v_i^2) \quad \Delta P.E = mg(z_f - z_i)$$

$$\rightarrow E_{in} - E_{out} = \Delta E_{system}$$

$$(Q_{in} - Q_{out}) + (W_{in} - W_{out}) + (E_{mass, in} - E_{mass, out}) = \Delta E_{sys} \text{ (kJ)}$$

$$\rightarrow \text{Energy per unit mass} : E_{in} - E_{out} = \Delta e_{system} \text{ (kJ/kg)}$$

→ rate of form 1<sup>st</sup> law of thermodynamics:

$$\dot{E}_{in} - \dot{E}_{out} = \frac{dE_{sys}}{dt} \text{ (kW)}$$

\* Note :- For a closed system undergoing a cycle, initial state and final state are identical  $\rightarrow \Delta E_{sys} = 0 \rightarrow E_{in} = E_{out}$

$$\rightarrow W_{net, out} = Q_{net, in}$$

$$\dot{W}_{net, out} = \dot{Q}_{net, in}$$

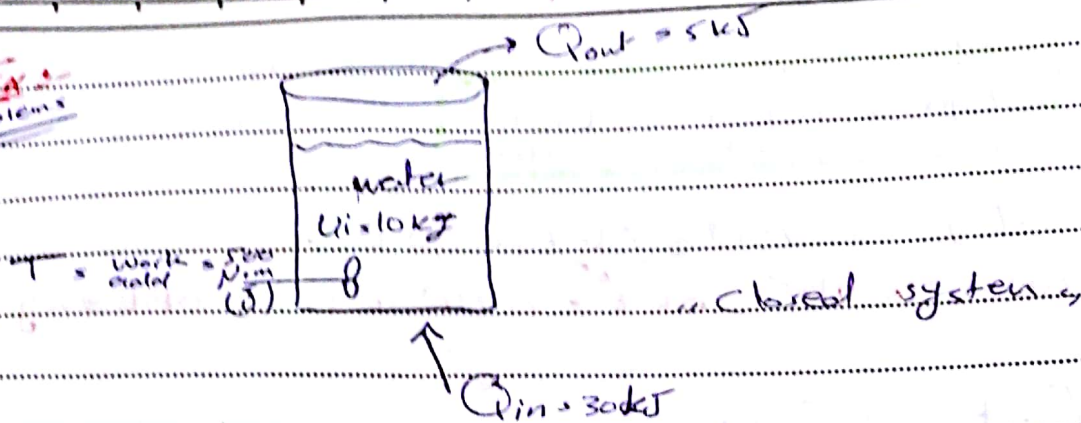
\* 3.7 :- Energy conservation efficiency :-

$$\eta = \frac{\text{Desired output}}{\text{Required input}}, \text{ coefficient of performance (COP)}$$



Subject :

\* Ex. Problems



Determine the final energy of the system if the initial energy is  $10 \text{ kJ}$ ?

sol:  $E_{in} - E_{out} = \Delta E_{sys} \rightarrow U_f - U_i$

$$(Q_{in} - Q_{out}) + (W_{in} - W_{out}) = \Delta U$$

$$(30 \times 10^3 - 5 \times 10^3) + (500 - 0) = U_f - 10 \times 10^3$$

$$U_f = 35500 \text{ J} \text{ or } 35.5 \text{ kJ}$$

## \* Ch. 4.1 :- Properties of pure substances :-

\* 4.1 :- Pure of substance :- a substance that has fixed chemical composition through its structure (water, nitrogen, helium, etc.).

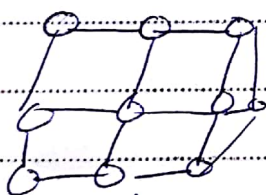
\* A mixture of different chemical elements may also be a pure substance as long as it is homogeneous. (Air is a mixture of several gases, because it has a uniform chemical composition).

\* A mixture of oil and water are not a pure substance.

## \* 4.2 :- Phase of pure substance :-

\* Phase :- is identified as a having a distinct molecular arrangement that is homogeneous throughout and separated from the others by easily identifiable boundary surface.

1 solid



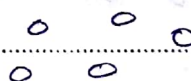
solid  
fixed

2 liquid



liquid moles  
free to relat  
and to translate

3 gas



gas molecules  
free with energy  
high



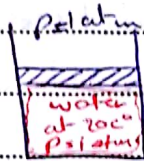
Subject :

→ intermolecular bonds is stronger in solid and weakest at gas

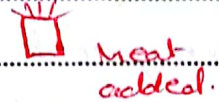
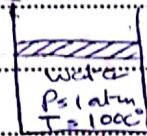
### \* 4.3 \* Phase change processes of pure substances:-

\* To understand the phase change process, consider a cylinder filled with water and piston to cover the cylinder.

\* **state 1**:- compressed liquid (subcooled liquid):-  
At  $20^\circ\text{C}$  and  $1\text{ atm}$  water exists in the liquid phase mean it is not about to vaporize.

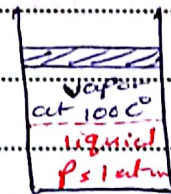


\* **state 2**:- (saturated liquid):- specific volume increase at constant pressure and a liquid that is about to vaporize



\* **state 3**:- saturated liquid-vapor mixture (mixture):-

The temperature remains constant at  $T = 100^\circ\text{C}$  while boiling and phase changing take place.



→ saturated vapor:-

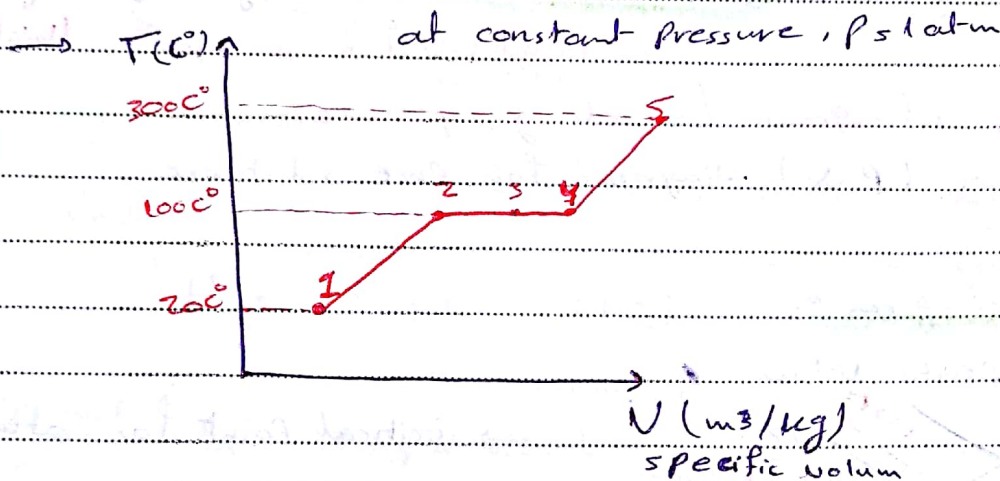
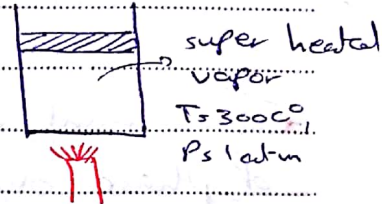
\* **state 4**:- Heating is still and the vaporization will continue until the last drop of liquid is vaporized, at this stage the cylinder contains only vapor at  $100^\circ\text{C}$  and  $1\text{ atm}$ . Any cooling process will cause some vapor

S T A R S N O T E B O O K

to condense to water.  
التكثيف



\* **state 5** - super heated vapor - a vapor which is not about to condense.



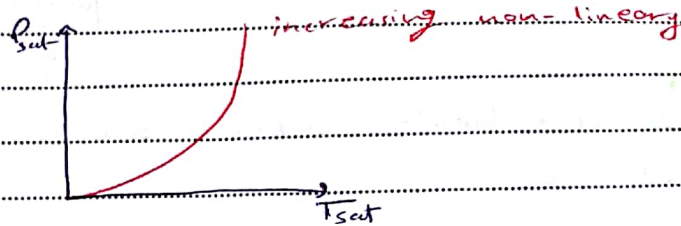
\* The temp. at which a pure substance change phase is called saturated temperature ( $T_{sat}$ ).

\* The pressure at which a pure substance change a phase is called saturated pressure ( $P_{sat}$ ).



Subject :

\* During phase change Temp and pressure are dependant on each other.  
 $T_{sat} = f(P_{sat})$



\* The amount of energy absorbed or released during process of phase change is called (latent heat).  $\Delta h = h_{fg} = h_g - h_f$   
 latent heat of vaporization gas fluid.

\* 4.4 :- Property diagrams for change phase:-  
 (T - V) and (P - V) diagrams for pure substance.

### The T - V diagram :-

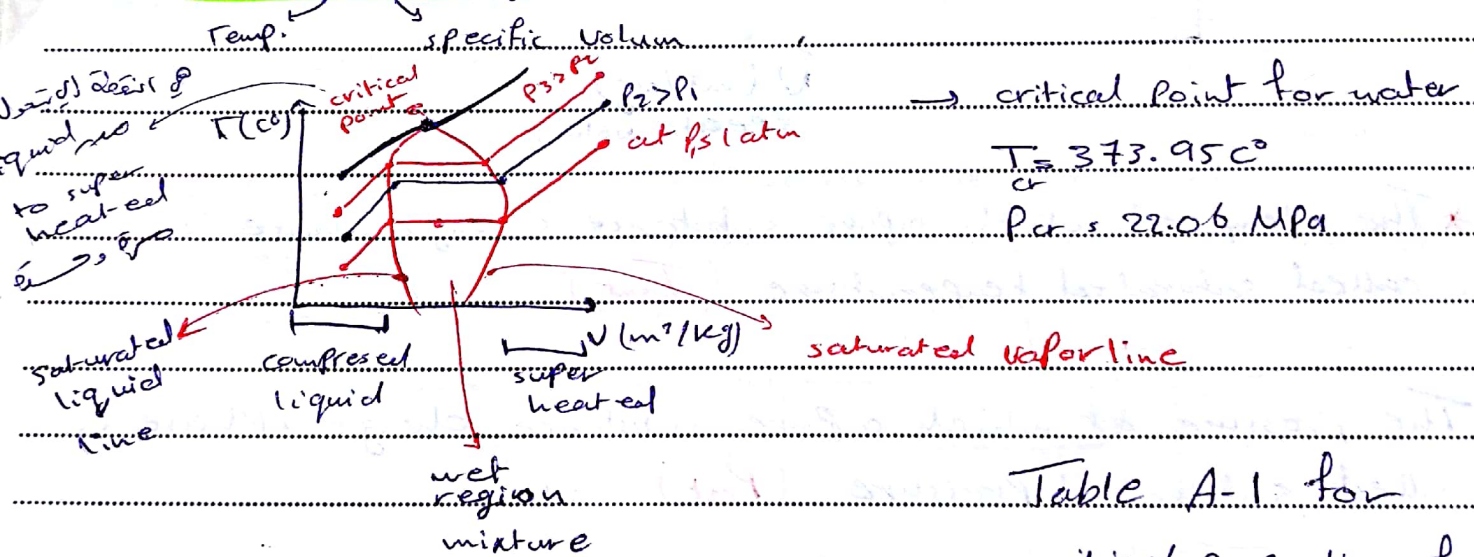


Table A-1 for  
 critical properties of  
 pure substance.

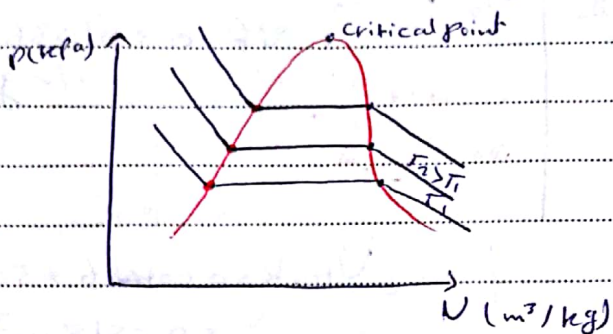
S T A R S N O T E B O O K

► Subject : .....

9 The P-V diagram is

pressure

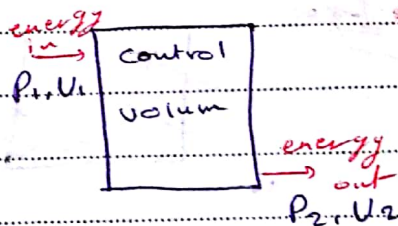
specific volume



\* 4.5 - Property Tables A-4, A-5  $\rightarrow$  for water.  $\checkmark$

**Enthalpy** - A combination property  
"heat content"

$$H = U + PV \quad (\text{KJ})$$



per unit  
→  
mass

$\mu = 1.4 \text{ pu} \quad (\text{kJ/kg})$

\*  $N_f$ : specific volume of sat liquid

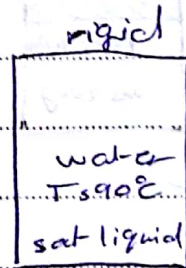
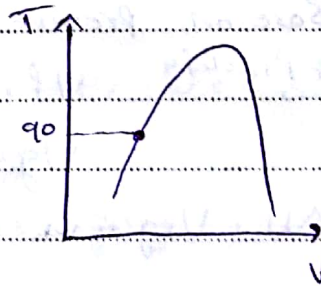
$\text{Ng} \rightarrow \dots \rightarrow \text{vapor}$

Ufg: difference between Ng and NF

ما یغیر از حجم

\* Ex:- A rigid tank contains 350 kg of saturated liquid water at  $90^\circ\text{C}$ .

Find the pressure in the tank and the volume of tank 2.





Subject :

from Table of water property :- (A-4), (A-5)

T	Psat	specific volume		
		$v_f$	$v_g$	$v_{fg}$
100	101.325 kPa			

$$v_f = 0.001036 \text{ m}^3/\text{kg}$$

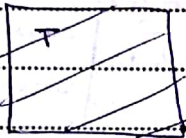
multiplied by 50  
to get 51.8 L

$$V_{\text{tank}} = 0.001036 \times 50 = 0.0518 \text{ m}^3$$

$$1 \text{ m}^3 \rightarrow 1000 \text{ L}$$

$$\rightarrow V_{\text{tank}} = 51.8 \text{ L}$$

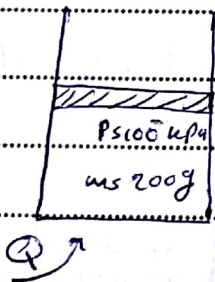
\* Ex :-



\* Ex :- A mass of 200g of saturated liquid water is completely vaporized at a constant pressure of 100 kPa.

- find :-
- ① The volume of change
  - ② The amount of energy transferred to the water.

