

تقدم لجنة EiCoM الأكاديمية

تلخيص فيرست وسكند لمادة:

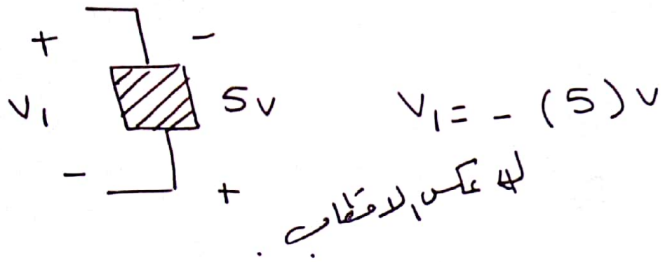
دوائر كهربائية (١)

جزيل الشكر للطالب:

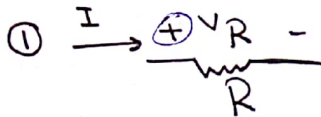
موسى النجار

* انجس سرت ١

* polarity:

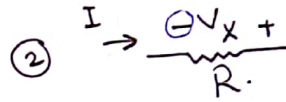


* ohm's law:



$$V_R = IR$$

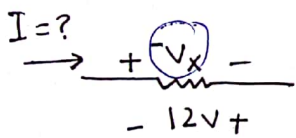
(التيار داخل في الموجبة)



$$V_X = -IR$$

(التيار داخل في السالبة)

* Example:



$$R = 1k$$

$$I = \frac{V}{R} \rightarrow I = \frac{+}{R} \quad \text{التيار عكس القطب}$$

$$= \frac{-12}{1} = -12A \quad \checkmark$$

ملاحظة: $-V_X = -12$

عكس القطبية

$$V_X = 12$$

OR

$$I = \frac{V}{R} = \frac{-12}{1} = -12A \quad \checkmark$$

داخل في السالبة
12

* Power:

$$P_{abs} = \pm IV \text{ (For any element).}$$

For R: على فرض التيار داخل عنده الموجب

$$IV = \frac{V}{R} * V = \frac{V^2}{R}$$

$$IV = I(IR) = I^2 R. \text{) } \underline{\underline{\text{only}}} \text{ For } \underline{\underline{R}}$$

$$P_{gen} = -P_{abs}$$

لغنى العنصر.

* Power in real LiFe:

1. absorbed

disipated.

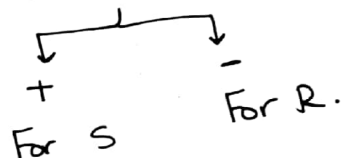
delivered by.



2. Supplied.

generated.

delivered into.



* Resistors:

1. $R = 0$



Short cct (S.C).

$$V = 0$$

$$I = ?$$

2. $R = \infty$

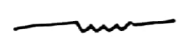


open cct (O.C)

$$I = 0$$

$$V = ?$$

3. $0 < R < \infty$



$$V, I$$

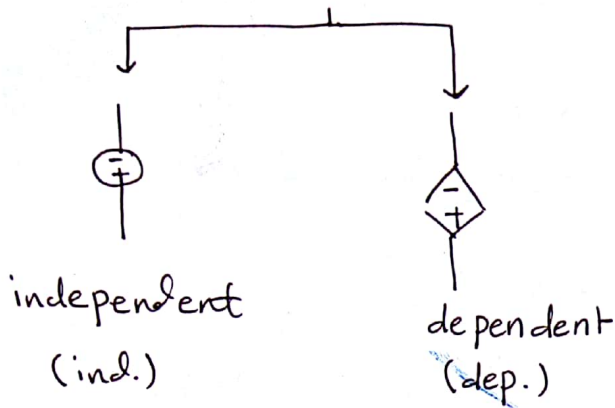
ohm's law.

* $G = \frac{1}{R} \Omega^{-1}$, Simens (conductance).

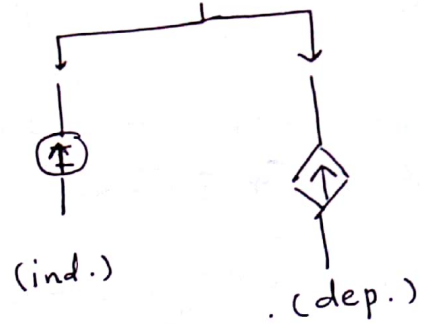
← مقلوب المقاومة

12.3 voltage and current sources:

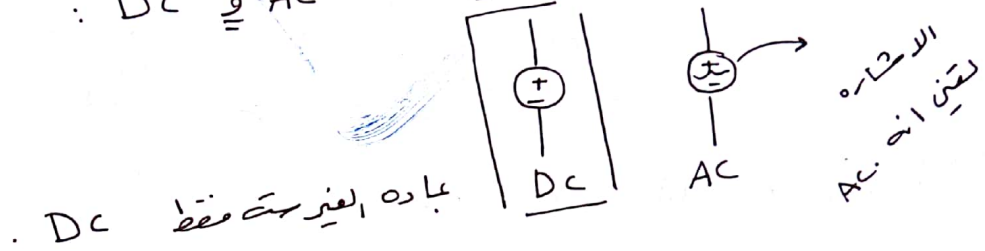
1. voltage source (DC)



2. current source (DC)



* كل واحد من النوعين في صورة DC و AC



* The default power For: (إذا السؤال طلب الـ power بدون ما يحدد نوعه يستخدم الـ Default)

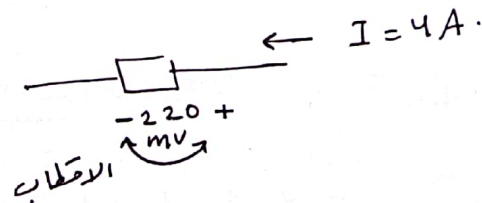
$R \rightarrow$ dissipated.

$S \rightarrow$ generated.

* P_{abs} : إذا كان التيار داخل في موجب سوار (+) كانت مقاومته أو سورس

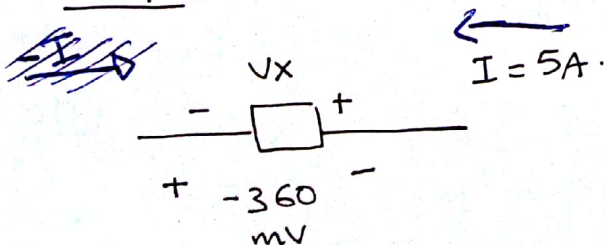
* إذا كان التيار داخل في السالب سوار (-) كانت مقاومته أو سورس

* Practice 2.6:



$$P_{abs} = +220 \times 4 = 880 mV.$$

* Example:



$V_x = ?$
 $P_{abs} = ?$
 $P_{gen} = ?$

الحل في الخلف

$$* V_X = -(-360) = 360 \text{ mV}$$

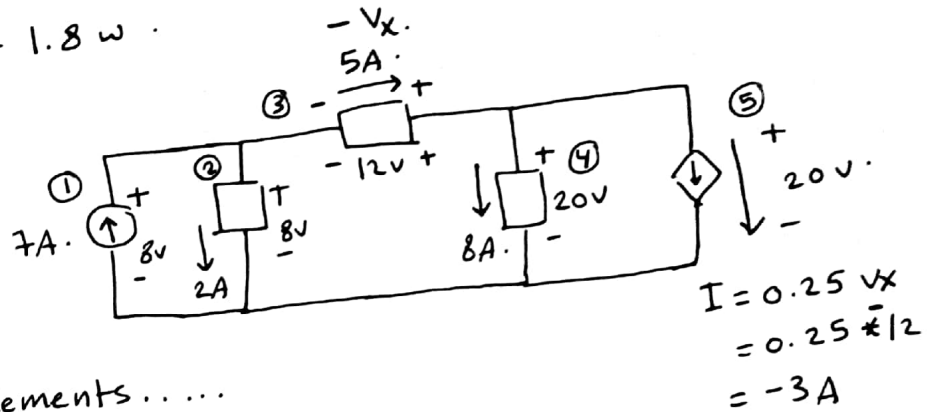
لـ
القطب

$$* P_{abs} = + I V_X = 5 * 360 = 1800 \text{ mW} = 1.8 \text{ W}$$

$$\text{OR} = - I (-360) = 5 * 360 = 1800 \text{ mW} = 1.8 \text{ W}$$

$$* P_{gen} = - P_{abs} = -1.8 \text{ W}$$

* Practice 2.9:



Find V_X , P_{abs} for all elements.....

* Solution:

* رقم العناصر بدايةً عننا ما نخرجه:

$$\text{For ①: } P_{abs} = - I V = - 7 * 8 = \underline{-56 \text{ W}}$$

$$\text{For ②: } P_{abs} = + 8 * 2 = \underline{16 \text{ W}}$$

$$\text{For ③: } P_{abs} = - 12 * 5 = \underline{-60 \text{ W}}$$

$$\text{OR} = - I (-V_X) = I V_X = 5 * -12 = \underline{-60 \text{ W}}$$

$$- V_X = 12 \quad * \text{ تذكر:}$$

$$V_X = -12$$

$$\text{For ④: } P_{abs} = + 20 * 8 = \underline{160 \text{ W}}$$

$$\begin{aligned} \text{For ⑤: } P_{abs} &= + 20 (0.25 * V_X) \\ &= + 20 (0.25 * -12) \\ &= \underline{-60 \text{ Watt}} \end{aligned}$$

3: voltage and current laws:

3.1 Nodes, Paths, loops and branches:

- node: نقطة مشتركة بين حدين أو أكثر.
- Path: أي مسار (طريق) يربط بين نقطتين في الدارة الكهربائية.
- loop: مسار path ولكن نقطة البداية لا بد أن تكون نفس نقطة النهاية.
- branch: أي path يتكون من عنصر واحد مع الاطراف تبعاً.

3.2 Kirchoff's current law:

$$\sum I = 0 \text{ node.}$$

* المجموع الجبري للتيارات الداخلة على أي node = صفر (على فرض أن جميع التيارات داخلة أو خارجة).

* مجموع التيارات الداخلة = الخارجة.

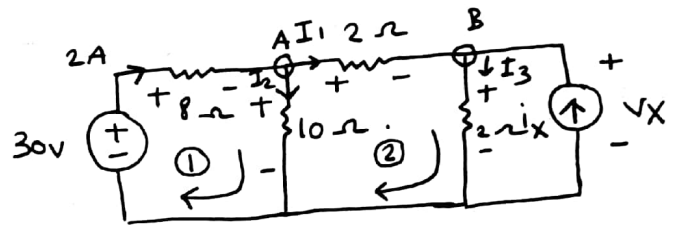
$$\sum I_{in} = \sum I_{out}$$

3.3 Kirchoff's voltage law:

* المجموع الجبري للجهود ضمن أي مسار مغلق (loop) = صفر.

* Practice 3.4:

Find V_X ? I_X ??



* Solution:

KVL at loop 1:

$$-30 + 2(8) + I_2(10) = 0 \rightarrow I_2 = \frac{30 - 16}{10} = 1.4A$$

KCL at node A:

$$I_{in} = I_{out} \rightarrow 2 = I_1 + I_2 \rightarrow I_1 = 2 - I_2 = 2 - 1.4 = 0.6A$$

KVL at loop 2:

$$-10(I_2) + 2(I_1) + I_3(2) = 0$$

$$-14 + 1.2 + V_X = 0 \rightarrow V_X = 12.8V$$

$$V_X = 2I_3 \Rightarrow I_3 = 6.4A$$

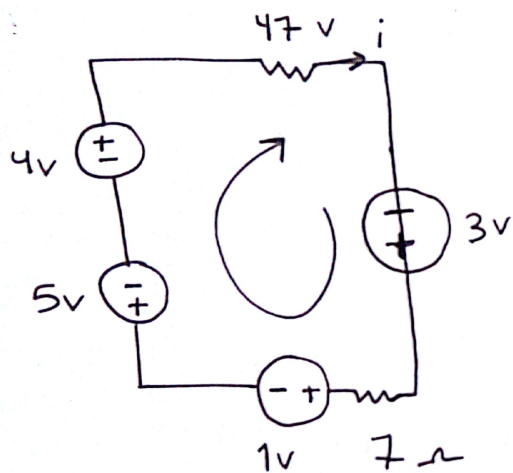
KCL at node B

$$I_1 + I_X = I_3$$

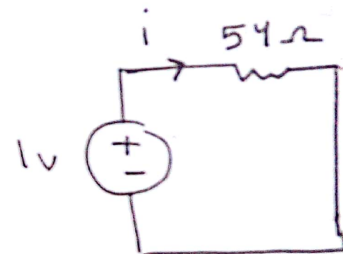
$$0.6 + I_X = 6.4$$

$$I_X = 5.8A$$

series voltage sources:



Find i ?



- سبب ای صحت، نه -

KVL :

$$-3 + 7i + 1 + 5 - 4 + 47i = 0$$

$$54i - 1 = 0$$

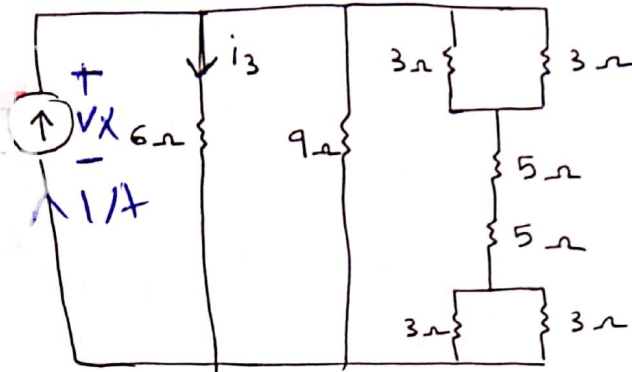
$$i = \frac{1}{54} \text{ A} \rightarrow i = \frac{V}{R} \rightarrow \frac{1V}{54\Omega}$$

Series: $R_{eq} = R_1 + R_2 + \dots + R_N$

Parallel: $R_{eq}^{-1} = R_1^{-1} + R_2^{-1} + \dots + R_N^{-1}$

$$R_{eq} = [R_1^{-1} + R_2^{-1} + \dots + R_N^{-1}]^{-1}$$

* Practice 3.14:



Find V_x ?

Sol:

$$R_{eq} = \left[(3 \parallel 3)^{1.5} + 10 + (3 \parallel 3)^{1.5} \right]$$

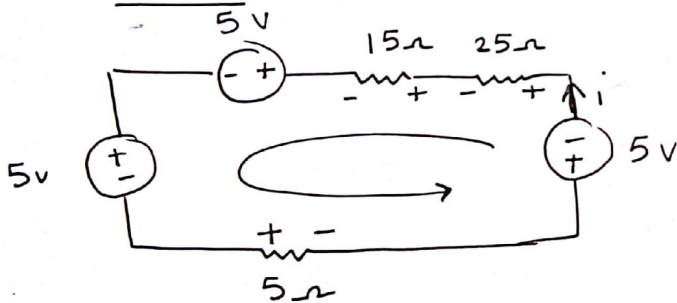
$$\parallel 9 \parallel 6$$

$$R_{eq} = 13 \parallel 9 \parallel 6$$

$$= \left(\frac{13^{-1} + 9^{-1} + 6^{-1}}{1} \right) = 2.8192 \Omega$$

$$V_x = I R_{eq} = 1 \times 2.8192 = 2.8192 \text{ V}$$

* Practice 3.12:



Find i ?

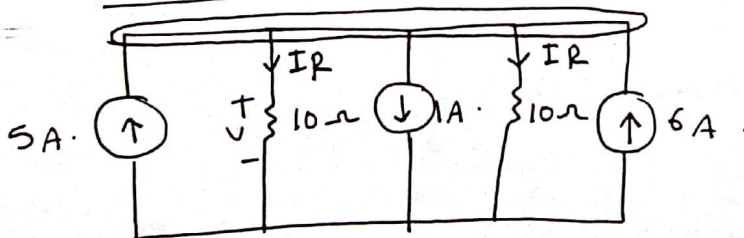
KVL:

$$5 + i(45) + 5 + 5 = 0$$

$$45i = -15$$

$$i = -\frac{1}{3} \text{ A} \checkmark$$

* Practice 3.13:



Find V ?

$$V = I_R \times 10$$

?

KCL:

$$5 + 6 = 2 I_R + 1$$

$$I_R = 5 \text{ V} \rightarrow V = 50 \text{ V}$$

الملاحظة: لو كانت المقاومات متسلسلة مثلاً $10 \geq 5$:

20

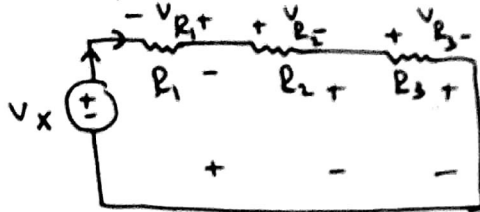
$$5 + 6 = I_{R_{10}} + I_{R_5} + 1$$

$$10 = \frac{V}{10} + \frac{V}{5}$$

لنضع التيار بدلالة الجهد والمقاومات (أولم)

$$10 = \frac{3V}{10} \rightarrow 3V = 100 \rightarrow \boxed{V = 33.33V}$$

* Voltage division:



شرط كلهم متوالي Series.

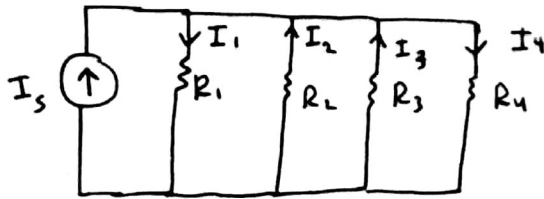
$$V_{R_1} = - V_x \left(\frac{R_1}{R_1 + R_2 + R_3} \right)$$

لأنه في السلسلة

$$V_{R_2} = + V_x \left(\frac{R_2}{R_{eq}} \right)$$

$$V_{R_3} = + V_x \left(\frac{R_3}{R_{eq}} \right)$$

* Current divider rule:



$$I_1 = + I_s \left(\frac{R_2 \parallel R_3 \parallel R_4}{R_1 + (R_2 \parallel R_3 \parallel R_4)} \right)$$

مع Is

$$I_2 = - I_s \left(\frac{R_1 \parallel R_3 \parallel R_4}{R_2 + (R_1 \parallel R_3 \parallel R_4)} \right)$$

عكس Is

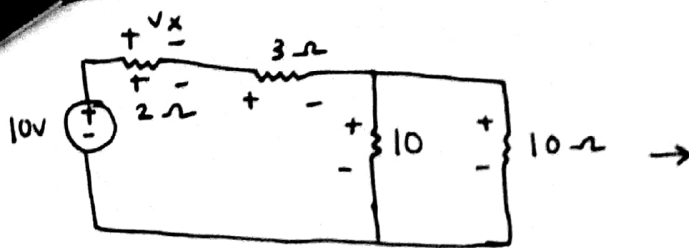
$$I_3 = - I_s \left(\frac{R_1 \parallel R_2 \parallel R_4}{R_3 + (R_1 \parallel R_2 \parallel R_4)} \right)$$

$$I_4 = + I_s \left(\frac{R_1 \parallel R_2 \parallel R_3}{R_4 + (R_1 \parallel R_2 \parallel R_3)} \right)$$

* السب ← محصلة المقاومة التي لا يمر فيها التيار المطلوب.

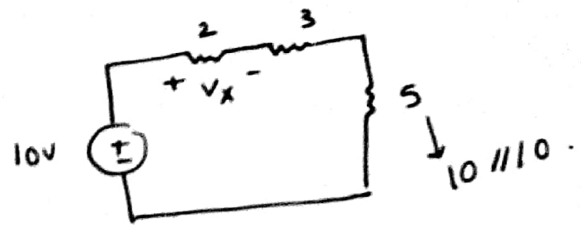
* المقام ← حاصل الجمع بين المقاومة المطلوبة عندها التيار ومحصلة المقاومة التي لا يمر فيها التيار المطلوب.

chice 3.15:



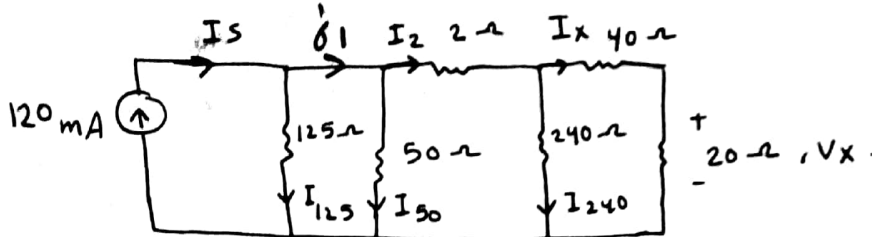
$$V_x = +10 * \left(\frac{2}{2+3+5} \right) = 2V$$

Find V_x ?