① To find volume of change :- liquid  $\downarrow$  gas  
Pressure before  $\downarrow$  after



Base on pressure 100 kPa from table A-5  
at  $P_{100 \text{ kPa}}$

$$v_f = 0.001043 \text{ m}^3/\text{kg}$$

$$v_g = 1.6941 \text{ m}^3/\text{kg}$$

$$\Delta V = v_{fg} \times m = 1.6931 \times 200 \times 10^{-3}$$

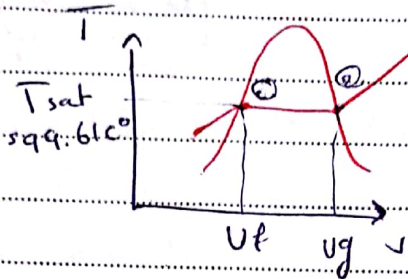
$$= 0.3386 \text{ m}^3$$

S T A R S N O T E B O O K

Subject :

(b)  $h_{fg} = 2257.5 \text{ kJ/kg}$

→  $Q = m h_{fg} = 200 \times 10^{-3} \times 2257.5 = 451.5 \text{ kJ}$



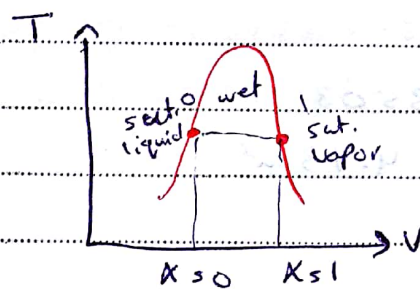
1-b saturated liquid-vapor mixture (wet region)

\* Quality (X) : The ratio of the mass of vapor to the total mass of mixture.

$$X = \frac{m_{\text{vapor}}}{m_{\text{total}}}$$

1-0 ratio (vapor)  
ratio (vapor)

$$0 < X < 1$$



$$\left[ \frac{p}{\rho} \right]$$

homogeneous mixture

homogeneous mixture

$$m_{\text{total}} = m_f + m_g$$

$$N_{\text{avg}} = V_f + V_g$$

$$V = m v$$

$$m_{\text{total}} V_{\text{avg}} = m_f v_f + m_g v_g$$

$$m_{\text{total}} V_{\text{avg}} = (m_{\text{total}} - m_g) v_f + m_g v_g$$

$$m_{\text{total}} V_{\text{avg}} = m_{\text{total}} v_f - m_g v_f + m_g v_g$$



Subject:

$$m_t v_{avg} = m_t v_f + m_g (v_g - v_f) \quad \text{--- } X$$

Divided by  $(m_t)$   $\rightarrow v_{avg} = v_f + \boxed{\frac{m_g}{m_t}} v_{fg}$  (X)

$$v_{avg} = v_f + X v_{fg}$$

$$V = m v$$

mass specific volume

--- a similar analysis gives:

$$* v_{avg} = v_f + X v_{fg}$$

$$* h_{avg} = h_f + X h_{fg}$$

\* Ex:- A rigid tank contains 10 kg of water at  $90^\circ\text{C}$  if 8 kg is in a liquid form and the rest is in vapor ~~vapor~~ form. Determine the pressure in the tank and the volume of the tank?

$\rightarrow$  From table A-4 at  $T = 90^\circ\text{C}$

$$P_{sat} = 70.183 \text{ kPa}$$

vapor	$m = 2 \text{ kg}$
liquid	$m = 8 \text{ kg}$

$T = 90^\circ\text{C}$

$$m_t v_{avg} = m_f v_f + m_g v_g \quad \text{(X)}$$

$$10 v_{avg} = 8(0.001036) + 2(2.3503)$$

$$v_{avg} = 0.473 \text{ m}^3/\text{kg}, \quad V = 4.73 \text{ m}^3$$

$$X = \frac{2}{10} = 0.2$$

$$v_{avg} = v_f + X v_{fg}$$

► Subject :

\*Ex:- An 80 L vessel contains 4 kg of Refrigerant R134a at pressure of 160 kPa. Determine (1) the temp. (2) the quality (3) the enthalpy (4) the volume occupied by the vapor phase.

→ From ~~table~~ table A-12 at  $P = 160 \text{ kPa}$ :-

[1]  $T_{\text{sat}} = -15.6^\circ\text{C}$

[2]  $X = \frac{V_{\text{avg}} - V_F}{V_{FG}} \rightarrow X = \frac{80 \times 10^{-3} - 0.007435}{(0.12355 - 0.0007435)} = 0.157$

[3]  $h_{\text{avg}} = h_F + X h_{FG}$

$h_{\text{avg}} = 31.18 + 0.157 \times 209.96$   
 $= 64.1 \text{ kJ/kg}$

[4]  $V_g \rightarrow$  from  $X \rightarrow$  mass of vapor  $\rightarrow m_g = 0.157 \times 4$   
 $= 0.628 \text{ kg}$

$V_g = m_g v_g = 0.628 \times 0.12355$

$V_g = 0.0775894 \text{ m}^3$



Subject:

### ② Super heated vapors:-

- compared to sat-vapor.
- lower pressure ( $P < P_{sat}$ ) at given Temp. → super heated
- higher temp. ( $T > T_{sat}$ ) at given pressure
- higher specific volume ( $U > U_g$ ) at given Temp. <sup>or</sup> pressure
- higher internal energy ( $U > U_g$ ) at give  $T$  and  $P$
- higher enthalpies ( $h > h_g$ ) at given  $T$  and  $P$

### ③ compressed liquid:-

- compared to sat-liquid.
- higher pressure ( $P > P_{sat}$ ) at given Temp.
- lower temp. ( $T < T_{sat}$ ) at give pressure.
- lower specific volume ( $U < U_f$ ) at given Temp. or pressure
- lower internal energy ( $U < U_f$ ) at given  $T$  or  $P$ .
- lower enthalpies ( $h < h_f$ ) at given  $T$  or  $P$

\* Note :- When no data available in compressed liquid table for water  $y \approx y_f$  at  $T$  for  $U_f$  and  $U_f$  → <sup>Press</sup> saturated liquid.

for  $h \rightarrow h \approx h_f @ T + U_f @ T (P - P_{sat} @ T)$

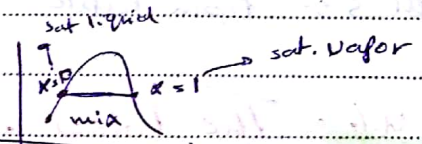
<sup>portant</sup>  
\* Ex :- Determine the missing properties and phase descriptions in the following table for water. →

Subject :

گشتی ۱۹ [۱] ریس و ال \*

#	TC°	P kPa	u (kJ/kg)	X	Phase
1	120.21	200	1719.26	0.6	mixture
2	125	232.23	1600	0.535	mixture
3	395.2 <del>379.88</del>	1000	2950		superheated vapor
4	75	500	313.99		compressed liquid
5	172.94	850	u <sub>f</sub> 731	0.0	sat. liquid

\* state 1:  $\rightarrow$   $x=0.6 \rightarrow$  mixture



$\rightarrow T \rightarrow$  دما

AS - at constant pressure

$\rightarrow$   $u_{avg} = u_f + x u_{fg}$

$$= 504.54 + 0.6 \times 2024.6$$

$$= 1719.26 \text{ kJ/kg}$$

\* state 2: table A4

$\rightarrow$   $u = 1600$  در mixture

دما  $u_f$  and  $u_{fg}$  را به دست آوریم

$\rightarrow$   $u_{avg} = u_f + x u_{fg}$

$$1600 = 524.83 + x \times 2009.5$$

$$\rightarrow x = 0.535$$

\* state 3: table A-5

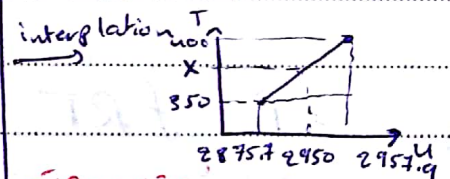
table A-5 به 3 درجه  $u_{avg}$  در

درجه  $P$  1 MPa در

$$2950 = u$$

$$@ T > 350^\circ \rightarrow u = 2875.7$$

$$T = 400^\circ \rightarrow 2957.9$$



تقریباً

$$\frac{400 - 350}{2957.9 - 2875.7} = \frac{x - 350}{2950 - 2875.7}$$

$$x = 395.2^\circ$$

$$x = 395.2^\circ$$



► Subject :

\* stat 4 :- from table A-4 :-

$P_{sat} = 38.597$  but  $P > P_{sat}$  → compressed liquid

→ from table A-7 → ~~compressible liquid~~

DSL Lines

Note :- from table A-7 at  $P = 500 \text{ kPa}$

does not exist so we back to table A-5 or A-4

→  $P = 500 \text{ kPa}$  is in table A-4

→ table A-4 @  $75^\circ\text{C}$  →  $u_f = 313.99 \text{ kJ/kg}$

\* stat 5 :- from table A-5

\* 4.6 :- The Ideal Gas Equation of state.

→ related to  $P$ ,  $V$  and  $T$  of a substance

$$P V = R T$$

↑  
absolute  
pressure  
(kPa)

↓  
specific  
volume  
( $\text{m}^3/\text{kg}$ )

→ Gas constant  
( $\text{kJ/kg} \cdot \text{K}$ )

Air → 0.287

He → 2.0769

Ar → 0.2081

N → 0.2968

OR

$$P = \rho R T$$

↑  
density  
of substance  
( $\text{kg}/\text{m}^3$ )

$$P V = m R T$$

↑  
mass (kg)

$$\rightarrow R = \frac{R_u}{M} \rightarrow \text{universal gas constant}$$

Molar  
mass ( $\text{kg}/\text{kmol}$ )

$$R_u = 8.314 \text{ kJ/kmol} \cdot \text{K}$$

x H.W 4.43

► Subject : .....

→ if constant mass →  $PV = nRT$  →  $\frac{PV}{T} = nR$  → constant

$$\boxed{\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}}$$



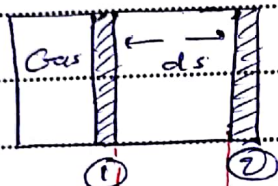
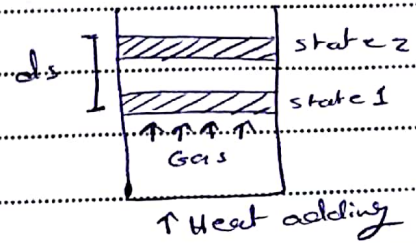
# Chapter 5: Energy analysis of closed systems

## Moving Boundary work:-

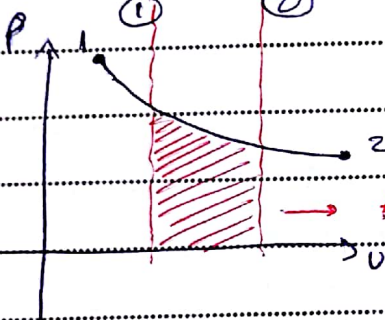
$$\sum w_b = \int_1^2 P \, dV$$

$$\sum w_A = P \, dV$$

Remark  $\rightarrow$   $F = P \times A$



for change (P) or constant (P)



Area under curve represent work (kJ)

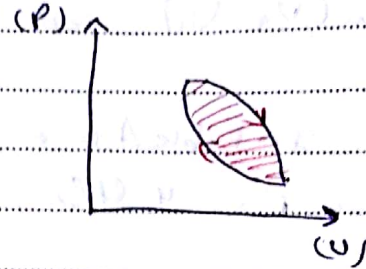
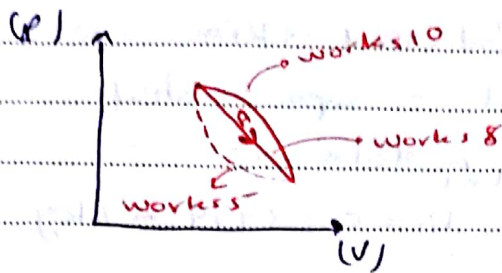
②  $P = f(V)$  "from P-V diagram"

The total Area under the ~~curve~~ <sup>Process</sup> 1  $\rightarrow$  2 is obtain by adding in differential areas:

## \* Note that:-

- 1) The Boundary work done during process depends on the path followed as well as end state.
- 2) The Net work during cycle the difference between the work done by the system & done ~~on~~ on system.

Subject :



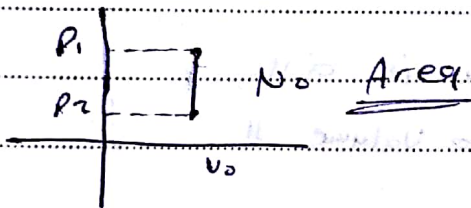
1 Expansion :-  $^+wb$  (work done by system)  
 piston cylinder

2 compression :-  $-wb$  (work done on system)  
 V constant

\*Ex: Rigid tank air  $P_1 = 500 \text{ kPa}$ ,  $T_1 = 150^\circ\text{C}$   
 $P_2 = 400 \text{ kPa}$ ,  $T_2 = 65^\circ\text{C}$

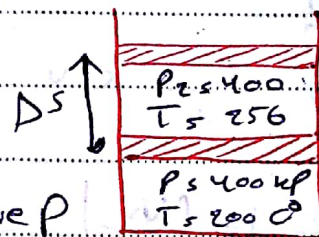
find the Boundary work done during process?

$\rightarrow wb = \int P dV$ , no change in volume work done is zero



\*Ex: piston cylinder 5kg of steam, find the work done by system during process?

$\rightarrow wb = \int P dV \rightarrow wb = P \Delta V$



$\rightarrow$  from table give S.U "A-4"  $\rightarrow$  give P

mass slipping



► **Subject :**

$$w_b = p_m (V_2 - V_1) \text{ at } t = 800 \text{ } p_{sat} = 1554.9 \text{ kPa}$$

$P < P_{\text{sat}}$  :- super heated

go table A-6 ← super ← state st.  
header

state (1)  $\rightarrow P = 0.4 \text{ MPa}$ ,  $t = 200^\circ\text{C}$ ,  $v = 0.53434 \text{ m}^3/\text{kg}$

state (2)  $\rightarrow$  The steam is superheated  $p < p_{sat}$

From table A-6

$P_2 = 0.4 \text{ MPa}$ ,  $t = 250$ ,  $U_2 = 0.59520 \text{ m}^3/\text{kg}$

$$W_b = 400 \times 10^3 (0.59520 - 0.53434) \times 5$$

$$W_b \approx 121.77 \times 10^3 \text{ J}$$

1.3) Air ← ideal gas ← ideal gas ← ideal gas

\* نواحی قدیمہ  
ideal  
goes

\*Ex: Piston cylinder  $V_1 = 0.4 \text{ m}^3$  of Air  $p_1 = 100 \text{ kPa}$ ,  $T_1 = 80^\circ\text{C}$   
compressed to  $\underbrace{0.1 \text{ m}^3}_{V_2}$  at constant temperature determine work  
boundary "isothermal system"

$$\rightarrow W_{B,1} = \int_1^2 P dv$$

→ air oils

ideal gas has no volume.

from ideal gas :-  $PV = nRT$   
(constant)

then  $\rho \in C$

$$\rightarrow W_B = \int_1^2 \frac{C}{v} dv = C \ln v \Big|_1^2 = C \ln \left[ \frac{v_2}{v_1} \right]$$

$$w_b s \leq \ln\left(\frac{V_2}{V_1}\right) \rightarrow w_b s \leq R_m T \ln\left(\frac{V_2}{V_1}\right)$$

↳ Remark:  $P_{mT} \leq P_{V1} \leq P_{V2}$

use this ✓

9 unknown

► Subject : \_\_\_\_\_

$$w_b = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$$

$$= (0.4)(100 \times 10^3) \ln\left(\frac{0.1}{0.4}\right)$$

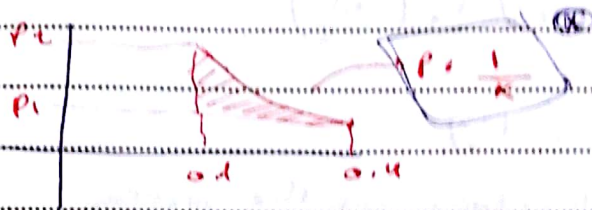
$$= \ominus 55.5 \text{ kJ}$$

↪ work done on the system



Subject :

Non linear graph is like Area under the curve



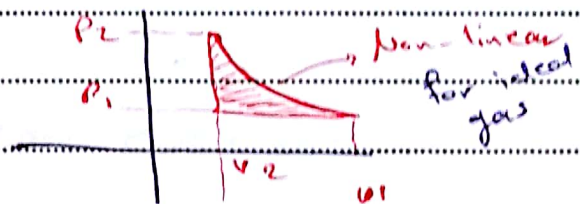
→ in ideal gas only suppose that  $PV = nRT$   
But during actual process of expansion of gas pressure volume are often related by:

$$PV^n = C \quad \text{where } n = \text{degree of poly tropic}$$

$C = \text{constant}$

→ Poly tropic Process:-  
 $P(V), P(V) \propto V^{-n}, P(V) \propto V^{-n}$

$$P \propto V^{-n} \quad (*)$$



→ work boundary:-

$$W_b = \int_1^2 P dV, \quad W_b = \int_1^2 C V^{-n} dV$$

$$W_b = C \frac{V_2^{-n+1} - V_1^{-n+1}}{-n+1} \rightarrow C \frac{V_2^{-n} V_2 - V_1^{-n} V_1}{-n+1}$$

$$W_b = \frac{P_2 V_2 - P_1 V_1}{-n+1} \rightarrow \frac{C V_2^{-n} \cdot V_2}{P_2}$$

$$= \frac{mRT_2 - mRT_1}{-n+1}$$

$$P \propto V^{-n}$$

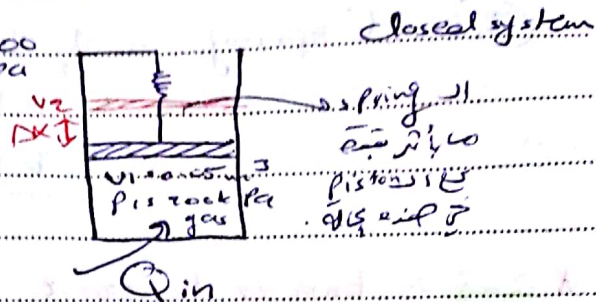
\* Ex:  $V_1 = 0.05 \text{ m}^3$  of gas at  $P_1 = 200 \text{ kPa}$

$K_{\text{spring}} = 150 \text{ kN/m}$

after  $Q_{\text{in}}$  the volume is double

$V_2 = 2V_1$

$A_{\text{piston}} = 0.25 \text{ m}^2$



Determine:- ① The final pressure inside the cylinder?