Series كسب كيرشوف

* Practice 3.16:



Find V_x ?

$$V_x = 20 I_x$$

* عنان اللمع I_x لدم اللمع i_2 وعنان اللمع i_2 بدي i_1 .

$$* i = + i_s \left(\frac{125}{125 + R_x} \right) = 100 \text{ mA} \checkmark$$

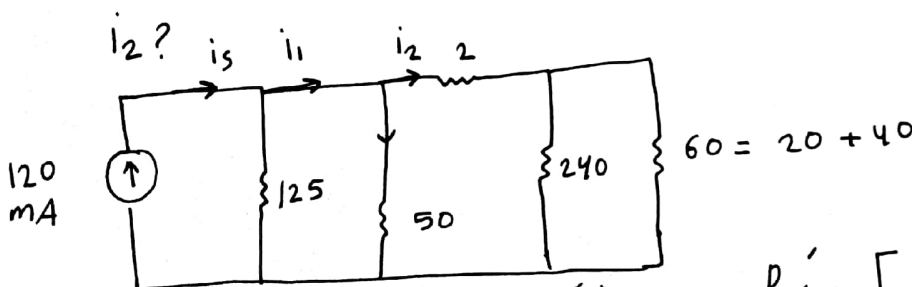
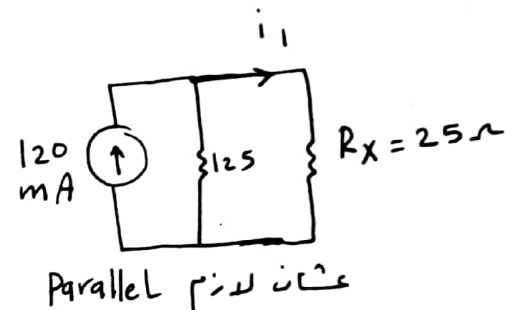
$R_s = 25\Omega$

$$* R_s = R_x + 125$$

$$\left[\left[(20 + 40) // 240 \right] + 2 \right] // 50$$

$$(60 // 240 = 48) + 2$$

$$= 50 // 50 = 25 \Omega$$



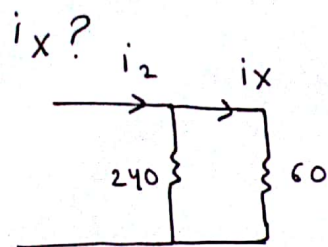
$$i_2 = i_1 \left(\frac{50}{50 + R_x'} \right)$$

$$= i_1 \left(\frac{50}{100} \right)$$

$$= 50 \text{ mA}$$

$$R_x' = [60 // 240] + 2$$

$$= 48 + 2 = 50$$



$$i_x = \left(\frac{240}{240 + 60} \right) i_2 = 40 \text{ mA}$$

$$V_x = i_x \times 20 = 40 \times 20 = 800 \text{ mV} = 0.8 \text{ V}$$

* CH. 4: Nodal and mesh analysis:

: (KCL) nodal *

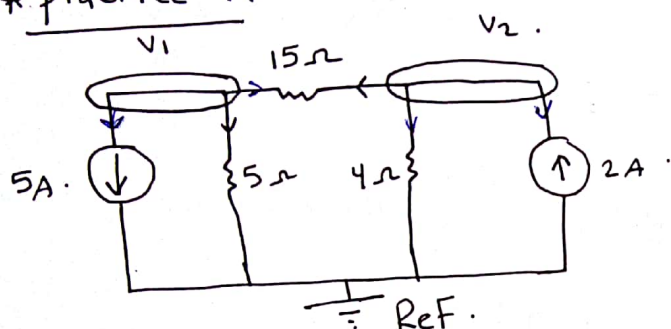
١. نحدد النقطة المرجعية (ref).

٢. نحدد الـ $V_1, V_2, V_3, \dots$

٣. نستخدم قانون أوم للتيار في اتجاهات بدلالة الجهد.

٤. نحل المعادلات على الآلة الحاسبة.

* practice 4.1:



KCL.

① apply KCL at node V_1 :

$$5 + \frac{V_1}{5} + \frac{V_1 - V_2}{15} = 0$$

$$V_1 \left(\frac{1}{5} + \frac{1}{15} \right) + V_2 \left(-\frac{1}{15} \right) = -5$$

$$0.267 V_1 - 0.067 V_2 = -5 \rightarrow \textcircled{1}$$

② apply KCL at node V_2 :

$$-2 + \frac{V_2}{4} + \frac{V_2 - V_1}{15} = 0$$

$$V_2 \left(\frac{1}{4} + \frac{1}{15} \right) + V_1 \left(-\frac{1}{15} \right) = 2$$

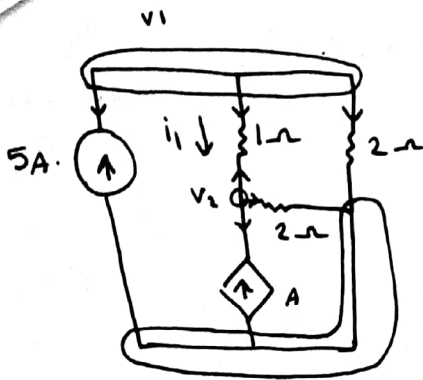
$$0.317 V_2 - 0.067 V_1 = 2$$

$$-0.067 V_1 + 0.317 V_2 = 2 \rightarrow \textcircled{2}$$

$$V_1 = -18.1 \text{ V}$$

$$V_2 = 2.482 \text{ V}$$

chce 4.3 :



h/s
Ref.
= 0V.

Find v_1 : ①
if $A = 2i_1$ and if $A = 2v_1$? ②

Sol:

* KCL at v_1 : $-5 + \frac{v_1 - v_2}{1} + \frac{v_1 - 0}{2} = 0 \rightarrow \boxed{3v_1 - 2v_2 = 10} \rightarrow ①$

* KCL at v_2 : $\frac{v_2 - v_1}{1} + \frac{v_2 - 0}{2} - A = 0$
 $\rightarrow 2v_2 - 2v_1 + v_2 - 2A = 0$ $\rightarrow$ ② $\rightarrow$ ②a

$\rightarrow \boxed{-2v_1 + 3v_2 - 2A = 0}$

if $A = 2i_1 = 2(i_1) = 2\left(\frac{v_1 - v_2}{1}\right) = 2v_1 - 2v_2$.

$\Rightarrow -2v_1 + 3v_2 - 4v_1 + 4v_2 = 0$

$\boxed{-6v_1 + 7v_2 = 0} \rightarrow ②b$

$v_1 = 70/9 \text{ V} , v_2 = 20/3 \text{ V} \checkmark$
 $7.78 \checkmark = 6.67 \text{ V}$

②b $\rightarrow A = 2v_1$.

$\Rightarrow -2v_1 + 3v_2 - 2(2v_1) = 0$

$-2v_1 + 3v_2 - 4v_1 = 0$

$-6v_1 + 3v_2 = 0$

① and ②b $\rightarrow \underline{v_1 = -10 \text{ V}, v_2 = -20 \text{ V} \checkmark}$

* Super node:

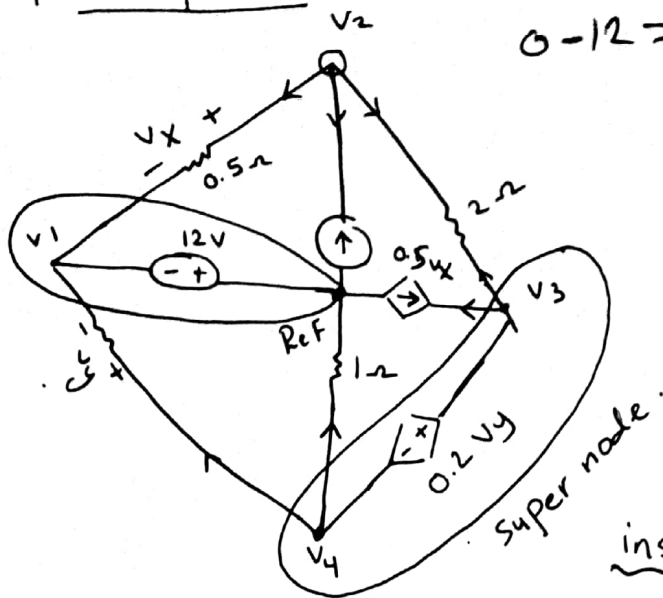


$v_B - v_A = X_v$

تو با كانت
القيمة

التي عند طرف
السورس
التي عند الطرف
الموجب للسورس

* Example 4.6:



$v_1 = -12 \text{ Volt}$
 $0 - 12 = v_1$ * KCL at node v_2 :

$$\frac{v_2 - v_1}{0.5} - 14 + \frac{v_2 - v_3}{2} = 0$$

$$4v_2 - 4v_1 + v_2 - v_3 = 28.$$

$$-4v_1 + 5v_2 - v_3 = 28 \rightarrow \textcircled{1}$$

$$5v_2 - v_3 = -20$$

* at Super node:

inside $\rightarrow v_3 - v_4 = 0.2v_y$

$$v_3 - v_4 = 0.2v_y - 0.2v_1$$

$$5v_3 - 5v_4 = v_4 - v_1$$

$$v_1 + 5v_3 - 6v_4 = 0 \rightarrow \textcircled{2}$$

$$5v_3 - 6v_4 = 12 \rightarrow \textcircled{2}$$

$v_y = v_4 - v_1 = v_4 + 12$

* KCL: (outside)

$$\frac{v_3 - v_2}{2} - 0.5(v_2 - v_1) + \frac{v_4}{1} + \frac{v_4 - (-12)}{2.5} = 0$$

$$5v_3 - 5v_2 - 5(v_2 + 12) + 10v_4 + 4v_4 + 4(12) = 0$$

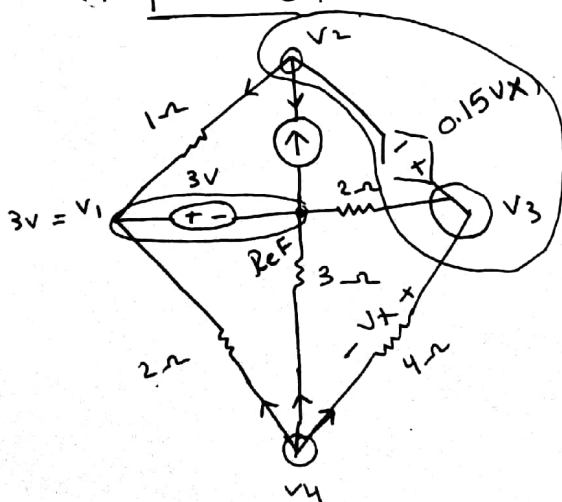
$$5v_3 - 5v_2 - 5v_2 - 60 + 10v_4 + 4v_4 + 48 = 0$$

$$v_2(-5-5) + v_3(5) + v_4(10+4) = 12$$

$$-10v_2 + 5v_3 + 14v_4 = 12 \rightarrow \textcircled{3}$$

$$v_2 = -4, v_3 = 0, v_4 = -2$$

* practice:



$$v_1 = 3V$$

KCL at node v_4 :

$$\frac{v_4 - v_3}{4} + \frac{v_4}{3} + \frac{v_4 - 3}{2} = 0$$

$$3v_4 - 3v_3 + 4v_4 + 6v_4 - 18 = 0$$

$$-3v_3 + v_4(3+4+6) = 18$$

$$-3v_3 + 13v_4 = 18 \textcircled{1}$$

7 amp 3.125 A

super node:

inside →

$$V_3 - V_2 = 0.15 (V_3 - V_4) \quad * 100$$

$$100 V_3 - 100 V_2 = 15 V_3 - 15 V_4$$

$$V_2 (-100) + V_3 (100 - 15) + V_4 (15) = 0$$

$$-100 V_2 + 85 V_3 + 15 V_4 = 0 \quad (2)$$

* kcl:

$$\frac{V_2 - 3}{1} - 4 + \frac{V_3}{2} + \frac{V_3 - V_4}{4} = 0 \quad * 4$$

$$4 V_2 - 12 - 16 + 2 V_3 + V_3 - V_4 = 0$$

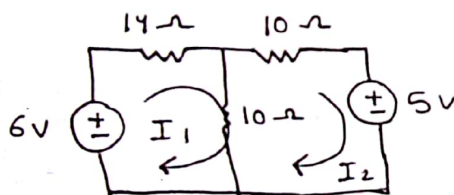
$$4 V_2 + 3 V_3 - V_4 = 28 \quad (3)$$

$$V_2 = 4.2122 \text{ V} / V_3 = 5.268 \text{ V} / V_4 = 2.4292 \text{ V}$$

* إلى صناديق الليزر

* Mesh analysis: (KVL)

* practice 4.6:



Find I_1, I_2 :

① kVL at loop 1:

$$-6 + 14 I_1 + 10 (I_1 - I_2) = 0$$

$$a = 14 + 10, \quad b = -10, \quad c = 6$$

$$= 24$$

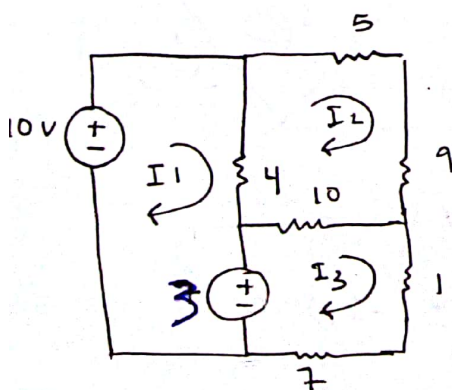
② kVL at loop 2:

$$10 (I_2 - I_1) + 10 I_2 + 5 = 0$$

$$a = -10, \quad b = 20, \quad c = -5$$

$$I_1 = 182.2 \text{ mA}, \quad I_2 = -157.9 \text{ mA} \quad \checkmark$$

* practice 4.7:



Find I_1, I_2, I_3 ?

Sol:

* kVL at loop 1:

$$-10 + 4 (I_1 - I_2) + 3 = 0$$

$$4 I_1 - 4 I_2 = 7$$

$$a = 4, \quad b = -4, \quad c = 0, \quad d = 7$$

* kVL at loop 2:

$$(5 + 9) I_2 + 10 (I_2 - I_3) + 4 (I_2 - I_1) = 0$$

$$a = -4, \quad b = 14 + 10 + 4, \quad c = -10, \quad d = 0$$

$$= 28$$

(7)

* KVL at loop 3:

$$-3 + 10(I_3 - I_2) + 8I_3 = 0$$

$$a = 0, b = -10, c = 18, d = 3$$

$$I_1 = 2.22 \text{ A}, I_2 = 0.47 \text{ A}, I_3 = 0.43 \text{ A} \checkmark$$

* Super Mesh: 4.9

③ 3A joins I_1 and I_3
(Super Mesh).

① KVL at loop 2:

$$4(I_2 - I_1) + 14(I_2) + 10(I_2 - I_3) = 0$$

$$a = -4, b = 4 + 14 + 10, c = -10, d = 0$$

$$= 28$$

* Super Mesh:

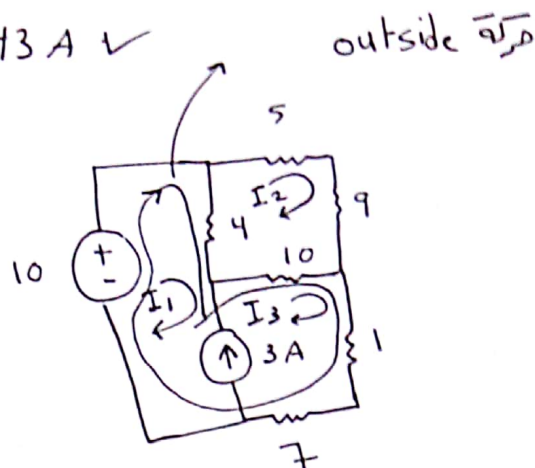
② inside: $3 = I_3 - I_1 \rightarrow a = -1, b = 0, c = 1, d = 3$

$$3A \text{ دالة } I_3 \quad 3A \text{ دالة } I_1$$

③ outside: $10 + 4(I_1 - I_2) + 10(I_3 - I_2) + 8(I_3) = 0$

$$a = 4, b = -4 - 10, c = 18, d = 10$$

$$= -14$$



* Practice 4.10:

Find V_3 ?

Sol:

① $-80 + 10I_1 + 20(I_1 - I_2) + 30(I_1 - I_3) = 0$ so

$$a = 60, b = -20, c = -30, d = 0$$

* For Super Mesh:

inside: $15I_1 = I_3 - I_2$

$$a = 15, b = 1, c = -1, d = 0$$

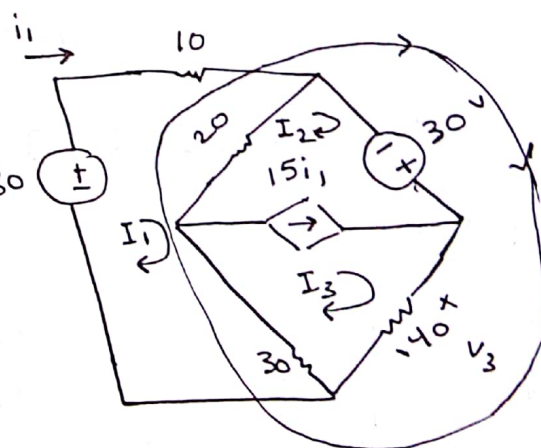
outside: ③ $-30 + 40(I_3) + 30(I_3 - I_1) + 20(I_2 - I_1) = 0$

$$a = -50, b = 20, c = 70, d = 30$$

$$I_1 = 0.584 \text{ A}, I_2 = -6.15, I_3 = 2.604, V_3 = +I_3(40)$$

$$= 104.2 \text{ V}$$

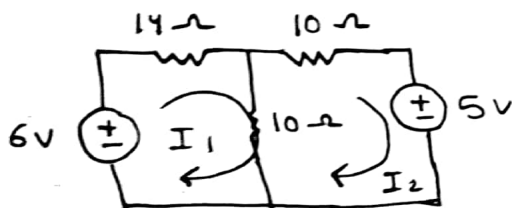
* التاب دائماً بنقله للطرف الأيسر.



$$* 15i_1 = 15I_1$$

* Mesh analysis: (KVL)

* practice 4.6:



Find I_1, I_2 :

① kVL at loop 1:

$$-6 + 14I_1 + 10(I_1 - I_2) = 0$$

$$a = 14 + 10, \quad b = -10, \quad c = 6$$

$$= 24$$

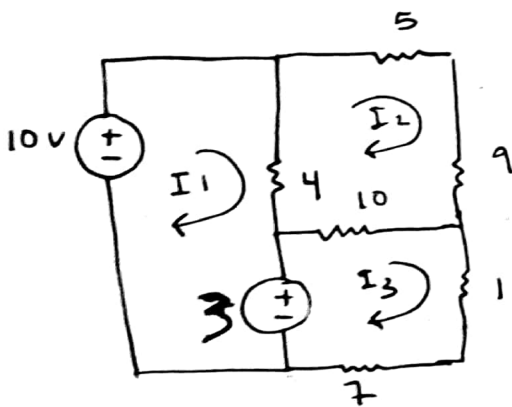
② kVL at loop 2:

$$10(I_2 - I_1) + 10I_2 + 5 = 0$$

$$a = -10, \quad b = 20, \quad c = -5$$

$$I_1 = 182.2 \text{ mA}, \quad I_2 = -157.9 \text{ mA} \quad \checkmark$$

* practice 4.7:



Find I_1, I_2, I_3 ?

Sol:

* kVL at loop 1:

$$-10 + 4(I_1 - I_2) + 3 = 0$$

$$4I_1 - 4I_2 = 7$$

$$a = 4, \quad b = -4, \quad c = 0, \quad d = 7$$

* kVL at loop 2:

$$(5 + 9)I_2 + 10(I_2 - I_3) + 4(I_2 - I_1) = 0$$

$$a = -9, \quad b = 14 + 10 + 4, \quad c = -10, \quad d = 0$$

$$= 28$$

(13)

* KVL at loop 3:

$$-3 + 10(I_3 - I_2) + 8I_3 = 0$$

$$a = 0, b = -10, c = 18, d = 3$$

$$I_1 = 2.22 A, I_2 = 0.47 A, I_3 = 0.43 A \checkmark$$

* Super Mesh: 4.9

② 3A joins I_1 and I_3
(Super Mesh).

① KVL at loop 2:

$$4(I_2 - I_1) + 14(I_2) + 10(I_2 - I_3) = 0$$

$$a = -4, b = 4 + 14 + 10, c = -10, d = 0 \\ = 28$$

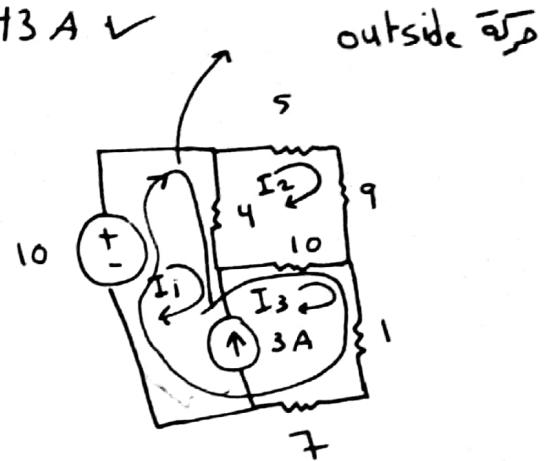
* Super Mesh:

$$② \text{ inside: } 3 = I_3 - I_1 \rightarrow a = -1, b = 0, c = 1, d = 3$$

$$3A \text{ joins } I_1 \text{ and } I_3$$

$$③ \text{ outside: } 10 + 4(I_1 - I_2) + 10(I_3 - I_2) + 8(I_3) = 0$$

$$a = 4, b = -4 - 10, c = 18, d = 10 \\ = -14$$



* practice 4.10:

Find V_3 ?

Sol:

$$① -80 + 10I_1 + 20(I_1 - I_2) + 30(I_1 - I_3) = 0 \text{ so}$$

$$a = 60, b = -20, c = -30, d = 0$$

* For Super Mesh:

$$\text{inside } ② 15I_1 = I_3 - I_2$$

$$a = 15, b = 1, c = -1, d = 0$$

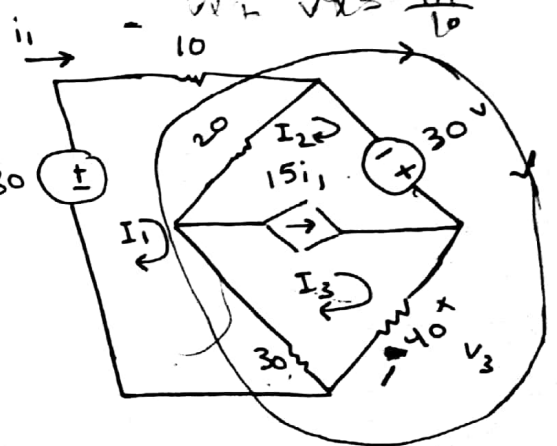
$$\text{out side } ③ -30 + 40(I_3) + 30(I_3 - I_1) + 20(I_2 - I_1) = 0$$

$$a = -50, b = 20, c = 70, d = 30$$

$$I_1 = 0.584 A, I_2 = -6.15, I_3 = 2.604, V_3 = +I_3(40)$$

$$= 104.2V$$

* ثابت دائماً بنقله للطرف الأيسر

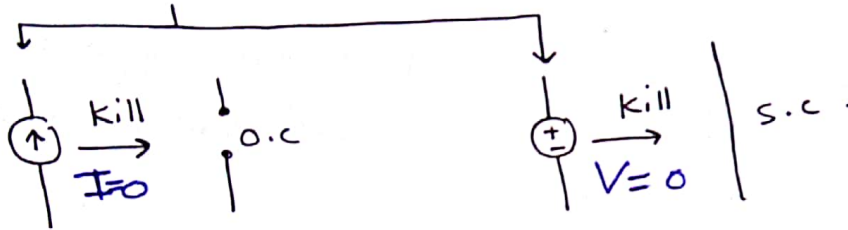


$$* 15i_1 = 15I_1$$

* Super position:

- من خلاله نتقدر نعرف دور كل سورس في الدارة / شوي يتوصله باقي العناصر.