② The total work done by gas?

③ work done against the spring to compressed it?

$$\rightarrow \textcircled{1} F_s = k \Delta x, \quad \Delta U = A \Delta x \rightarrow \Delta V = 0.25 \Delta x$$

$$(0.1 - 0.05) = 0.25 \Delta x$$

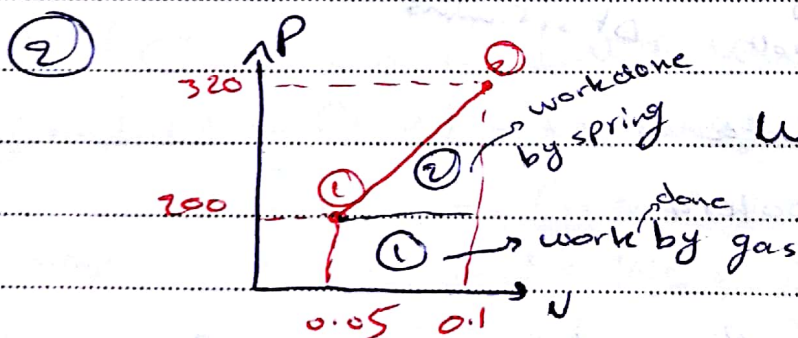
$$\Delta x = 0.2 \text{ m}$$

$$\rightarrow F_s = k \Delta x$$

$$= 150 \times 10^3 \times 0.2 = 30 \text{ kN}$$

$$\rightarrow P_s = \frac{F_s}{A} = \frac{30 \times 10^3}{0.25} = 120 \text{ kPa}$$

$$P_{\text{inside cylinder}} = P_s + P_{\text{gas}} = 120 \text{ kPa} + 200 \text{ kPa} = 320 \text{ kPa}$$



$$W = \int P dV$$

$$W_{\text{total}} = W_{\text{gas}} + W_{\text{spring}}$$

$$W_{\text{trapezoidal}} = \frac{1}{2} (320 + 200) \times 10^3 \times (0.1 - 0.05)$$

$$= 13 \text{ kJ}$$



Subject:  $E_{in} + E_{out} = \Delta E$  (win)  $\Delta m \cdot h \cdot e = P \cdot e$

$$\textcircled{3} W_{spring} = \frac{1}{2} k (x_2^2 - x_1^2)$$

$$= \frac{1}{2} \times 150 \times 10^3 (0.2^2 - 0)$$

$$= \boxed{3 \text{ kJ}}$$

\* S.2 :- Energy balance for closed system :-

→ from ch. 3 :-  $E_{in} - E_{out} = \Delta E$  (kJ)

$\underbrace{E_{in}}_{\substack{\text{net of energy} \\ \text{transfer} \\ \text{by heat} \\ \text{work} \\ \text{mass of energy}}} - \underbrace{E_{out}}_{\substack{\text{change in internal, kinetic,} \\ \text{potential, etc.}}} = \Delta E$

per unit mass →  $e_{in} - e_{out} = \Delta e$  (kJ/kg)

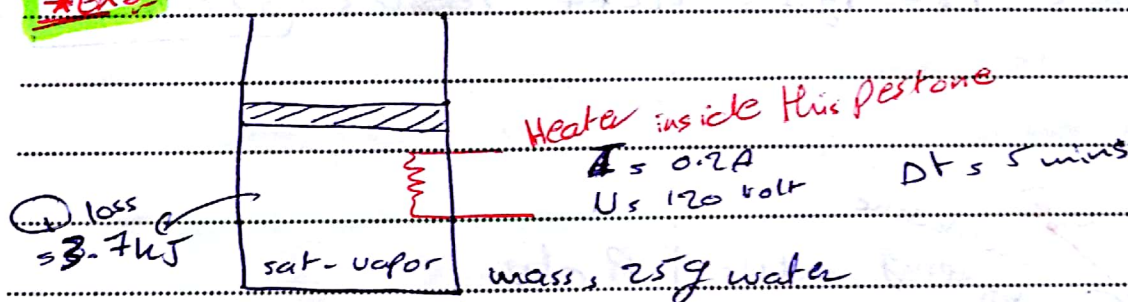
rate →  $\dot{E}_{in} - \dot{E}_{out} = \frac{dE}{dt}$

→ for closed system under goes a cycle :-

$$E_{in} = E_{out} = 0 \rightarrow Q_{in, net} = W_{out, net} = 0$$

$$(Q_{in} - Q_{out}) - (W_{out} - W_{in}) = 0$$

\* Exo



at constant pressure = 300 kPa

→ Piston cylinder  $m = 25 \text{ g}$ ,  $P = 300 \text{ kPa}$ , sat-vapor.

$I = 0.2 \text{ A}$ ,  $U = 120 \text{ volt}$  for  $t = 5 \text{ mins}$ , heat loss = 3.7 kJ

Subject :

→ final :- (a) Show that for a closed system the boundary work and the change in the internal energy ( $\Delta U$ ) in the first law relation can be combined into one term ( $\Delta H$ ) for constant pressure?

(b) determine the final Temp. of the system?

→ sol :- (a)  $Q_{net, in} - W_{net, out} = \Delta U + \Delta KE + \Delta PE$   
 $Q_{net, in} - (W_{boundary} + W_{electrical}) = \Delta U$   
 $Q_{net, in} - (P_0(V_2 - V_1) + W_e) = \Delta U$   
 $Q_{net} - P_0(V_2 - V_1) + W_e = \Delta U$  (PV)  
 $Q_{net} - W_e = \Delta U + P_0(V_2 - V_1)$   
 $Q_{net} - W_e = \Delta U + P_0 \Delta V$   
#  $Q_{net} - W_e = \Delta H$   $\rightarrow H_2 - H_1$  (kJ)  
for constant pressure.

(b) state 1 :- (a)  $P_s = 300$  kPa and sat - vapor  $\rightarrow h_{1g} = 2724.9$  kJ/kg  
from table A-5 @  $P_s = 300$  kPa

→  $W_e = IV \Delta t = 0.2 \times 120 \times 5 \times 60 = 7.2$  kJ

$Q_{net, in} - W_{net, out} = \Delta U$

$(Q_{in} - Q_{out}) - (W_{out} - W_{in}) = \Delta U$

$(0 - Q_{out}) - (W_{boundary} - W_{electrical}) = \Delta U$

$- Q_{out} - P_0(V_2 - V_1) + W_e = \Delta U$

$- Q_{out} + W_e = \Delta H$

$- 3.7 \times 10^3 + 7.2 \times 10^3 = 2724.9 + 25 \times 10^3 (h_2 - 2724.9)$

$h_2 = 2864.9$  kJ/kg

S T A R S N O T E B O O K



Subject :

from table A-5 @  $P_s = 300 \text{ kPa}$

$$h_f = 561.43 \text{ kJ/kg}$$

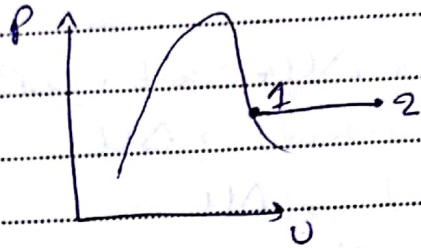
$$h_{gs} = 2724.9 \text{ kJ/kg}$$

state ② super heated

from table A-6 @  $P_s = 300 \text{ kPa}$

$$h_s = 2864.9$$

$$T = 200^\circ\text{C} \text{ at } P = 0.3 \text{ MPa}$$



for constant pressure

### \* 5.3 - specific heat - الحرارة النوعية

→ Energy required to rise the Temperature of a unit mass of a substance by one degree.

↳ Two kinds of specific heat :-

① specific heat at constant volume (CV)

$$C_P > C_V$$

② specific heat at constant pressure (CP)

→  $C_V = \frac{du}{dT}$  | internal energy at constant volume

→  $C_P = \frac{dh}{dT}$  | at C. Pressure

↳  $h = u + Pv$

$dh = du + Pdv + vdp$

→ unit for CV :  $\frac{\text{kJ}}{\text{kg} \cdot ^\circ\text{C}}$  or  $\frac{\text{kJ}}{\text{kg} \cdot \text{K}}$

Subject :

\* 5-4 = Internal Energy, enthalpy, specific heats of Ideal gas :-

per unit mass

$$PV = RT$$

$$u = u(T)$$

$$h = u + PV$$

$$h = u + RT$$

du = Cv dT  
dh = Cp dT

The differential changes in the internal energy and enthalpy  $h$  of an ideal gas

$$\int du = \int C_v dT \rightarrow \Delta u = \int C_v dT$$

$$\int dh = \int C_p dT \rightarrow \Delta h = \int C_p dT$$

for small intervals

$$\Delta u = C_{v,avg}(\Delta T)$$

$$\Delta h = C_{p,avg}(\Delta T)$$

$$\frac{C_{v,avg}}{C_{p,avg}} \rightarrow \text{at } \frac{T_1 + T_2}{2}$$

From Table (A-2) 15

from

$$h = u + RT$$

$$dh = du + R dT$$

$$C_p dT = C_v dT + R dT$$

$$C_p = C_v + R$$

S T A R S N O T E B O O K



Subject :

specific heat ratio ( $k$ ) =  $\frac{C_p}{C_v}$

for Air  $k = 1.4$

\* 5-5:- Specific heat,  $u$  and  $h$  for solid and liquid:-

$C_v = C_p = C$  from table (A-3)

$$\int_1^2 du = \int_1^2 C dt \rightarrow \Delta u = \int_1^2 C(T) dt \rightarrow \Delta u = C_{avg} \Delta T$$

at  $T_1$  &  $T_2$

$h = u + Pv$  zero for solid and liquid

$$dh = du + Pdv + vdp$$
$$dh = du + vdp$$

$$\Delta h = \Delta u + v \Delta P \Rightarrow \Delta h = C_{avg} \Delta T + v \Delta P$$

for solid or  $\Delta P = \text{Zero} \rightarrow \Delta h = C_{avg} \Delta T$

for liquid or  $\rightarrow$  constant ( $P$ )  $\rightarrow \Delta h = C_{avg} \Delta T$

$\rightarrow$  constant ( $T$ )  $\rightarrow \Delta h = v \Delta P$

Subject: Ch. 6.

Open system

## \* Ch. 6:- Mass and energy analysis of control volume

### \* 6-1:- Conservation of mass:-

→ For closed system required that the mass of the system remains constant during process.

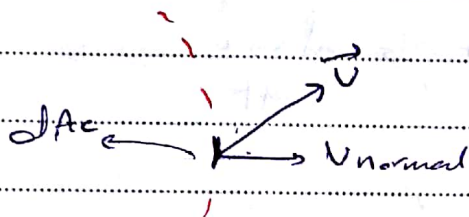
→ For control volume (<sup>open system</sup> control volume) mass can cross boundaries, so mass in and mass out need to be tracked.

### \* Mass and volume flow rules:-

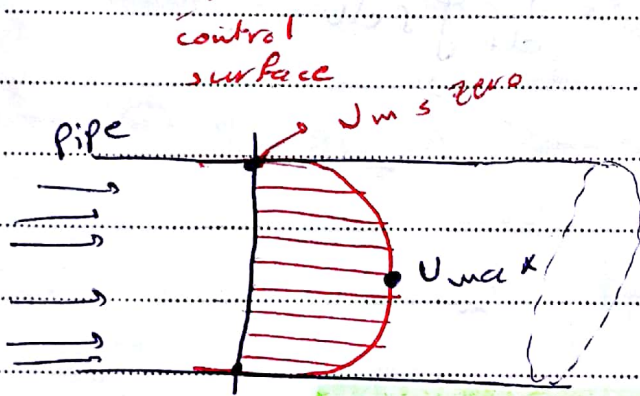
↳ mass flow rate:- the amount of the mass flowing

(i) through a cross section per unit time (kg/s)

(ii) → the amount of the volume flowing through — (m<sup>3</sup>/s)



$$\int_{A_c} \dot{m}_{in} = \int_{A_c} \rho U_n dA_c \rightarrow \dot{m}_{in} = \int_{A_c} \rho U_n dA_c \quad (\text{kg/s})$$



→ Average velocity

$$U_{avg} = \frac{1}{A_c} \int_{A_c} U_n dA_c$$

⚡ \*  $\dot{m}_{in} = \int U_{avg} A_c$



Subject:

Navg A

\* Volume flow rate ( $\dot{V}$ )  $\rightarrow \dot{V} = \int V_n dA \quad (m^3/s)$

in general  $\dot{V} = V_{avg} A_c$

mass = density \* volume

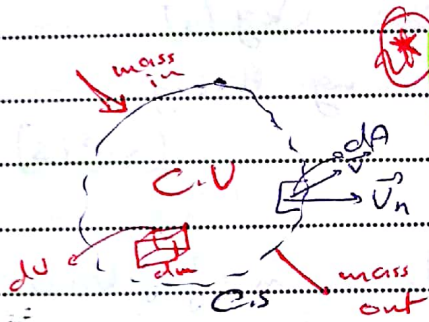
rate  $\dot{m} = \rho \dot{V}$  or  $\dot{m} = \frac{\dot{V}}{V} = \frac{m^3/s}{m^3/kg} = \frac{kg}{s}$

specific volume

zero at steady state

conservation of mass principle:

(Total mass entering the C.V. during  $\Delta t$ ) - (Total mass leaving the C.V. during  $\Delta t$ ) = (net change of mass within the control volume during  $\Delta t$ )



$\dot{m}_{in} - \dot{m}_{out} = \frac{dm_{cv}}{dt}$  mass balance

rate  $\dot{m}_{in} - \dot{m}_{out} = \frac{dm_{cv}}{dt}$

total mass within C.V.  $\rightarrow m_{cv} = \int \rho dV$

rate of change of mass within the C.V.