- بتبطل واحد كل مرة وبنتغير إجابتي (Killing the source).



* practice 5.2:

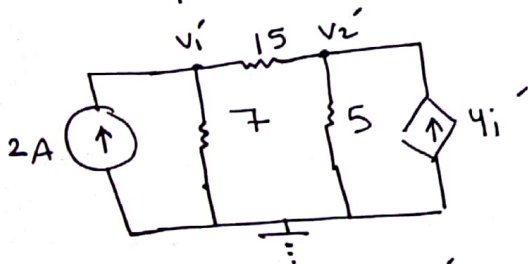
Find: V_1, V_2 due to each current and voltage source:

: Sol

* due to 2A: (بقي طاري 2A سغال وطافي الباقي)

Kill 3V $\rightarrow$ s.c

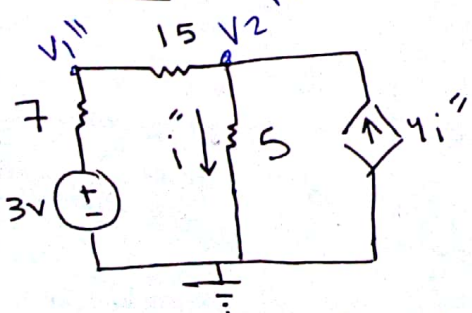
* (Killing the source is only for indep sources).



nodal $\rightarrow V_1, V_2$ (طريقة الفيرست) مناخه

* due to 3V:

Kill 2A $\rightarrow$ o.c



nodal $\rightarrow V_1, V_2$ مناخه

* الناتج النهائي يكون على شكل:

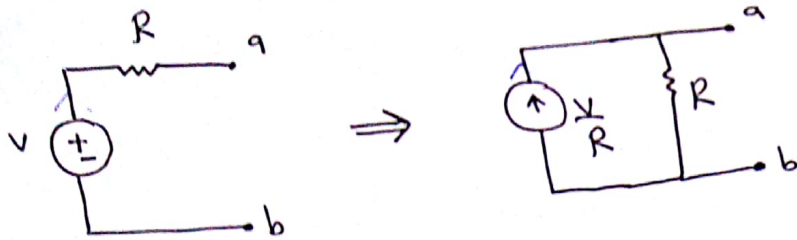
$$V_1 = V_1' + V_1''$$

(كلتا)

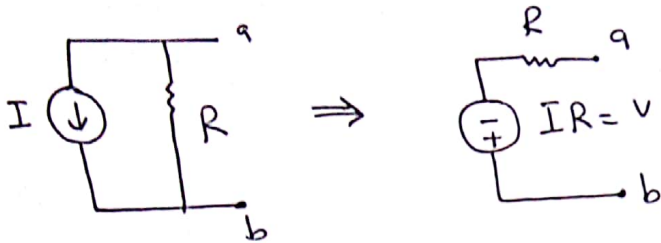
$$V_2 = V_2' + V_2''$$

(كلتا)

* 5.2: Source transformation:



* اتجاه التيار في السورس الجديد طالع من الموجب مع السورس القديم

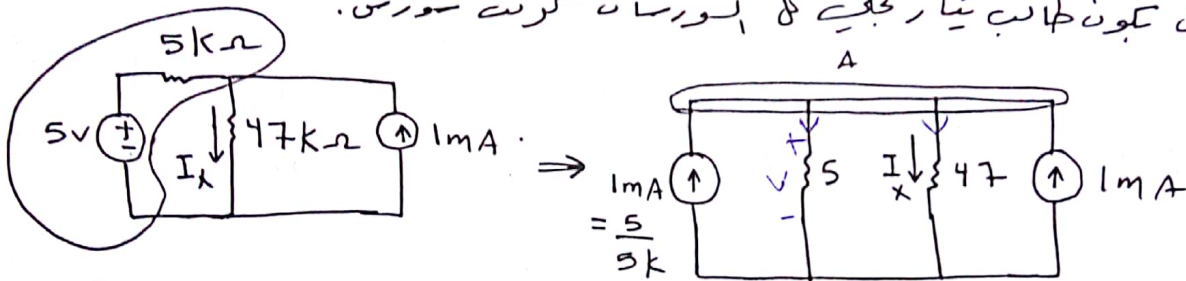


* قطبية الفولتج الجديد موجبة من محل ما طلع التيار من السورس القديم

* practice 5.3:

Find I_x by S.T?

* السؤال يكون طالع تيار رجلي كل السورسات كرنه سورس



* KCL at node A:

$$-1 - 1 + \frac{V}{5} + \frac{V}{47} = 0$$

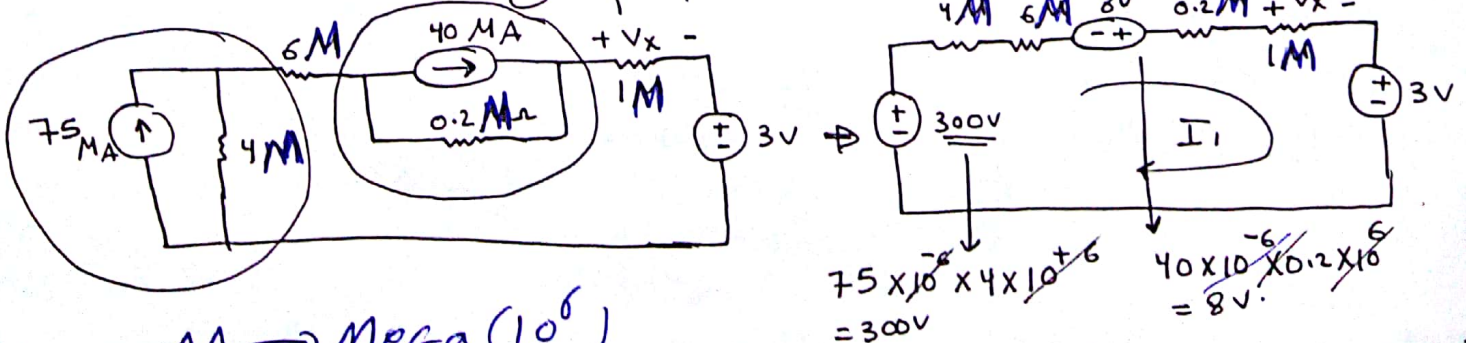
$$V = 9.04 \text{ volt}$$

$$I_x = \frac{V}{47k} = 192.3 \mu A \checkmark$$

* practice 5.4:

Find V_x by S.T?

* السؤال طالع مولتيه جادل اقليم ظلم فونج سورس



$$M \Rightarrow \text{Mega} (10^6)$$

$$\mu \Rightarrow \text{Micro} (10^{-6})$$

* المتاهات باطبعا

* KVL:

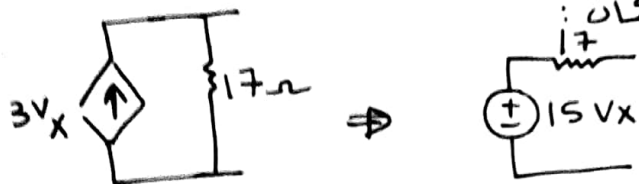
$$-300 + i(4 + 6 + 0.2 + 1) - 8 + 3 = 0$$

$$I = \frac{300 + 8 - 3}{11.2} = 27.23 \text{ mA}$$

له باللا يكون لانه لقا، مات كانت بالبحا.

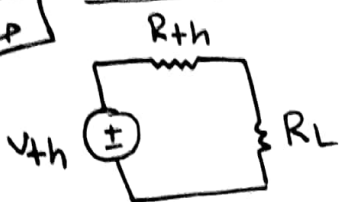
$$V_X = IR = 27.23 \text{ M} \times \text{M} = 27.23 \text{ V.}$$

ملاحظة: ال S.T نبفع لا dep sources



* Thevenin and Norton eq cct:

صق

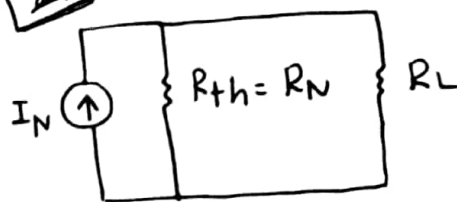


The eq cct:

$$R_{th} = R_N$$

$$I_N = \frac{V_{th}}{R_N} = \frac{V_{th}}{R_{th}}$$

صق



N eq cct:

$$V_{th} = I_N R_N$$

نقته القانوت.

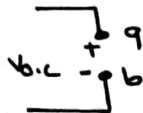
* Case 1: R + ind p

* Case 2: R + ind + dep.

* Case 1: R + ind:

١. بفعل RL وخط حلها 0.c واسبب Vo.c عليها وهايه إتوليتة صي نقشا Vth

$$V_{o.c} = V_{th}$$



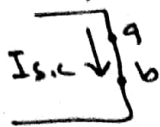
٢. فب Req الـ بنشوفها بين اطراف RL سببا نشيفها ونسج ما نخل Kill للسورسات على فرض انه كلم ind

$$I_N = \frac{V_{th}}{R_{th}}$$

← اذا كنت حاسب Vth , Rth

٢. عنان اصب IN

← اذا بيدي اصبا قبل ما اصب Rth و Vth بعمل شورت سيركتة على اطراف RL



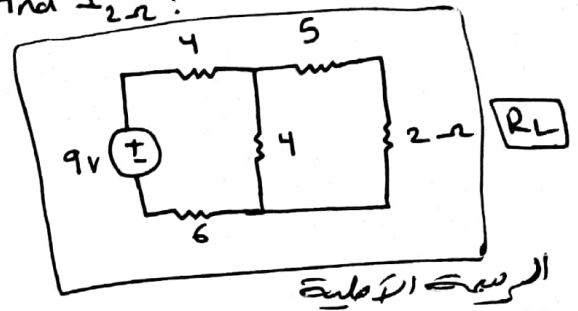
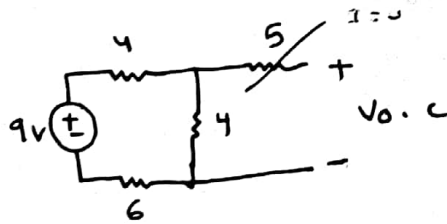
(١٧)

* practice 5.6:

Find: V_{th} , R_{th} , I_N at $R_L = 2\Omega$ and Find $I_{2\Omega}$?