$\frac{dm_{cv}}{dt} = \frac{d}{dt} \int \rho dV$

from mass balance:

$\sum \dot{m}_{in} - \sum \dot{m}_{out} = \frac{dm_{cv}}{dt}$

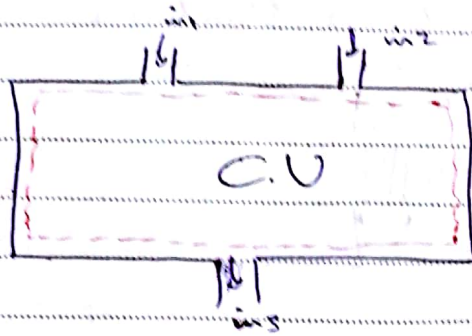
special case: if the system is steady state

$\frac{dm_{cv}}{dt} = \text{zero}$ ,  $\sum \dot{m}_{in} = \sum \dot{m}_{out}$

$\rho_1 \dot{V}_1 = \rho_2 \dot{V}_2$

$\rho_1 V_1 A_1 = \rho_2 V_2 A_2$

S T A R S N O T E B O O K

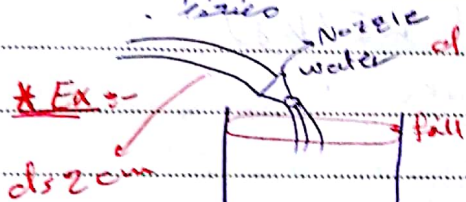


$\dot{m}_{in1} + \dot{m}_{in2} = \dot{m}_{in3}$

(\*)

in compressible flow  $\sum \dot{m}_{in} = \sum \dot{m}_{out}$ ,  $\sum \dot{V}_{in} = \sum \dot{V}_{out}$

Compressible flow  $\sum \dot{m}_{in} = \sum \dot{m}_{out}$ ,  $\sum \dot{V}_{in} \neq \sum \dot{V}_{out}$



So sec to fill the Bucket

① determine the volum and mass flow rate of the water through the pipe?

→ ② the average velocity of water at the nozzle exist?

sol:- ①  $\dot{V} = \frac{V}{t} = \frac{40}{50} = 0.8 \text{ L/sec or } 0.8 \times 10^{-3} \text{ m}^3/\text{s}$

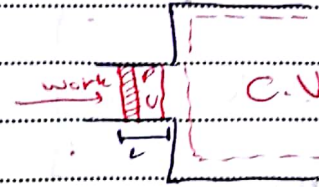
→  $\dot{m} = \rho \dot{V} = 1000 \times 0.8 \times 10^{-3} = 0.8 \text{ kg/s}$

②  $\dot{V} = V_{avg} A_{nozzle} \rightarrow 0.8 \times 10^{-3} = V_{avg} \times \frac{\pi}{4} (d_{nozzle})^2$   $\rightarrow V_{avg} = 15.9 \text{ m/s}$



## \* 6.2: Flow work and energy of a flowing fluid:-

→ flow work:- is the energy needed to push a fluid in to or out of a control volume.



$$F = PA \quad \text{flow} \quad W = F \cdot L \Rightarrow W = PA \cdot L$$

$$\text{Pressure} \quad \text{Area} \quad \text{Flow} \quad W_{\text{flow}} = P \cdot V \quad \text{volume} \quad (\text{kJ})$$

$$\text{rate (per unit mass)} \Rightarrow W_{\text{flow}} = P \cdot v \quad (\text{kJ/kg})$$

specific volume

$$\text{* Total energy } (e) = u + k.e + p.e$$

$$= u + \frac{v^2}{2} + gz \quad (\text{kJ/kg})$$

→ Add flow energy to total energy of a flowing fluid:

$$\text{total energy} \quad \text{flow energy} \quad \theta = P \cdot V + e$$

$$\theta = P \cdot V + u + \frac{v^2}{2} + gz$$

$$\text{*} \quad \theta = h + \frac{v^2}{2} + gz$$

$$\text{* Energy transport by mass} \rightarrow \dot{E}_{\text{mass}} = \dot{\theta}_{\text{in}} = \dot{m} (h + k.e + p.e)$$

$$\text{rate of energy transport} \rightarrow \dot{E}_{\text{mass}} = \dot{\theta}_{\text{in}} = \dot{m} (h + k.e + p.e)$$

(kJ/s)  
(kWatt)

Subject :

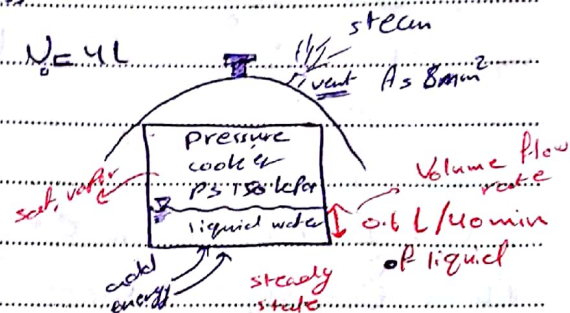
② = 47 kcal

\* O s h a k e P.E

↳ total energy of flow per unit mass

\* Ex:-

→ Determine:- ① mass flow rate of the steam exist and velocity?



② The total energy and flow energy of the steam per unit mass?

③ The rate at which energy leaves the cooker by the steam?

→ ① mass balance:-  $\dot{m}_{in} - \dot{m}_{out} = \frac{dm}{dt}$  zero (steady state)  
 $\dot{m}_{in} = \dot{m}_{out}$

$$\dot{V}_f = \frac{0.6 \times 10^{-3}}{40 \times 60} \Rightarrow \dot{m}_f = \rho_f \dot{V}_f$$

$$\dot{m}_f = \frac{\dot{V}_f}{v_f}$$

$$\rightarrow \dot{m}_f = \frac{25 \times 10^{-8}}{0.001053}$$

$$= 2.37 \times 10^{-4} \text{ kg/s}$$

from tables at  $P_s = 150 \text{ kPa}$   
 $v_f = 0.001053 \text{ m}^3/\text{kg}$   
 $v_g = 1.1594 \text{ m}^3/\text{kg}$

$$\rightarrow \dot{m}_g = 2.37 \times 10^{-4} \text{ kg/s}$$

$$\rightarrow \dot{m}_g = \rho_g \dot{V}_g$$

$$2.37 \times 10^{-4} = \frac{\dot{V}_g A_g}{v_g} \Rightarrow \dot{V}_g = ?$$

$$2.37 \times 10^{-4} = \frac{\dot{V}_g \times 8 \times 10^{-6}}{1.1594} \Rightarrow \dot{V}_g = 34.3 \text{ m/s}$$

leaving

S T A R S N O T E B O O K



Subject: \_\_\_\_\_

stream is at  
height  
velocity

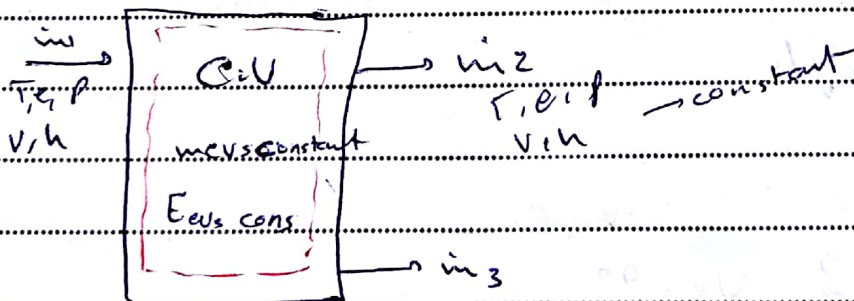
②  $\dot{Q} = \dot{m} \left( h + \frac{V^2}{2} + g z \right)$   
 $\dot{Q} = \dot{m} h_g \rightarrow$  from the table  
 for the steam  $h_g = 2693.1 \text{ kJ/kg}$

flow energy  
 $\dot{Q} = \dot{m} (Pv + u + \frac{V^2}{2} + g z)$   
 $Pv = \dot{Q} - \dot{m} u \rightarrow$  for steam  
 $= 2693.1 - 2519.2 \text{ kJ/kg}$   
 $= 173.9 \text{ kJ/kg}$

③  $\dot{E}_{\text{steam}} = \dot{m} \dot{Q}$   
 $= 2.37 \times 10^{-4} \times 2693.1 = 0.638 \text{ kW}$

### \* 6.3 - Energy analysis of steady flow systems

→ under S.S conditions, the mass, energy contents of a control volume remain constant, the fluid properties at an inlet or exit remain constants



mass balance:

$$\dot{m}_{in} = \dot{m}_{out} \rightarrow S.S$$

Subject 2 energy balance:  $\dot{E}_{in} = \dot{E}_{out}$   $\dot{Q}_{in} + \dot{W}_{in} + \sum \dot{E}_{in} = \dot{Q}_{out} + \dot{W}_{out} + \sum \dot{E}_{out}$  (h.k.e.p.e) (h.k.e.p.e)

→ The mass balance for S.S.P.:

$$\sum \dot{m}_{in} - \sum \dot{m}_{out} = \frac{dm}{dt} \xrightarrow{zero} \boxed{\sum \dot{m}_{in} = \sum \dot{m}_{out}}$$

$$\rho_1 U_1 A_1 = \rho_2 A_2 U_2$$

→ Energy balance:

$$\dot{E}_{in} - \dot{E}_{out} = \frac{dE}{dt} \xrightarrow{zero} \boxed{\dot{E}_{in} = \dot{E}_{out}}$$

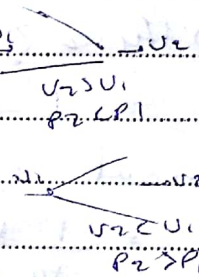
$$\dot{Q}_{in} + \dot{W}_{in} + \sum \dot{E}_{in} = \dot{Q}_{out} + \dot{W}_{out} + \sum \dot{E}_{out} \quad (kW)$$

\* 6-4 = steady flow devices:  $\rho = \rho_1$

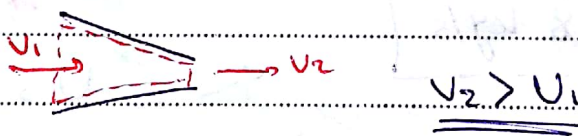
1 Nozzle and Diffuser:

Decreasing Area

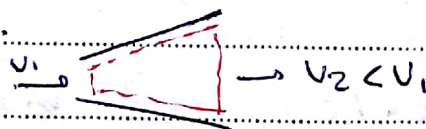
increasing Area



\* Nozzle is a device that used to increase the velocity of fluid



\* Diffuser is a device that used to increase the pressure of a fluid by slowing it down.

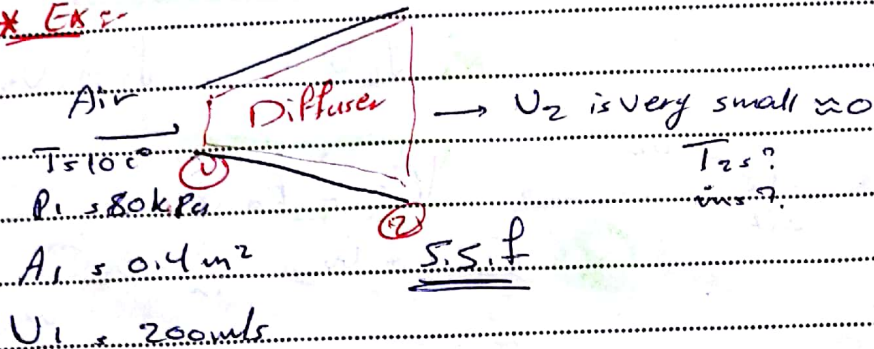




Subject:

\* Nozzle and Diffuser are adiabatic (Q=0), (Δk.e=0), (Δp.e=0), (ΔU=0)

\* Ex:-



- Determine ① The mass flow rate of Air ?  
 ② The Temperature of Air leaving the Diffuser ?

→ ①  $\dot{m}_{in} = \dot{m}_{out} = \rho_1 U_1 A_1$  → from ideal gas law

$$= \frac{1}{V_1} U_1 A_1$$

$$= \frac{1}{1.015} \times 200 \times 0.4$$

$$= 78.8 \text{ kg/s}$$

$$80 \times 10^3 \text{ N} = 287 \times (10 + 273)$$

$$V = 1.015 \text{ m}^3/\text{kg}$$

$$U = 1.015 \text{ m}^3/\text{kg}$$

②  $E_{in} = E_{out}$

$$\dot{Q}_{in} + \dot{W}_{in} + \sum \dot{m}_{in} (h + k.e + p.e) = \dot{Q}_{out} + \dot{W}_{out} + \sum \dot{m}_{out} (h + k.e + p.e)$$

$$\sum \dot{m}_{in} (h + k.e + p.e) = \sum \dot{m}_{out} (h + k.e + p.e)$$

► Subject :

$$\rightarrow h_2 = h_1 + k.e$$

$$h_2 = h_1 + \frac{V_1^2}{2}$$

$$= 283.14 + \frac{(200)^2}{2}$$

$\rightarrow h_1$  at  $T_s 100^\circ$  from table A-21

$T = 283 \text{ K}$  for air

$$h_1 = 283.14 \text{ kJ/kg}$$

$$h_2 = 303.14 \text{ kJ/kg}$$

$\rightarrow$  from table A-21 at  $T_s 303.14$

$\rightarrow T = 303 \text{ K}$

$T_s 30^\circ \text{C}$

\* Ek :-

$$Q_{\text{loss}} = 25 \text{ kW}$$

steam  $\rightarrow$  Nozzle  $\rightarrow T_2 = 300^\circ \text{C}$   
 $T_1 = 400^\circ \text{C}$  (1)  $\xrightarrow{\text{condition}}$  (2)  $P_2 = 200 \text{ kPa}$

$P_1 = 800 \text{ kPa}$  s.s. flow

$$V_1 = 10 \text{ m/s}$$

$$A_{\text{nozzle}} = 800 \text{ cm}^2$$

$\rightarrow$  Determine : (1) The velocity and ~~the~~ volum flow rate of the steam at exist

$\rightarrow$  in in, out

$$\rho_1 V_1 A_1 = \rho_2 V_2 A_2$$

$$\frac{V_1 A_1}{V_{\text{specific}_1}} = \frac{V_2 A_2}{V_2}$$

$$\rightarrow \dot{E}_{\text{in}} - \dot{E}_{\text{out}} = \frac{dE}{dt}$$

$$\dot{Q}_{\text{in}} + \dot{W}_{\text{in}} + \dot{m}_{\text{in}} \left( h_1 + k.e + p.e \right) = \dot{Q}_{\text{out}} + \dot{W}_{\text{out}} + \dot{m}_{\text{out}} \left( h_2 + k.e + p.e \right) + \dot{Q}_{\text{loss}}$$

$$\dot{m}_{\text{in}} \left( h_1 + k.e + p.e \right) = \dot{m}_{\text{out}} \left( h_2 + k.e + p.e \right) + \dot{Q}_{\text{loss}}$$

$$\dot{m}_{\text{in}} \left( h_1 + \frac{V_1^2}{2} \right) = \dot{Q}_{\text{out}} + \dot{m}_{\text{out}} \left( h_2 + \frac{V_2^2}{2} \right)$$



Subject: →

Nozzle

steam

superheated

from table A-5 at  $P = 800 \text{ kPa}$ ,  $T > T_{\text{sat}} \rightarrow$  superheated  
go to table A-6 @  $P = 0.8 \text{ MPa}$  }  $h_1 = 3267.7 \text{ kJ/kg}$   
 $T = 400^\circ\text{C}$  }  $v_1 = 0.38429 \text{ m}^3/\text{kg}$

from table A-5 at  $P = 200 \text{ kPa}$ ,  $T > T_{\text{sat}} \rightarrow$  superheated  
go to table A-6 @  $P = 0.2 \text{ MPa}$  }  $h_2 = 3072.1 \text{ kJ/kg}$   
 $T = 300^\circ\text{C}$  }  $v_2 = 1.31623 \text{ m}^3/\text{kg}$

in = out

$$\frac{v_1 A_1}{v_1} = \frac{v_2 A_2}{v_2}$$

$$\text{in} = \frac{100 \times 800 \times 10^{-4}}{0.38429} = 2.082 \text{ kg/s}$$

$$\dot{Q}_{\text{loss}} = 2.082 \left( 3267.7 \times 10^3 + \frac{10^2}{2} \right) - 2.082 \left( 3072.1 \times 10^3 + \frac{v_2^2}{2} \right)$$

$$v_2 = 606 \text{ m/s}$$

$$\dot{V}_2 = v_2 A_2 \quad \text{and} \quad \dot{m}_2 = \frac{\dot{V}_2}{v_2} \rightarrow \dot{V}_2 = 2.74 \text{ m}^3/\text{s}$$

## \* [2] Turbines and Compressors

\* Turbine:- devices that use to drive the electric generator.  $\dot{Q} \approx 0$ ,  $\Delta P.e \approx 0$ ,  $\Delta k.e \neq 0$

Subject :

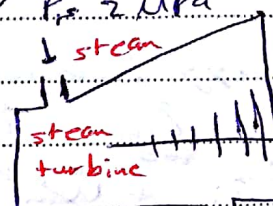
\* compressor :- a device that used to increase the pressure up to high pressure. (for gas only)



Pumps :- similar to compressor but for liquid only  
 $\Delta P > 0$  ,  $\Delta K > 0$  ,  $\dot{Q} = 0$

\* Ex :- Adiabatic steam turbine without power 5 MW.

$V_1 = 50 \text{ m/s}$  /  $T_1 = 400^\circ \text{C}$  /  $P_1 = 2 \text{ MPa}$   
 $z_1 = 10 \text{ m}$



→ find :- ①  $\Delta h$ ?

②  $\Delta K$ ?

③  $\Delta P$ ?

④ work done per unit mass of steam?

⑤ Mass flow rate?

$P_2 = 15 \text{ kPa}$

$x_2 = 0.9$

$V_2 = 180 \text{ m/s}$

$z_2 = 6 \text{ m}$

① →  $\Delta h$  <sup>mass</sup> tables <sub>size</sub>

from table A-5 @  $P_1 = 2 \text{ MPa}$  ,  $T_1 = 400^\circ \text{C}$  → super-heated  
go to table A-6 @  $P_1 = 2 \text{ MPa}$  ,  $T_1 = 400^\circ \text{C}$  }  $h_1 = 3248.4 \text{ kJ/kg}$

→  $h_2 = h_f + x h_{fg}$  → kJ/kg <sub>mixture</sub>

from table A-5 @  $P_2 = 15 \text{ kPa}$  →  $h_f = 225.94 \text{ kJ/kg}$

$h_{fg} = 2372.3 \text{ kJ/kg}$



Subject :

$$h_2 = 225.94 + 0.9 \times 2372.2$$

$$h_2 = 2361.01 \text{ kJ/kg}$$

$$\rightarrow \Delta h = h_2 - h_1 = -887.39 \text{ kJ/kg}$$

$$\textcircled{2} \Delta k.e = \frac{V_2^2}{2} - \frac{V_1^2}{2} = \frac{180^2}{2} - \frac{50^2}{2} = 14.95 \text{ kJ/kg}$$

$$\textcircled{3} \Delta p.e = g(z_2 - z_1) = 9.81(6 - 10) = -39.24 \text{ kJ/kg}$$

→ Energy balance :-

$$\dot{E}_{in} = \dot{E}_{out}$$
$$\dot{Q}_{in} + \dot{W}_{in} + \dot{m}_{in} = \dot{Q}_{out} + \dot{W}_{out} + \dot{m}_{out}$$

$$\dot{m} \left( h_1 + \frac{V_1^2}{2} + gz_1 \right) = \dot{W}_{out} + \dot{m} \left( h_2 + \frac{V_2^2}{2} + gz_2 \right)$$

(kJ/kg)

$$\dot{W}_{out} = \dot{m}_{out} \left( h_2 + \frac{V_2^2}{2} + gz_2 \right) - \dot{m}_{in} \left( h_1 + \frac{V_1^2}{2} + gz_1 \right)$$
$$\frac{\dot{W}_{out}}{\dot{m}} = \left( h_2 - h_1 + \frac{V_2^2}{2} - \frac{V_1^2}{2} + gz_1 - gz_2 \right)$$

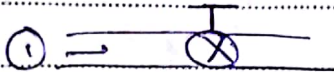
$$\dot{W}_{out} = (887.39 - 14.95 + 0.04)$$

$$\dot{W}_{out} = 872.39 \text{ kJ/kg}$$

$$\textcircled{4} \dot{m} = \frac{\dot{W}_{out}}{\dot{W}_{in}} = \frac{5 \times 10^6}{872.39} = \boxed{5.03 \text{ kg/s}}$$

### 3 Throttling Valve:-

→ Device that cause large pressure drops in the fluid,  
 $(\dot{w} \approx 0)$ ,  $(\dot{Q} \approx 0)$ ,  $(\Delta P \neq 0)$  (k.e.g), temperature drop or temp. rise is used in AC cycle, refrigeration cycle "isenthalpic" ( $h_1 \approx h_2$ )  
 another name



A adjustable  
Valve



A capillary  
tube



A Porous plug

→ mass balance :-

$$\dot{m}_{in} = \dot{m}_{out}$$

→ energy balance :-

$$\dot{E}_{in} = \dot{E}_{out}$$

$$h_1 = h_2$$

$$P_1 V_1 + U_1 = P_2 V_2 + U_2$$

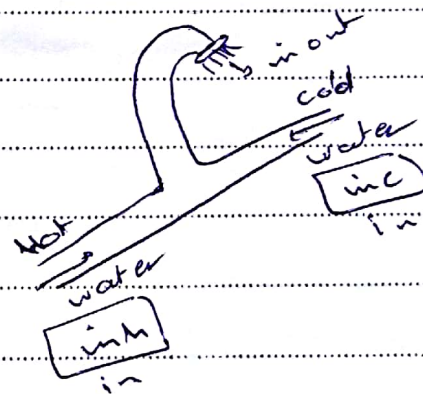
### 4 (a) Mixing chamber:-

$$\dot{q} \approx 0$$

$$\dot{W} \approx 0$$

$$\Delta K.E. \approx 0$$

$$\Delta P.E. \approx 0$$





H.W : EX 6-8 (3) 6-10  
 EX 6-9

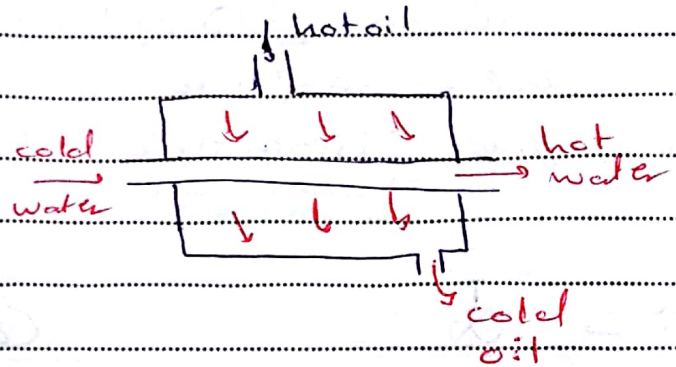
► Subject :

4) (b) Heat exchanger :-  $\rightarrow$  no mix between 2 fluids

$\rightarrow$  used to exchange heat between two fluids without mixing

\* Types of H.E :-

- ① shell and tube
- ② cross flow H.E



( $W = 0$ ), ( $k.e = 0$ ), ( $\Delta p.e = 0$ ), ( $Q = 0$ ) Ideal  
 For

## \* Ch. 7 :- The second law of thermodynamics :-

→ The first law is only concerned with the conservation of energy of systems.

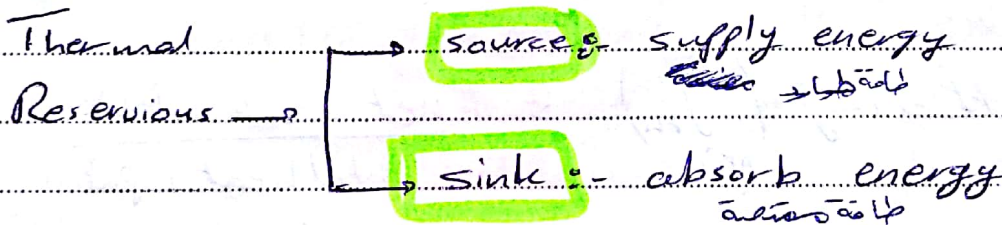
→ The second law has been introduced to deal with process direction, energy quality as well as quantity and the theoretical limitation of thermal system.

### \* 7-2 :- Thermal Energy Reservoirs :-

→ A large body with large thermal capacity (mass  $\times$  Thermal capacity)

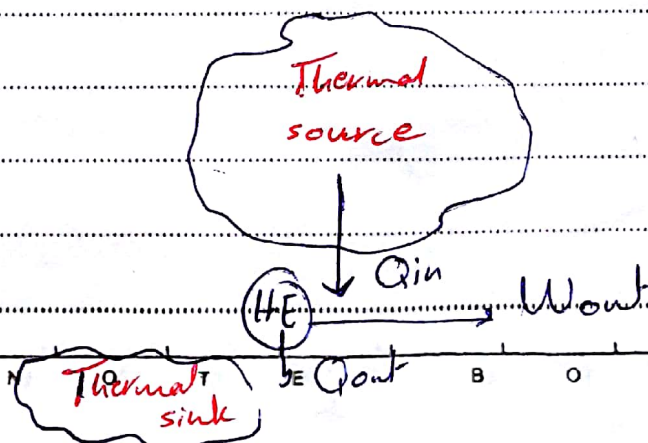
can supply or absorb energy without change Temperature.

→ Ex :- Oceans, seas, rivers, atmospheric air, Industrial furnace.  
الافواه الصناعيه



### \* 7.3 :- Heat engines (H.E) devices :-

→ H.E :- is a special devices use to convert heat to work.





1)  $Q_{in}$  - from high temp source (solar energy, nuclear reactors)

2) Work out

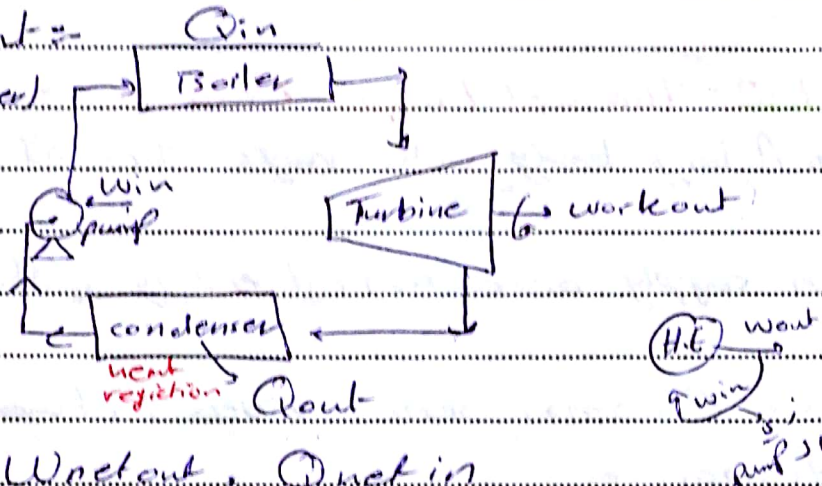
$$W_{out} = Q_{in} - Q_{out} \quad (*)$$

3)  $Q_{out}$  to surrounding (Thermal sink)

4) operate on cycle

\* steam power plant -

working fluid (water)



first law

$W_{net, out} = Q_{net, in}$

$$W_{out} - W_{in} = Q_{in} - Q_{out}$$

Thermal efficiency ( $\eta_{th}$ ) =  $\frac{\text{net work output}}{\text{total heat input}}$

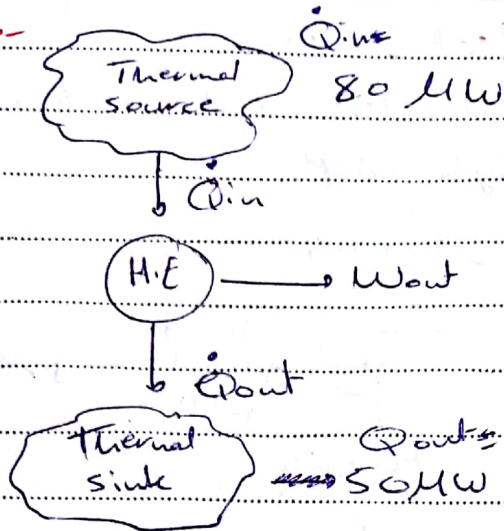
$$= \frac{W_{net, out}}{Q_{in}}$$

$$= \frac{Q_{in} - Q_{out}}{Q_{in}}$$

$$= 1 - \frac{Q_{out}}{Q_{in}}$$

$$\Rightarrow \eta_{th} < 1$$

# Ex :-



→ Determine net power output and thermal efficiency?

$$\eta = \frac{W_{out}}{Q_{in}} = \frac{Q_{in} - Q_{out}}{Q_{in}}$$

$$\rightarrow W_{net} = Q_{in} - Q_{out} = 80 - 50 = \boxed{30 \text{ MW}} = W_{out}$$

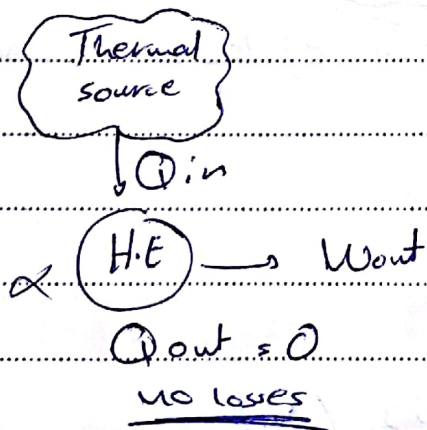
$$\rightarrow \eta_{th} = 1 - \frac{Q_{out}}{Q_{in}} = 1 - \frac{50}{80} = 0.375$$

$$= \boxed{37.5\%}$$

→ The second law of Thermodynamics (Kelvin planck statement) :-

it is impossible for any device that operates on a cycle to receive heat from a single reservoir and produce a net amount of work, it is impossible to have H.E with  $\eta = 100\%$ .