* For V_{th} :

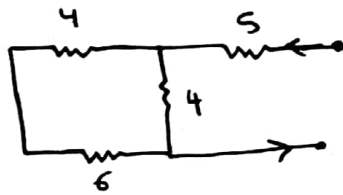
$V_{o.c}$ at R_L :



$$V_{o.c} = V_{4\Omega} = V_{th} = 9 \times \left(\frac{4}{4+4+6} \right) = 2.57V.$$

* For R_{th} :

Req between R_L terminals after killing the sources (only indep):

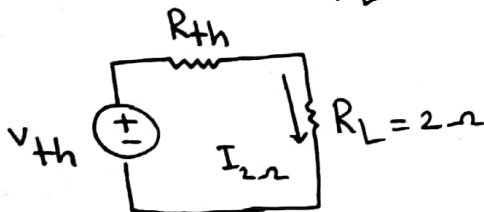


$$\Rightarrow R_{eq} = [4 \parallel 6] + 5 = 7.857\Omega.$$

* For I_N :

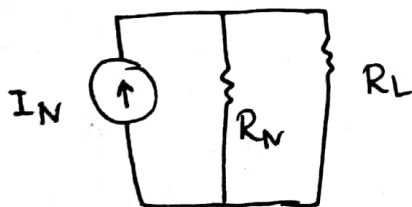
$$I_N = \frac{V_{th}}{R_{th}} = \frac{2.57}{7.857} = 327.2mA.$$

* For $I_{2\Omega} = I_{RL} \neq I_N$.



$$\Rightarrow I_{2\Omega} = \frac{V_{th}}{R_{th} + R_L} = \frac{2.57}{7.857 + 2} = 260.8mA.$$

OR



$$\Rightarrow I_{RL} = I_N \left(\frac{R_N}{R_L + R_N} \right) = 327.2 \left(\frac{7.857}{2 + 7.857} \right) = 260.8mA.$$

* Case 2: ind + dep + R.

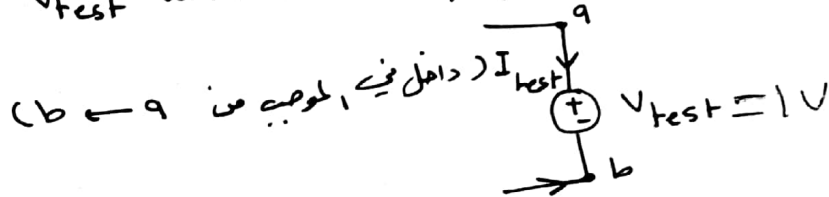
method 1:

1. Calculate $V_{o.c}$ at R_L
2. $I_{s.c}$ at R_L
3. $R_{th} = \frac{V_{o.c}}{I_{s.c}} = \frac{V_{th}}{I_N}$

* ملاحظة: ما قبل احسبنا عن طريق Req لان هون ما بقدر نعمل Kill لل dep.

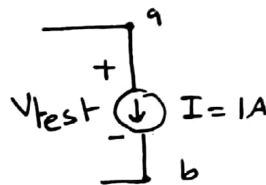
method 2:

1. Kill ind. sources. (فجّل dep كفاين).
2. Put V_{test} with $\Rightarrow V = 1V$, Then calculate $I_{test} \rightarrow R_{th} = \frac{1}{I_{test}}$.



3. put I_{test} with $\Rightarrow I = 1A$, Then calculate $V_{test} \rightarrow R_{th} = V_{test}$.

* عند حساب الموصّل
الطبيعي

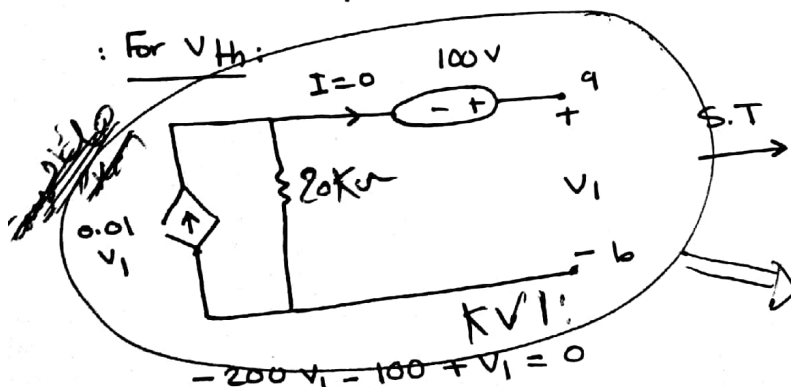


* ملاحظة: هاي بب ستغير من انا احيي R_{th} لا
($V_{test} \neq V_{th}$)
 $I_{test} \neq I_N$.

* practice 5.8:

Find the eq cct? (V_{th} , R_{th} , I_N).

: For V_{th} :



$$-200V_1 - 100 + V_1 = 0$$

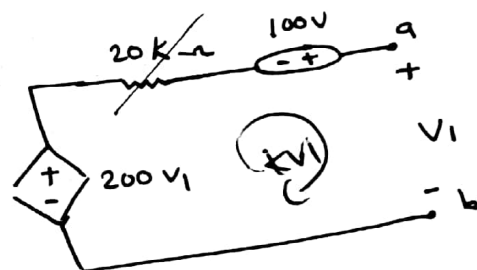
$$V_1(-200 + 1) = 100$$

$$V_1 = 100 / -199 = -502.5m = V_{th}$$

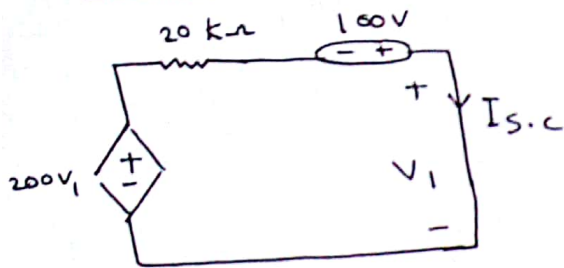
$$V_1 = V_{th}$$

+ الملاحظة بالأساس عليها 0 بين a و b ←

من السؤال
o.c



: For I_N :



$$* V_1 = V_{S.C} = 0$$

$$200 V_1 = 0$$

$$*(20k)I - 100 = 0$$

$$I = 5mA$$

: For R_{th} : $V_{th} / I_N = -100.5 \Omega$.

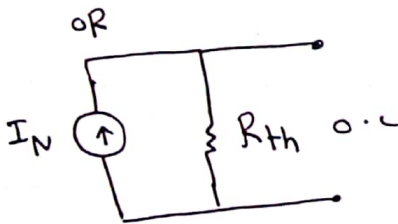
* اطلب منا للدلالة على ان هناك مقاومة $+100.5$ دكن التيار يكون داخل في القبة
السالبة للمقاومة.

* بالامكان اذا كان بالجارات كالتالي لست اسوال:

a) 100.5 , b) -100.5 , c) none .

or

a) 50.1 , b) -100.5 , c) none



* practice 5.8:

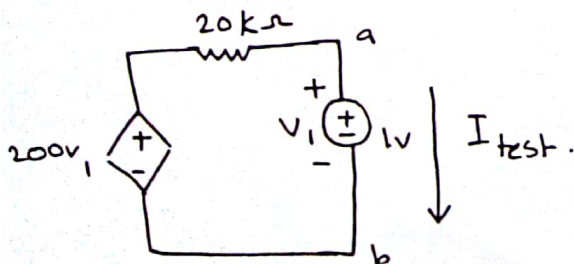
* لست اسوال السابق نكن بدلي احب ال R_{th} باستخدام

ال Test Source .

: Sol:

1. Kill all ind sources.

2. put $V_{test} = 1V$.



$$V_{test} = 1 \text{ volt}.$$

$$V_1 = 1 \text{ volt}.$$

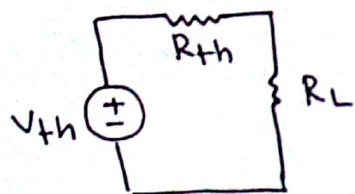
$$200 V_1 = 200 \text{ volt}.$$

$$\text{KVL: } -200 + 20k(I) + 1 = 0$$

$$I_{test} = \frac{200-1}{20k} = 9.95 \text{ mA} \checkmark$$

$$R_{th} = 1 / I_{test} = 100.5 \Omega.$$

5.4: Maximum power transfer:



$$P_{at R_L} = \frac{V^2}{R_L} = \left(\frac{V_{th} \cdot R_L}{R_L + R_{th}} \right)^2 \cdot \frac{1}{R_L} = \frac{V_{th}^2 \cdot R_L}{(R_L + R_{th})^2}$$

$\downarrow$ certain value (قيمة معينة)
 $\downarrow$ voltage divider.
 $\downarrow$ هنا

At maximum power $\rightarrow R_L = R_{th} \rightarrow P_{Max} = \frac{V_{th}^2}{4 R_{th}}$ هنا

① What is R_L at Maximum power? ($R_L \mid = R_{th}$)
Max power

② What is the Maximum power delivered by R_L ?

$$P_{Max} = \frac{V_{th}^2}{4 R_{th}} \leftarrow R_{th} \approx V_{th} \text{ حسب}$$

③ What is the values of R_L at a certain power?

بعض قيم غير Maximum

$$P = \frac{V_{th}^2 R_L}{(R_{th} + R_L)^2}$$

$\rightarrow$ تكون R_{th} , V_{th} في والد P في حسب هنا
قيم R_L بتعمل الصيغة التربيعية.

* practice 5.10:

a) if $R_{out} = 3k\Omega$

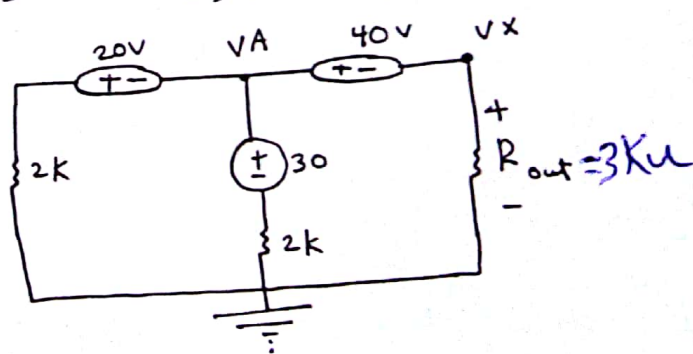
Find power delivered to it (P_{abs})?

use nodal $\rightarrow V_A = 13.75$

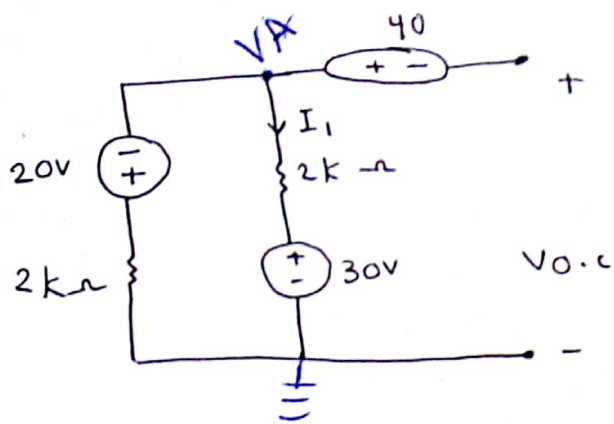
$$V_A - V_X = 40 \rightarrow V_X = -26.25V$$

$$\rightarrow V_{R_{out}} = V_{X-0} = -26.25V$$

$$P_{abs} = \frac{V^2}{R} = \frac{689.0625}{3 \times 1000} = 0.230W = 230mW$$



b) Find V_{th} at R_{out} ? and R_{th} ? P_{Max} at any R_L ?



$$V_A = 5V$$

$$\xrightarrow{\text{nodal}} I_1 = \frac{5 - 30}{2} = -12.5 \text{ mA} \checkmark$$