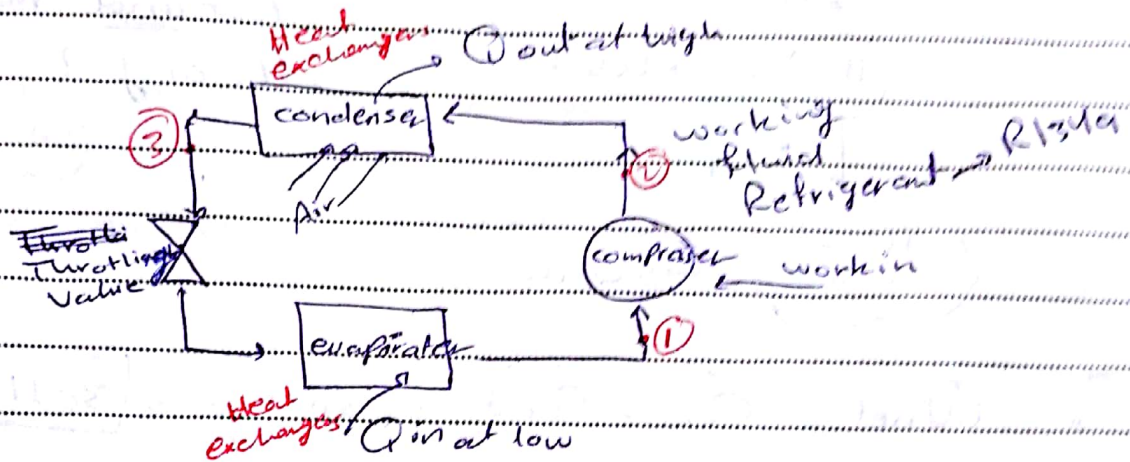
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## \* 7.4 = Refrigerators and Heat Pumps

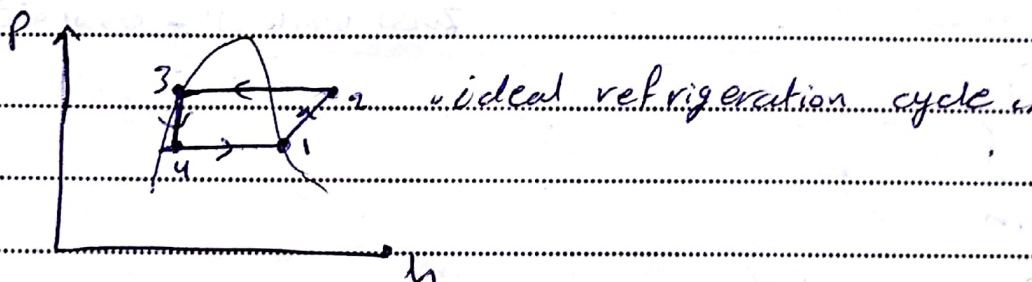
↳ special device used to transfer of heat from low temp. medium to a high temp.



$$\text{COP}_R = \frac{\text{Desired output}}{\text{Required input}} = \frac{Q_L}{W_{in}} = \frac{Q_L}{Q_H - Q_L} > 1$$

$$\text{COP}_H = \frac{Q_H}{W_{in}} = \frac{Q_H}{Q_H - Q_L} > 1$$

$$\text{COP}_H = \text{COP}_R + 1$$



\* Ex 7.3 / 7.4

suggested = 21 / 39 / 42 / 43 / 53 / 101





Subject: Thermal Physics

\* second law of Thermodynamics (Clausius statement):

→ it is impossible to construct a device that operates in a cycle and produces no effect other than the heat transfer from low temp. body to a higher temp. body.

\* 7-5: <sup>ideal</sup> Reversible and Irreversible Processes:-

→ **Reversible Process**:- process that can be reversed without leaving any trace on the surrounding

→ **Irreversible Process**:- not reversible, it will leave change on the surrounding

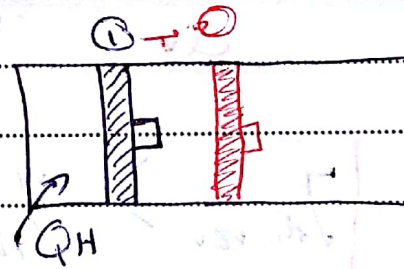
→ Ex:- Friction, Mixing with two fluids.

\* 7-6:- Carnot cycle:-

→ it is a thermodynamic cycle consist of four reversible processes.

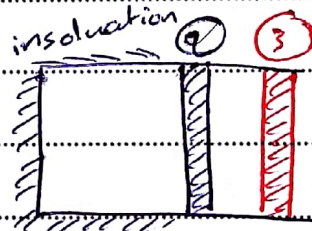
[1] Reversible isothermal expansion

① → ②

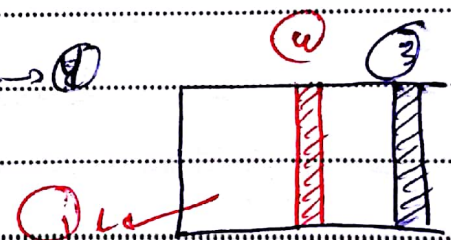


[2] Reversible adiabatic expansion

② → ③



[3] Reversible isothermal compression ③ → ④



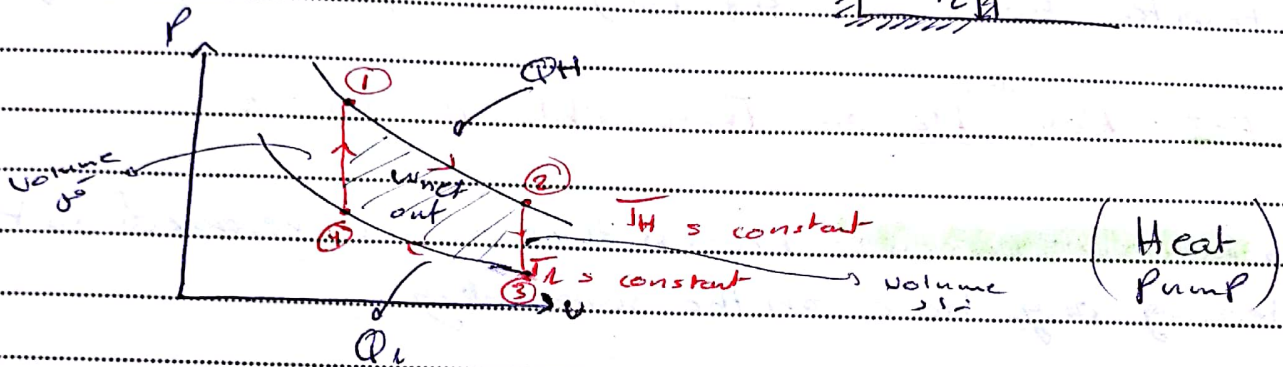
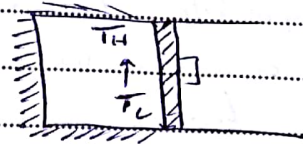


$J_{rev} > J_{irr}$

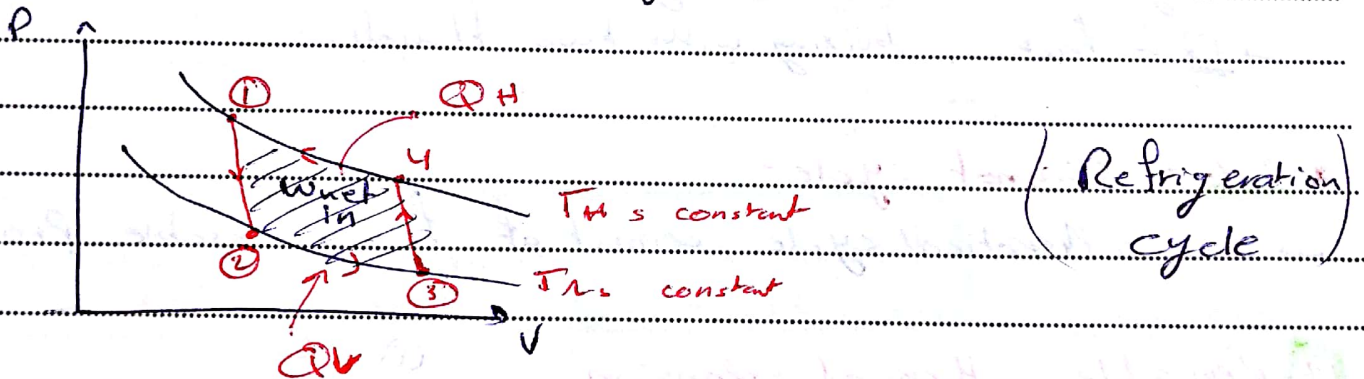


► Subject :

**u** Reversible Adiabatic compression  $(3 \rightarrow 1)$



→ The reversed carnot cycle:



$$\eta_{th, rev} > \eta_{th, irr}$$

\* 7-8 :- Thermodynamic Temp scale :- (kelvin-scale)

$$\eta_{th, rev} = f(T_H, T_L), \quad \frac{Q_H}{Q_L} = f(T_H, T_L)$$

→ for carnot cycle  $\eta_{th} = 1 - \frac{Q_L}{Q_H}$   $\eta_{th, rev} = 1 - \frac{T_L}{T_H}$

→ Refrigeration and heat pump :-

$$COP R_{rev} = \frac{Q_L}{Q_H - Q_L} = \frac{1}{\frac{Q_H}{Q_L} - 1} = \frac{1}{\frac{T_H}{T_L} - 1}$$

$$COP H_{rev} = \frac{Q_H}{Q_H - Q_L} = \frac{1}{1 - \frac{Q_L}{Q_H}} = \frac{1}{1 - \frac{T_L}{T_H}}$$



Subject: Ch. 11

## \* Ch. 11: fluid statics:

### Fluid Mechanics

Fluid statics

"fluid at rest"

fluid dynamic

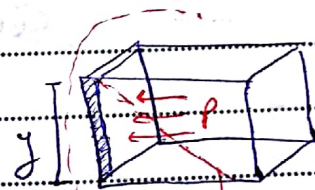
"fluid at motion"

used to determine the force acting on floating or submerged bodies and the forces developed by devices such as Hydraulic pressure and car jacks, water dams and liquid storage tanks.

→ Remark from chapter (2):

$$P_{\text{gage}} = \rho g \Delta h$$

not constant (P)  
"depends on (h)"



linear distribution

→ Force → Normal force

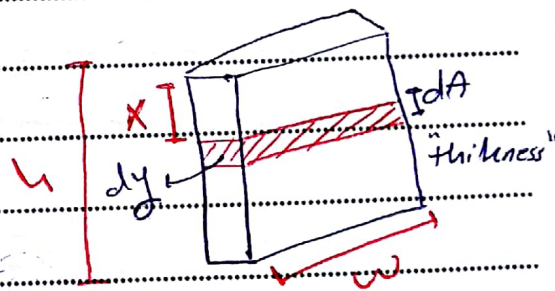
$$P = \frac{F}{A} \quad \text{"Normal force"}$$

to find the (P) related to Area by using integration:

$$F = \int_A \rho g y \, dA = \int_A P \, dA$$

$$F = \rho g \int y \, dA \rightarrow F = \rho g \int_0^h y \cdot w \, dy$$

$$F = \frac{\rho g w y^2}{2} \Big|_0^h = \frac{\rho g w h^2}{2}$$



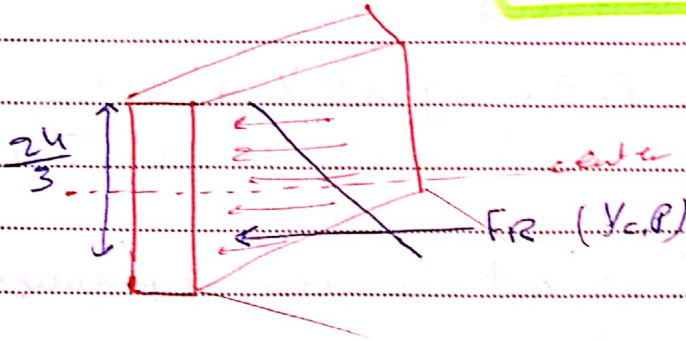


$$\rightarrow F_R = \rho g \frac{h}{2} (A)$$

$$\rightarrow \text{But } \rho g h = P$$

$$\rightarrow \boxed{\rho g \frac{h}{2} = P_{avg}}$$

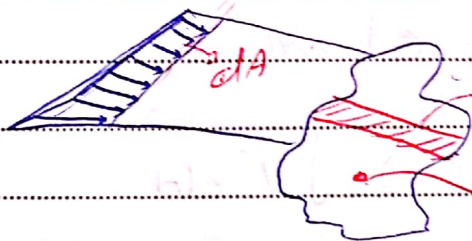
then: Resultant force  $(F_R) = P_{avg} \times A$



H.2 :- Hydraulic force on submerged plane surface:-

Vacuum Pressure  $\leftarrow P_v$

$$\boxed{h = y \sin \theta}$$



submerged object (A)

centroid of object

$P_v = \text{atmospheric}$   
 $\rightarrow 0$

Pressure at any point on plane:-

$$\boxed{P = P_v + \rho g h = P_v + \rho g y \sin \theta}$$

fluid weight

$\rightarrow$  to find resultant force (Hydraulic force  $(F_R)$ ) :-

$$F_R = \int (P_v + \rho g y \sin \theta) dA$$



$$\rightarrow FR = \int_A p \cdot dA + \int_A \rho g y \sin \theta \cdot dA$$

$$FR = p \cdot A + \rho g \sin \theta \int_A y \cdot dA$$

$$y_c = \frac{1}{A} \int_A y \cdot dA \rightarrow y_c A = \int_A y \cdot dA$$

"centroid"

first moment of Area

Then =

$$FR = p \cdot A + \rho g \sin \theta y_c A$$

90° = 0°

→ when does the force act "center of pressure"  
"static fluid"  $\rightarrow$   $\rho$  constant

By using moment =

$\sum M = 0$

$$y_{cp} \cdot FR = \int_A y \cdot p \cdot dA \rightarrow \text{from equation (1)}$$

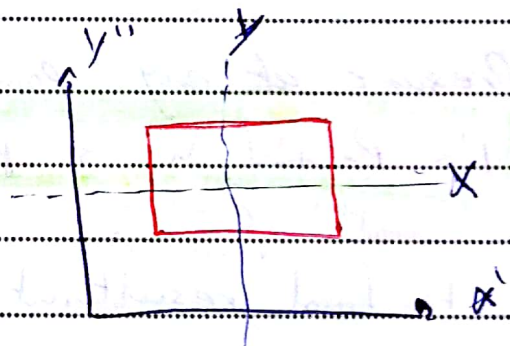
$$y_{cp} \cdot FR = \int_A y (p + \rho g y \sin \theta) \cdot dA$$

$$y_{cp} \cdot FR = p \cdot \int_A y \cdot dA + \rho g \sin \theta \int_A y^2 \cdot dA$$

Remark:

$$I_y = \frac{1}{12} ab^3$$

$$I_x = \frac{1}{12} ba^3$$



Parallel axis theorem (Any Axis)  $\rightarrow I_P = I_{\text{centroid}} + A d^2$

$$I_A = I_{\text{centroid}} + A d^2$$

$$Y_{\text{cp}} F_R = P \cdot Y_{\text{CA}} + \rho g \sin \theta (I_{xx} + A Y^2_{\text{c}})$$

"centroid"

$$\# Y_{\text{cp}} = Y_{\text{c}} + \frac{I_{xx}}{(Y_{\text{c}} + P / \rho g \sin \theta) A}$$

$$\# F_R = P \cdot A + \rho g \sin \theta \cdot Y_{\text{c}} A$$

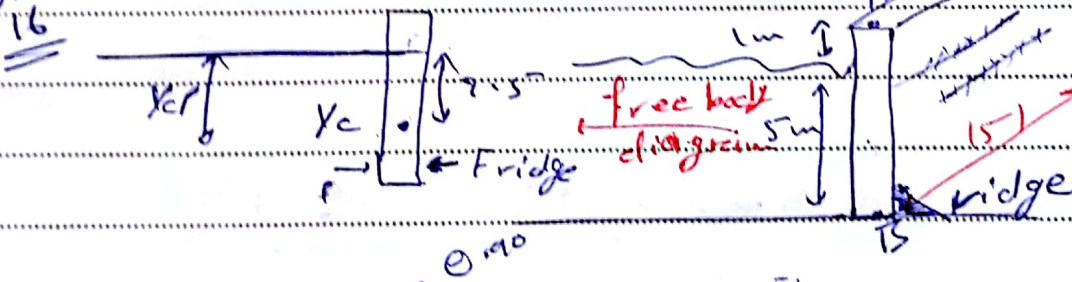
Rectangular gate in line

$$\rightarrow Y_{\text{cp}} = \frac{h}{2} + \frac{\frac{1}{12} w h^3}{\frac{1}{2} (w h)}$$

$$\rightarrow Y_{\text{cp}} = \frac{h}{2} + \frac{2}{12} h \rightarrow \boxed{Y_{\text{cp}} = \frac{2}{3} h}$$

centroid below ( $Y_{\text{cp}}$ ) not "is"

\*Ex: determine the force exerted on plane by ridge?  
suggested



$$F_R = \rho g \sin \theta Y_{\text{c}} A$$

$$= 1000 \times 9.81 \times (2.5) (5 \times 5) \rightarrow F_R = 613.125 \times 10^3 \text{ N}$$



Subject : .....

(5)

$$\rightarrow Y.P. = \frac{2}{3} L = \frac{10}{3} = 3.333 \text{ m}$$

$\Sigma M_{B=0}$

$$\rightarrow FR (3.333 \text{ m}) - F \times 6 = 0$$

$$\frac{6(3.125 \times 10^3)(4.333)}{6} = F$$

$$F = 442.47 \times 10^3 \text{ N}$$

$$\text{OR } \boxed{F = 442.47 \text{ kN}}$$

$\rightarrow$  suggested :- 15/16/25/42/45/52

Subject:

Ch. 12.

## \* Ch. 12: Bernoulli eq and Energy equations -

\* 12.1 - The Bernoulli equation is concerned with the conservation of kinetic, potential and flow energies of a fluid stream and their conversion to each other in the regions of flow where net viscous forces are negligible.

$$\frac{P}{\rho} + \frac{U^2}{2} + gz = \text{constant} \quad (\text{along stream line})$$

(kJ/kg)

flow energy      kinetic energy      potential energy

→ limitations on the use of the Bernoulli eq.:

- 1- steady state (not change with time)
- 2- Viscous (friction) effects are negligible.
- 3- Incompressible flow → ( $\rho = \text{constant}$ )
- \* 4- flow is irrotational and there is no vorticity.

alt. eq. ⑥ →

$$\frac{P}{\rho g} + \frac{U^2}{2g} + Z = \text{constant} \quad (\text{m})$$

pressure head      velocity head      elevation head

③ →

$$P + \frac{\rho U^2}{2} + \rho g Z = \text{constant} \quad (\text{Pa})$$

static pressure      dynamic pressure      hydrostatic pressure.

Sum of static and dynamic pressures → stagnation pressure

$$P_{\text{stag}} = P + \frac{\rho U^2}{2}$$

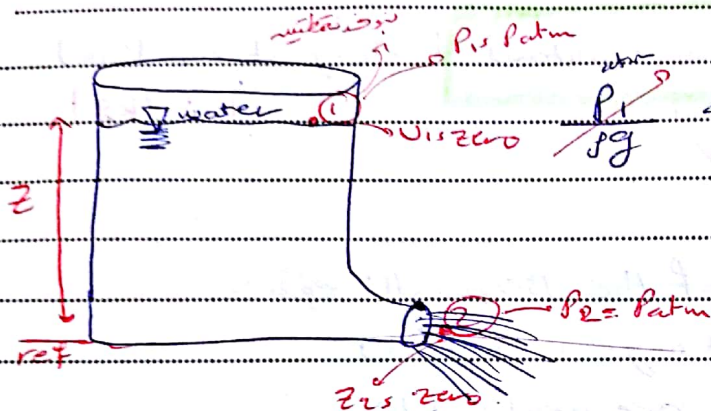


Subject: \_\_\_\_\_

\* stagnation pressure - represent the pressure at a point where the fluid is brought to a complete stop  $\rightarrow [V=0]$

## \* Applications of the Bernoulli eqn:-

### 1- Water discharge from a large tank:-



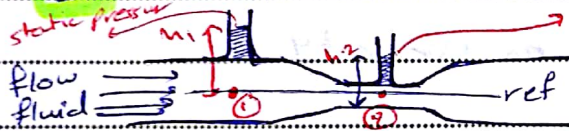
$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + Z_2$$

where  $Z_1 = \frac{V_2^2}{2g}$

$$V_2 = \sqrt{2Z_1g}$$

Torricelli equation

### 2- Venturi meter - piezo meter (measure static pressure)



from mass balance

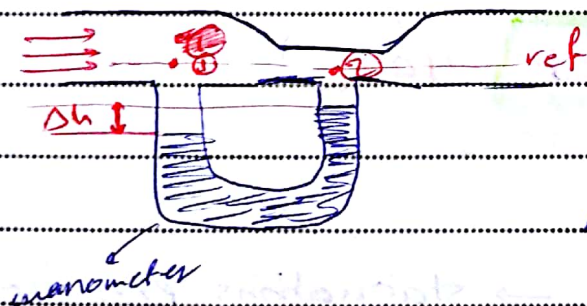
$$m_{in} = m_{out}$$

$$\rho A_1 V_1 = \rho A_2 V_2$$

Incompressible fluid flow

$$\text{then } A_1 V_1 = A_2 V_2$$

Area  $\propto$  velocity



$$P_1 = \rho g h_1$$

$$P_2 = \rho g h_2$$

$$\rightarrow \frac{P_1}{\rho g} + \frac{U_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{U_2^2}{2g} + z_2 \quad \text{they are in the same ref}$$

→ from mass balance:-

$$in_1 = in_2$$

$$\rho U_1 A_1 = \rho U_2 A_2$$

$$U_1 A_1 = U_2 A_2$$

$$\boxed{U_1 = U_2 \frac{A_2}{A_1}}$$

$$\rightarrow \frac{P_1}{\rho g} + \frac{U_2^2 \left(\frac{A_2}{A_1}\right)^2}{2g} = \frac{P_2}{\rho g} + \frac{U_2^2}{2g}$$

$$\frac{P_1}{\rho} - \frac{P_2}{\rho} = \frac{U_2^2}{2} - \frac{U_2^2}{2} \left(\frac{A_2}{A_1}\right)^2$$

$$\frac{2(P_1 - P_2)}{\rho} = U_2^2 \left(1 - \frac{A_2^2}{A_1^2}\right)$$

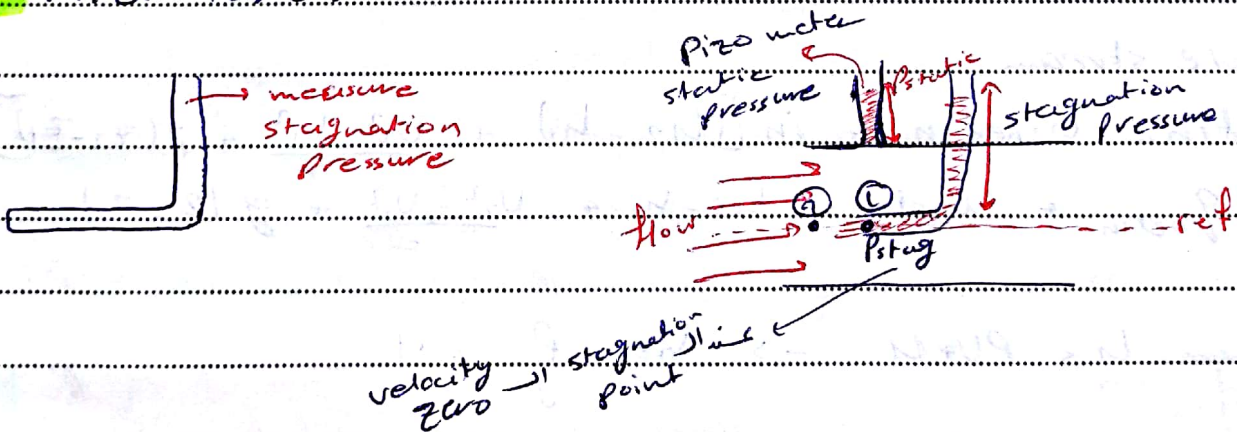
$$\rightarrow \boxed{U_2 = \sqrt{\frac{2(P_1 - P_2)}{\rho \left(1 - \frac{A_2^2}{A_1^2}\right)}}$$

→ flow rate

$$in_1 = \rho U_1 A_1$$

$$in_2 = \rho U_2 A_2$$

### 3- Pitot tube:-



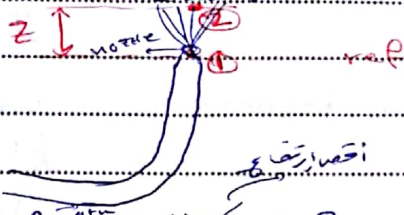
$$\frac{P_1}{\rho g} + \frac{U_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{U_2^2}{2g} + z_2$$

$$U_2 = \sqrt{\frac{2(P_1 - P_2)}{\rho}} = \sqrt{\frac{2(P_{stag} - P_{static})}{\rho}}$$

S T A R S N O T E B O O K



4- spraying water into the air :-



$$\frac{P_1}{\rho g} + \frac{U_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{U_2^2}{2g} + z_2$$

→ if  $U_1 \neq 0$

$$z_2 = \frac{P_1 - P_2}{\rho g} + \frac{U_1^2}{2g}$$

→ if  $U_1 = 0$

$$z_2 = \frac{P_1 - P_2}{\rho g}$$

note :- to know the value of  $U_1$  → from mass flow rate or volume flow rate if we have the cross sectional Area  $[A_1]$

## \* 12-20r Energy analysis of steady flow

$$\dot{Q}_{net in} + \dot{W}_{net in} = \sum_{out} \dot{m} (h + \frac{U^2}{2} + gz) - \sum_{in} \dot{m} (h + \frac{U^2}{2} + gz)$$

→ for single stream

$$\dot{Q}_{net in} + \dot{W}_{net in} = \dot{m} [(h_2 - h_1) + \frac{U_2^2 - U_1^2}{2} + g(z_2 - z_1)]$$

divided by  $\dot{m}$

$$q_{net in} + w_{net in} = h_2 - h_1 + \frac{U_2^2 - U_1^2}{2} + g(z_2 - z_1)$$

enthalpy eq

$$h = u + Pv \rightarrow h = \frac{P}{\rho} + u$$

enthalpy eq

$$w_{net in} + \frac{P_1}{\rho_1} + \frac{U_1^2}{2} + g z_1 = \frac{P_2}{\rho_2} + \frac{U_2^2}{2} + g z_2 + (u_2 - u_1) \quad \text{--- note}$$

Mechanical energy input

Mechanical energy output

Mechanical energy loss

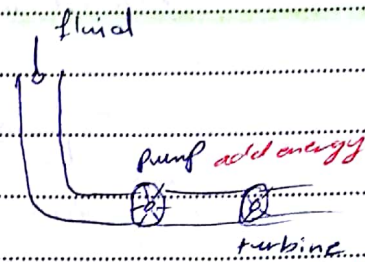


Subject :

$$\rightarrow E_{\text{mech, loss}} = U_2 - U_1 - \dot{Q}_{\text{net in}}$$

$$\rightarrow W_{\text{net in}} = \dot{W}_{\text{in}} - \dot{W}_{\text{out}}$$

shaft pump      shaft turbine



$$\textcircled{1} \# \frac{P_1}{\rho_1} + \frac{U_1^2}{2} + gZ_1 + \dot{W}_{\text{pump}} = \frac{P_2}{\rho_2} + \frac{U_2^2}{2} + gZ_2 + \dot{W}_{\text{turbine}} + E_{\text{mech, loss}}$$

extract energy turbine

$$\textcircled{2} \# \text{in} \left( \frac{P_1}{\rho_1} + \frac{U_1^2}{2} + gZ_1 \right) + \dot{W}_{\text{pump}} = \text{in} \left( \frac{P_2}{\rho_2} + \frac{U_2^2}{2} + gZ_2 \right) + \dot{W}_{\text{turbine}} + E_{\text{mech, loss}} \quad (\text{KW})$$

$$\textcircled{3} \# \frac{P_1}{\rho_1 g} + \frac{U_1^2}{2g} + Z_1 + \overset{\substack{\text{useful} \\ \text{head}}}{h_{\text{pump}}} = \frac{P_2}{\rho_2 g} + \frac{U_2^2}{2g} + Z_2 + h_{\text{turb}} + h_L$$

(head pump)  $\dot{W}_{\text{pump}} / \dot{Q}$   
fluid side of pump  $\dot{W}_{\text{pump}} / \dot{Q}$

$$h_{\text{pump}} = \frac{\dot{W}_{\text{pump}}}{\dot{m}g}$$

$\rightarrow$  useful head pump delivered

$$h_{\text{turb}} = \frac{\dot{W}_{\text{turb}}}{\dot{m}g}$$

$\rightarrow$  extracted head turbine removed

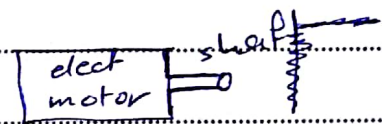
$$h_L = \frac{E_{\text{mech, loss}}}{\dot{m}g}$$

head loss

$\rightarrow$  irreversible head loss between two points due to all components of piping system.

$\rightarrow$  Mechanical efficiency:

$$\eta_{\text{pump}} = \frac{\dot{W}_{\text{pump}}}{\dot{W}_{\text{shaft, in}}} \rightarrow \text{in pump}$$



$$\eta_{\text{turb}} = \frac{\dot{W}_{\text{shaft out}}}{\dot{W}_{\text{turbine}}} \rightarrow \text{power of shaft} \rightarrow \text{extracted power (in } h_{\text{turb}})$$

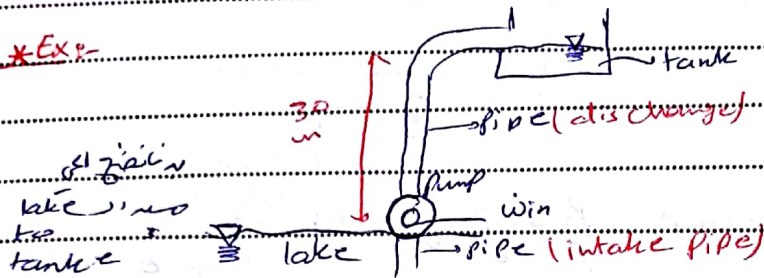


► Subject :

$$\eta_{\text{motor}} = \frac{W_{\text{shaft, out}}}{W_{\text{elect, in}}}$$

$$\eta_{\text{gen}} = \frac{W_{\text{elect, out}}}{W_{\text{shaft, in}}}$$

\* Ex \*



$$\eta_{\text{pump}} = 78\%$$

$$W_{\text{shaft}} = 5 \text{ kW}$$

$$D_{\text{pipe, intake}} = 7 \text{ cm}$$

$$D_{\text{pipe, discharge}} = 5 \text{ cm} \quad \text{assume that } h_{\text{mechanical loss}} = 0$$

Determine :- (a) The maximum flow rate (in l/s)

(b) The pressure difference across the pump?  $\Delta P$ .

sol: (a)  $\eta_{\text{pump}} = \frac{W_{\text{pump}}}{W_{\text{shaft, in}}}$

$$0.78 \times 5 \text{ kW} = W_{\text{pump}}$$

$$W_{\text{pump}} = 3.9 \text{ kW}$$

$$\dot{m} g h_{\text{pump}} = 3.9 \text{ kW}$$

$$\dot{m} \times 9.81 \times 30 = 3.9 \text{ kW} \rightarrow \dot{m} = 13.25 \text{ kg/s}$$

$$\dot{V} = \frac{\dot{m}}{\rho_{\text{water}}} = 13.25 \times 10^{-3} \text{ m}^3/\text{s}$$

► Subject :

$$\textcircled{Q} \ln \left( \frac{P_1}{P_2} + \frac{U_1^2}{2} + g z_1 \right) + \dot{W}_{\text{pump}} = \ln \left( \frac{P_2}{P_1} + \frac{U_2^2}{2} + g z_2 \right) + \dot{W}_{\text{pump}}$$

$$\rightarrow U_1 = \frac{\dot{V}}{A_1} = \frac{\dot{V}}{\frac{\pi}{4} (7 \times 10^{-2})^2}$$

$$U_1 = 3.44 \text{ m/s}$$

$$U_2 = \frac{\dot{V}}{A_2} = \frac{\dot{V}}{\frac{\pi}{4} (5 \times 10^{-2})^2}$$

$$U_2 = 6.74 \text{ m/s}$$

→ to find  $\Delta P$ ?