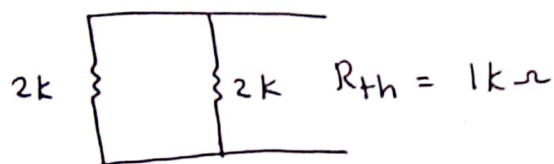
$$-V_{oc} - 40 + I_1(2) + 30 = 0$$

$$V_{th} = -40 - 12.5 \times 2 + 30$$

$$= -40 + 30 + (-25)$$

$$= -35V \checkmark$$

$R_{th} \rightarrow$ Kill all indep sources: (s.c)



voltage source. $\rightarrow$ Δ $\rightarrow$ Δ

$$P_{Max} \text{ at any } R_L = P_{Max} \Big|_{R_L = R_{th}} = \frac{V_{th}^2}{4R_{th}} = \frac{(-35)^2}{4 \times 1000} = 306 \text{ mW}.$$

c) Find R_L values if $p = 20 \text{ mW}$?

$$P_{at} \Big|_{R_L = ?} = 20 \text{ mW} \quad \left(\begin{array}{l} \text{Maximum} \\ R_L \neq R_{th} \end{array} \right)$$

$$P = \frac{V_{th}^2 R_L}{(R_L + R_{th})^2} \rightarrow 20 \times 10^{-3} = \frac{1225 R_L}{(1000 + R_{th})^2}$$

$$\rightarrow 0.02 R_L^2 - 1205 R_L + 20000 = 0$$

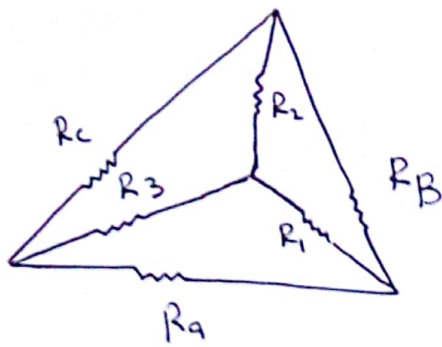
* كلاً له علاقة ما بفرم كان الثابت بعد المسألة يعني لا نريد بعد المسألة تكون صفر
بن. (هو مثل النور والليست).

$$a = 0.02, b = -1205, c = 20000$$

$$R_{L1} = 60.26 \text{ k}\Omega / R_{L2} = 16.60 \Omega$$

* إذا طلع منجم وحدة سايه ما هو هذا.

5.5: delt to why transformation:



$\Delta \rightarrow Y$

$$R_1 = \frac{R_A R_B}{R_A + R_B + R_C}$$

$$R_2 = \frac{R_B R_C}{R_A + R_B + R_C}$$

$$R_3 = \frac{R_A R_C}{R_A + R_B + R_C}$$

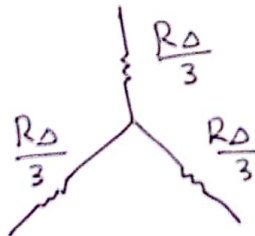
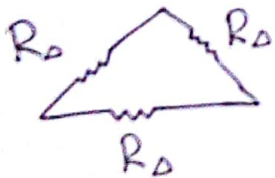
$Y \rightarrow \Delta$

$$R_A = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_3}$$

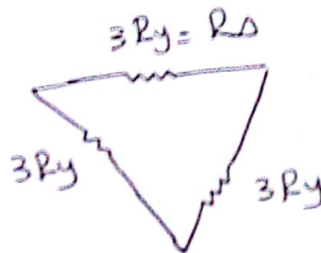
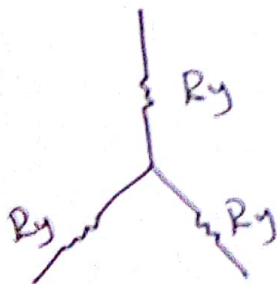
$$R_B = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_2}$$

$$R_C = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_1}$$

Δ to Y, Y to Δ

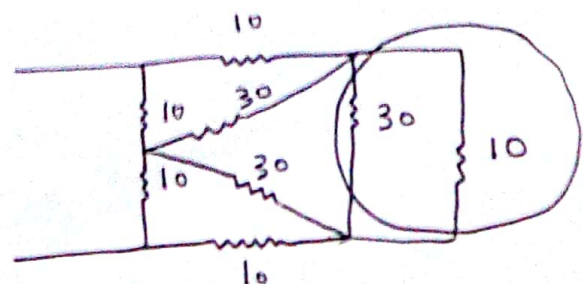
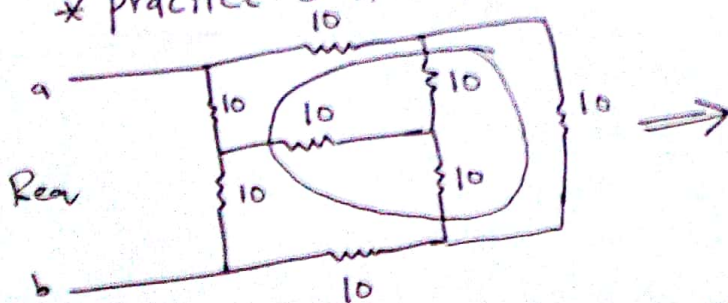


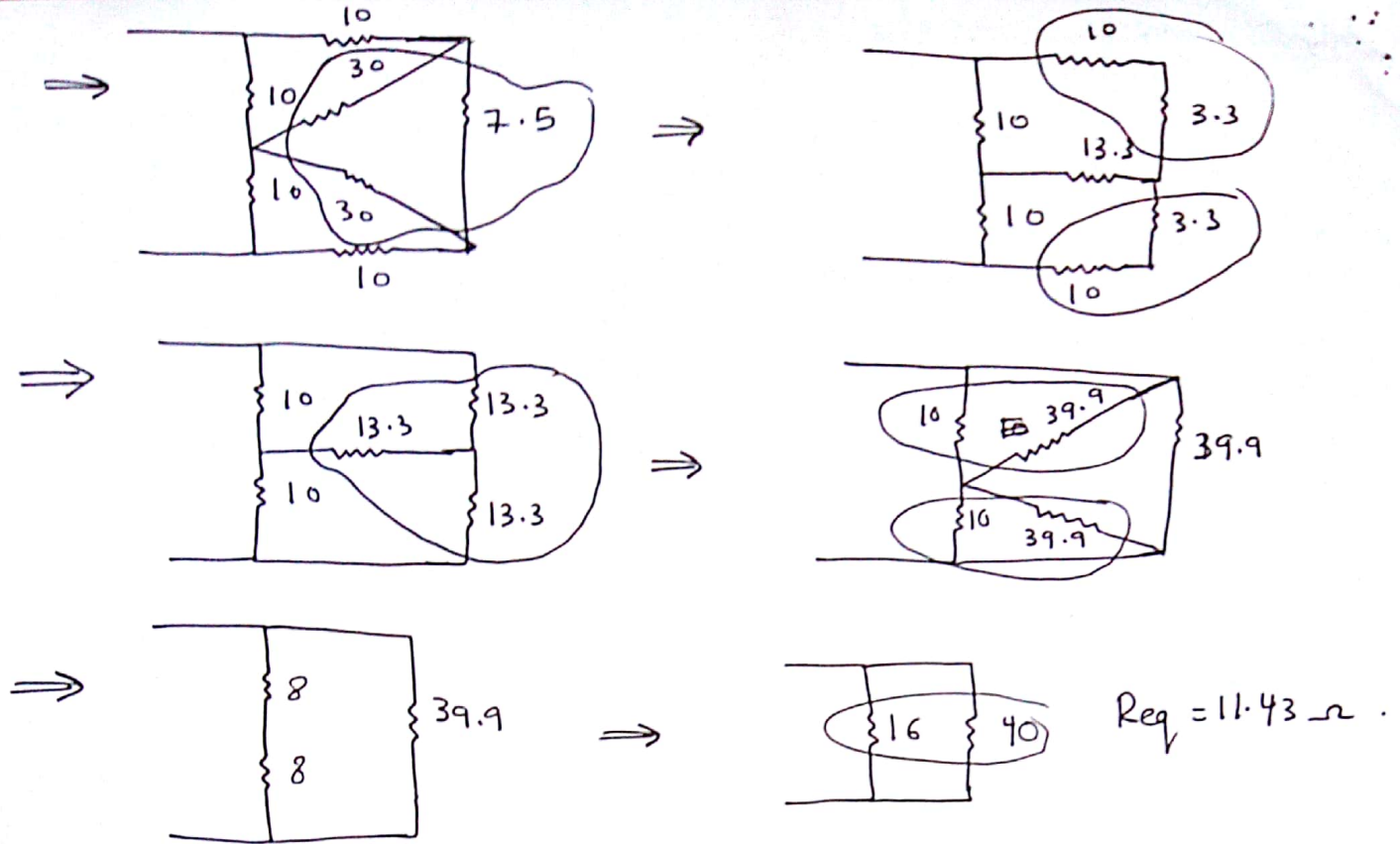
$$R_Y = \frac{R_\Delta}{3}$$



$$R_\Delta = 3R_Y$$

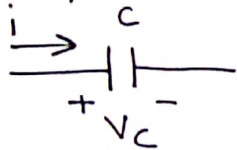
* Practice 5.11: $R=10$ For each; Find Req?





* CH. 7: Inductor and capacitor

Capacitor



$$i = C \frac{dv}{dt} = C \frac{\Delta V}{\Delta t}$$

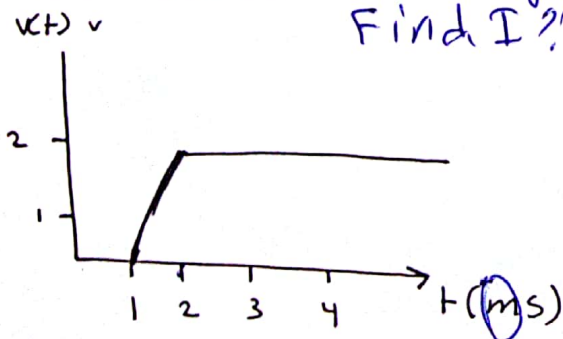
نسبة التغير في الجهد إلى الزمن
نسبة التغير في الجهد إلى الزمن

$$* V_C(t) = \frac{1}{C} \int_{t_0}^t i_C(t) \cdot dt + V(t_0)$$

* الجهد في المواسع متصل (لا يتغير) يكون قانونه تكامل.

* practice 7.1: $C = 100 \text{ pF}$

Find I ??



$C = 100 \text{ pF}$

Find I ?