معادله برابری

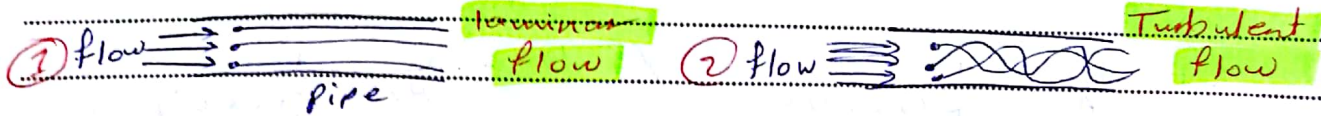
$$P_2 - P_1 = f \left[ \frac{U_1^2 - U_2^2}{2} \right] + \frac{\dot{W}_{\text{pump}}}{\dot{V}}$$

$$\Delta P = 1000 \left[ \frac{3.44^2 - 6.74^2}{2} \right] + \frac{3900}{13.25 \times 10^{-3}} = 277.5 \times 10^3 \text{ Pa}$$
$$= 277.5 \text{ kPa}$$



Subject : Ch. 14

## \* Ch. 14 : Internal flow :- Types of flow :-



→ laminar flow :- smooth stream lines and highly order motion.

→ Turbulent flow :- non smooth, it is characterized by velocity fluctuations and highly disordered motion.

→ Transition flow :- region in between laminar and turbulent.

## \* Reynolds Number (Re)

→  $Re = \frac{\text{inertia force}}{\text{viscous force}}$

$$Re = \frac{U_{avg} \times D}{\nu}$$

$D$  → geometric diameter  
 $\nu$  → kinematic viscosity ( $m^2/s$ )

$$Re = \frac{\rho U_{avg} D}{\mu}$$

$\mu$  → dynamic viscosity ( $kg/m.s$ )

$$\nu = \frac{\mu}{\rho}$$


→  $D$  :- hydraulic diameter (depend on geometry)

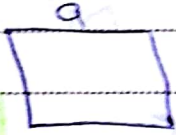
→ flow  $Re < 2300$  laminar flow

$2300 < Re < 4000$  transition flow

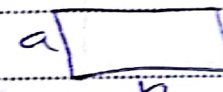
$Re > 4000$  Turbulent flow

① circular pipe  $\Rightarrow D = \frac{4A_c}{P}$  cross sectional area  
Perimeter (b.s.)

$\Rightarrow D_{ppe} = \frac{4 \times \frac{\pi}{4} D^2}{\pi D} = D$  

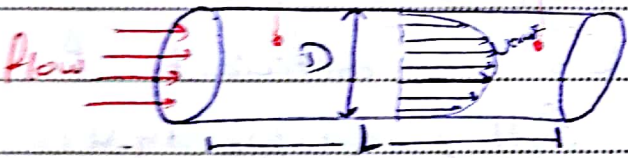
② square duct  $\Rightarrow D_{duct} = \frac{4 \times a^2}{4a} = a$  

③ rectangular duct  $\Rightarrow D_{duct} = \frac{4 \times a \times b}{2a + 2b} = \frac{4 \times a \times b}{2(a+b)}$

$D_{duct, rec} = \frac{2ab}{a+b}$  

\* Sec 14.4 :- Laminar flow in pipes:-

①  $P_1$       ②  $P_2$        $P_1 > P_2$



$\Delta P_{1-2}$  (pressure drop in pipe)

$\Delta P_{1-2} = P_1 - P_2$

$\Delta P = f \frac{L}{D} \rho \frac{U_{avg}^2}{2}$  for laminar flow

friction factor  $\Rightarrow f = \frac{64}{Re}$



Subject: \_\_\_\_\_

→ Head loss ( $h_L$ )

$$h_L = \frac{\Delta P}{\rho g} = \frac{f L}{D g} \frac{V_{avg}^2}{2}$$

↳ Major pressure drop

\* sec 14-5: Turbulent flow in pipes:

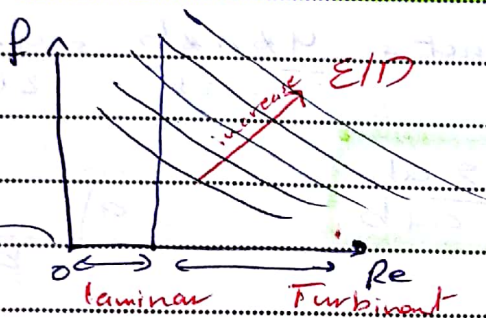
$$\Delta P_{L-2} = f \frac{L}{D} \rho \frac{V_{avg}^2}{2}$$

roughness of surface

in back  
table  
14-2

$$\frac{1}{\sqrt{f}} = -2.0 \log \left( \frac{\epsilon/D}{3.7} + \frac{2.51}{Re \sqrt{f}} \right)$$

implicit eq.  
(colebrook eq.)



Moody chart

sec 14-6: Minor losses (In fittings):

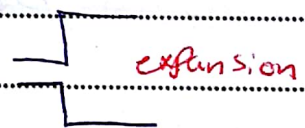
$$h_m = K \frac{V^2}{2g}$$

where  $K$  = loss coefficient of fitting (Table 14-4)

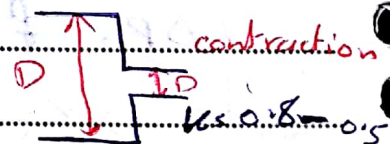
total pressure drop:

$$h_{total} = h_{major} + h_{minor}$$

(due to friction in pipe) (due to fittings)



expansion



contraction

$K = 0.8 - 0.5$



► Subject :

Ch. 16

## \* Ch. 16 :- Mechanisms of Heat Transfer

\* Heat transfer :- Transfer thermal energy from higher temp region to lower temp region.

→ Three mechanisms (modes) of heat transfer

1) conduction →

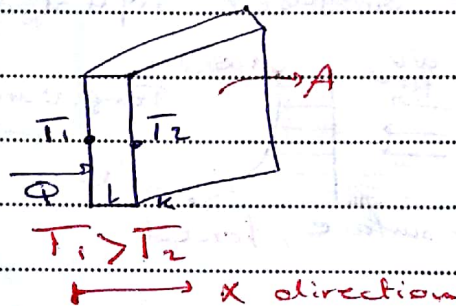
2) convection →

3) radiation →

1) **conduction** :- Transfer of energy from more energetic particles to less energetic ones.

→ 1 Direction heat flow :-

Heat transfer rate  $\propto \frac{\text{Area (Temp. diff)}}{\text{Thickness}}$



$$\dot{Q}_{\text{cond}} = -k A \frac{dT}{dx} \quad (\text{Fourier's law of conduction})$$

if  $\dot{Q}$  in steady state flow

Direction of flow  $\leftarrow$  Temp. gradient  $\downarrow$

→ k unit →  $\text{W/m}\cdot^\circ\text{C}$  or  $\text{ks W/m}\cdot\text{k}$

From Table 16-1 → Diamond →  $k \approx 2300$   $\text{W/m}\cdot^\circ\text{C}$



Subject :

→ conduction take place in solids, liquids and gases.  
solids > liquids > gases.

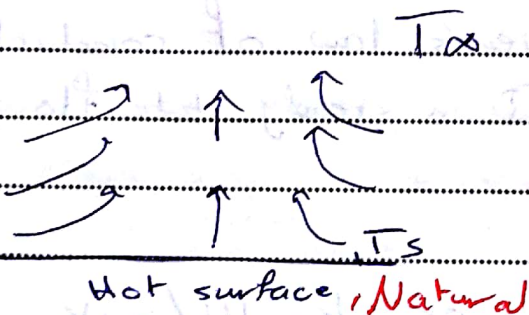
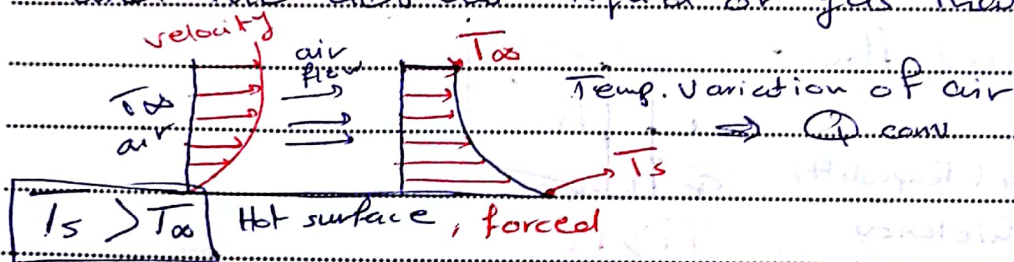
\* Example 16-1 / 16-2 from Book

\* Thermal diffusivity  $\alpha$  :- represents how fast heat diffuses.

$$\alpha = \frac{\text{Heat conduction}}{\text{Heat storage}} = \frac{k}{\rho C_p} \quad (\text{m}^2/\text{s})$$

From Table 16-4 in Book.

2 - **Convection** :- energy transfer between a solid surface and the adjacent liquid or gas that is in motion.



→ **Convection** → Natural is due to density variations.  
→ forced is due to external force (fan)

► Subject :

→ Newton's law of cooling →  $\dot{Q}_{\text{conv}} \propto A_s (\text{Temp diff})$

$$\dot{Q}_{\text{conv}} = h A_s (T_s - T_{\infty}) \quad \text{at S.S.}$$

where  $h$  = heat transfer coefficient ( $\text{W/m}^2 \cdot ^\circ\text{C}$ )

Table 16-5 from Book

3- **Radiation** = energy emitted by ~~solid~~ matter in the form of electromagnetic waves.

→ Stefan - Boltzmann law:

$$\dot{Q}_{\text{rad, emit}} = \underbrace{\sigma}_{\text{constant}} A_s T_s^4 \quad \text{kelvin}$$

Stefan - Boltzmann constant  $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot ^\circ\text{C}^4$

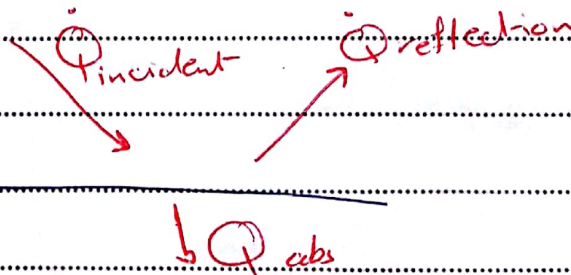
$$\dot{Q}_{\text{rad}} = \epsilon A_s T_s^4$$

$\epsilon$  emissivity  $0 \leq \epsilon \leq 1$

black body

Table 16-6


\* absorptivity ( $\alpha$ ) = The fraction of the radiation energy incident on the surface that is absorbed by the surface.



الاشعاع الساقط  
الاشعاع المنعكس



► Subject : .....

  $\alpha = \frac{\dot{Q}_{\text{absorbed}}}{\dot{Q}_{\text{incident}}}$

$\dot{Q}_{\text{ref}} = (1 - \alpha) \dot{Q}_{\text{incident}}$

→ between two surfaces

$\dot{Q}_{\text{rad}} = \epsilon \sigma A_s (T_s^4 - T_{\text{sur}}^4)$

→ \* Example

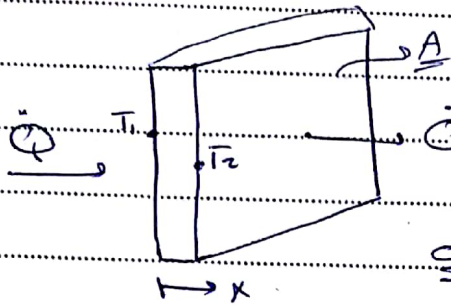
16-5

16-6

16-7

from T sink

\* Ch. 17, - steady Heat conduction



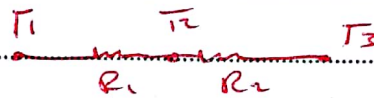
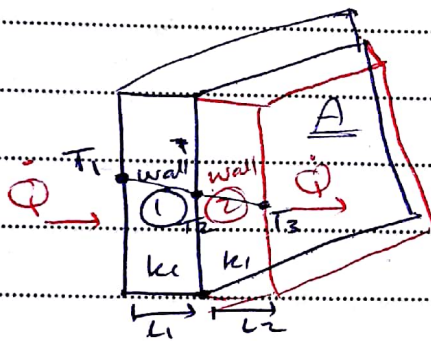
$$\dot{Q}_{cond} = -kA \frac{dT}{dx}$$

$$\text{or } \dot{Q}_{cond} = \frac{\Delta T}{R_{thermal}} = \frac{\Delta T}{\frac{\Delta x}{kA}}$$

Thermal resistance (C/W)

$$\dot{Q}_{conv} = h A_s \Delta T$$

$$\dot{Q}_{conv} = \frac{\Delta T}{R_{conv}} \rightarrow \left( \frac{1}{h_{conv} A_s} \right)$$



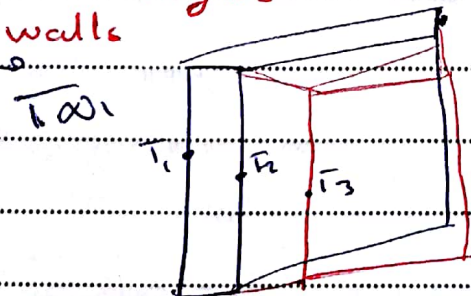
$$\dot{Q}_{1-3} = \dot{Q}_{1-2} = \dot{Q}_{2-3}$$

$$\frac{T_3 - T_1}{R_{total}} = \frac{T_1 - T_2}{R_1} = \frac{T_2 - T_3}{R_2}$$

$$\downarrow \quad \downarrow$$

$$\frac{L_1}{k_1 A} \quad \frac{L_2}{k_2 A}$$

for multilayers



$$\frac{1}{R_{total}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\dot{Q}_{conv, T_{\infty 1}-T_1} = \dot{Q}_{cond, 1-2} = \dot{Q}_{cond, 2-3} = \dot{Q}_{conv, T_3-T_{\infty 2}}$$

$$h_{\infty 1} A (T_{\infty 1} - T_1) = \frac{\Delta T_{1-2}}{R_1} = \frac{\Delta T_{2-3}}{R_2} = h_{\infty 2} A (T_3 - T_{\infty 2})$$

\* Examples 17-1 / 17-2 / 17-3