* SOL

نقسم الحركة لثلاث (كل قطعة اياها ميل واحد بأخذها بفترة وحدة)

For $t \leq 1 \rightarrow \text{slope} = 0 \rightarrow I = C \frac{dv}{dt} = C \cdot \text{slope} = 0$

For $1 \leq t \leq 2 \rightarrow \text{slope} = \frac{2-0}{2-1} = 2 \rightarrow I_C = 200 \text{ nA}$
 $= 100 \times 10^{-12} \times 2 \times 10^3$

For $t \geq 2 \rightarrow \text{slope} = 0 \rightarrow I = 0$

* For DC Source (For long time) $\rightarrow C \rightarrow 0.C$
 $\frac{1}{T} \rightarrow \frac{1}{1}$

$$I_C = 0, V_C = V_{O.C}$$

نفسها بطرق الفيرستاد
 السكند

* For AC:

$$* I_C = C \frac{dV}{dt}, V_C = \int_{t_0}^t I_C \cdot dt + V_C(t_0)$$

$$* W_C(t) = \frac{1}{2} C V_C^2(t) \rightarrow \text{stored energy in capacitor. (Joul)}$$

$$* P_C(t) = I_C(t) V_C(t)$$

* capacitors $\rightarrow$ series $\rightarrow C_{eq}^{-1} = C_1^{-1} + C_2^{-1} + C_3^{-1} + \dots$
 $\rightarrow$ Parallel $\rightarrow C_{eq} = C_1 + C_2 + C_3 + \dots$

* practice 7.3:

$W_C(t)$ stored in 1mF at $t = 50$ if $V_C(t) = 1.5 \cos(10^5 t)$ V? rad

SOL

$$W_C(50M) = \frac{1}{2} C V^2(50M) =$$

$$* V = 1.5 \cos(286.62) = 0.43$$

$$W_C = \frac{1}{2} \times 10^{-3} \times 0.184 = 92.52 \text{ MJ} \checkmark$$

$$V(50M) = 1.5 \cos(10^5 \times 50 \times 10^{-6})$$

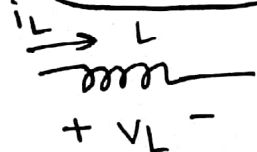
$$= 1.5 \cos \frac{5}{\text{Rad.}}$$

$$\frac{\pi}{5} = \frac{180}{\theta}$$

$$\theta = \frac{180 \times 5}{3.14} = 286.62.$$

أو بنسبة 5 وبقول الـ θ الحاسبة من $R \leftarrow D$

* Inductor



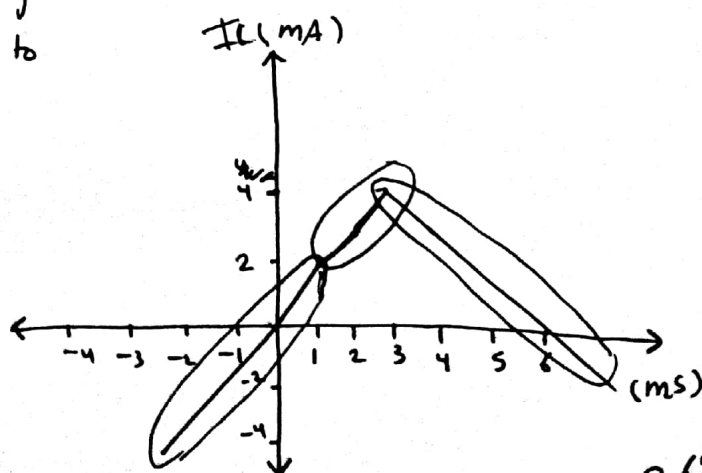
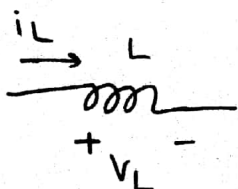
$$V_L = L \frac{dI}{dt} = L \frac{\Delta I}{\Delta t}$$

$$I_L(t) = \frac{1}{L} \int_{t_0}^t V_L(t) + I(t_0)$$

- 1) shift
- 2) mode
- 3) 4-Rad

* practice 7.4:

$L = 200 \text{ mH}$, Assume passive sign
 (داخل في الموجبة)



Find V_L at t equal?

a) $t=0 \rightarrow$ slope of the line
معدل التغير

$$\text{slope} = \frac{2 - (-2)}{1 - (-1)} = 2$$

$$V_L = L \frac{di}{dt} = L \times \text{slope} = 0.2 \times 2 = 0.4 \text{ V}$$

b) $t=2 \text{ ms} \rightarrow \text{slope} = \frac{4-2}{3-1} = 1, V = 0.2 \times 1 = 0.2 \text{ V}$

c) $t=6 \text{ ms} \rightarrow \text{slope} = \frac{0-4}{6-3} = -\frac{4}{3}, V = \frac{0.2 \times -4}{3} = -0.267 \text{ V}$

* For DC Source : (For long time)

$V_L = 0, I_L = I_{S.C}$
بغضها بقرت المغرمت
او المعنى

$\left. \begin{array}{c} | \\ | \\ | \end{array} \right\} \rightarrow | \text{ S.C}$

* For AC Source:

$$V_L(t) = L \frac{di}{dt}, I_L(t) = \frac{1}{L} \int_{t_0}^t V_L(t) \cdot dt + I_L(t_0)$$

* $W_L(t) = \frac{1}{2} L I^2(t)$

* $P_L(t) = V(t) I(t)$

* Inductor $\left\{ \begin{array}{l} \rightarrow \text{series} \\ \rightarrow \text{Parallel} \end{array} \right.$ نفس القابلات

Practice 7.6:

$L = 0.1 \text{ H}, V_L(t) = 2e^{-3t} \text{ V}, i_L(-0.5) = 1, \text{ Find } i_L?$

Sol: $i_L = \frac{1}{L} \int_{t_0}^t V_L(t) \cdot dt + I(t_0) = \frac{1}{0.1} \int_{-0.5}^t 2e^{-3t} \cdot dt + 1$

$$= \frac{20}{-3} e^{-3t} \Big|_{-0.5}^t + 1 = \frac{20}{-3} (e^{-3t} - e^{1.5}) + 1 = -\frac{20}{3} e^{-3t} + 29.9 + 1$$

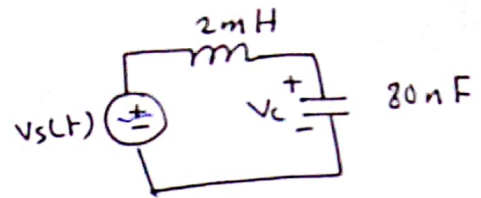
$$= \boxed{-\frac{20}{3} e^{-3t} + 30.9} \text{ A}$$

-26-

Practice 7.9 :

$L = 2 \text{ mH}$, $C = 80 \text{ nF}$, $V_C = 4 \cos 10^5 t \text{ V}$, Find $V_S(t)$?

$$* V_S(t) = V_C(t) + V_L(t) \\ = 4 \cos(10^5 t) + \boxed{V_L(t)}?$$



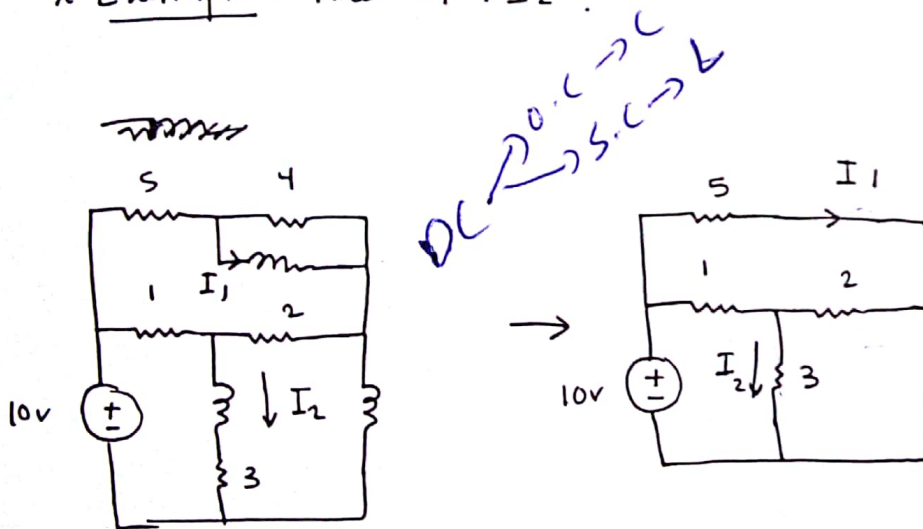
$$V_L(t) = L \frac{dI_L}{dt}; I_L = I_C \text{ (series)}.$$

$$I_C = C \frac{dV_C}{dt} = 80 \times 10^{-9} (4 \times -10^5 \sin 10^5 t) = -0.032 \sin 10^5 t \text{ A}.$$

$$V_L(t) = L \frac{dI_L}{dt} = 2 \times 10^{-3} (-0.032 \times 10^5 \cos 10^5 t) = -6.4 \cos 10^5 t \text{ V}$$

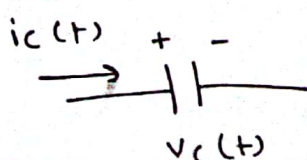
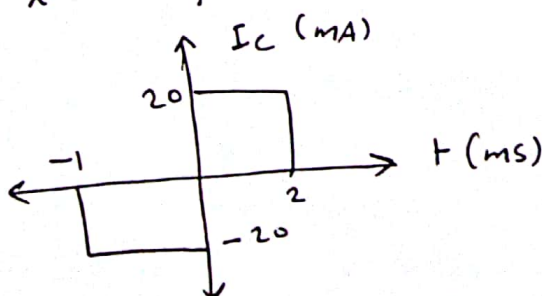
$$V_S(t) = 4 \cos 10^5 t - 6.4 \cos 10^5 t = \boxed{-2.4 \cos 10^5 t \text{ V}}.$$

* Example: Find I_1, I_2 ?



Mesh analysis

* Example: $C = 5 \text{ MF}$



sketch $V_C(t)$?

$$v_c(t) = \frac{1}{C} \int_{t_0}^t I_c(t) \cdot dt + v(t_0)$$

* نقسم التيار الى فترات من $(-\infty \rightarrow \infty)$
 * نغيره باثران متعكبان.

$$I_c(t) = \begin{cases} 0 \text{ m,} & -\infty < t < -1 \\ -20 \text{ m,} & -1 < t < 0 \\ 20 \text{ m,} & 0 < t < 2 \\ 0, & 2 < t < \infty \end{cases}$$

⊕ مائناً $v_c(t)$ التي تقطع بالسؤال تكون
 لفترة معينة راسية ثابتة لكل فترة.

⊖ $v_c(t)$ For $-\infty < t < -1$

$$v_c(t) = \frac{1}{C} \int_{-\infty}^t 0 \cdot dt + v(-\infty) = \boxed{0}$$

⊖ $v_c(t)$ For $-1 < t < 0$ ms.

$$= \frac{1}{C} \int_{-1}^t -20 \text{ m} \cdot dt + v(-1) \rightarrow \text{نطلعها من الفترة اللي قبل}$$

$$= -\frac{20 \text{ m}}{5 \mu\text{F}} \int_{-1}^t dt + 0$$

$$= -4 \text{ k} (t + 1 \text{ ms}) = 0$$

$$= \boxed{-4000t - 4} \text{ V}$$

⊖ $v_c(t)$ For $0 < t < 2$.

$$v_c(t) = \frac{1}{C} \int_0^t 20 \text{ m} \cdot dt + v_c(0)$$

$$= 4 \text{ k} \int_0^t dt + [-4000(0) - 4] = \boxed{4000t - 4} \text{ V}$$

⊖ $v_c(t)$ For $2 < t < \infty$

$$v_c(t) = \frac{1}{C} \int_2^t 0 \cdot dt + v_c(2) = 4000(2 \text{ m}) - 4 = 8 - 4 = \boxed{4 \text{ V}}$$

* طريقة الرسم : نبرعن $V_C(t)$ باثنان تشبي (مقسق) :

$$V_C(t) = \begin{cases} 0 & , -\infty \leq t \leq 1m \\ -4000t - 4, & -1 \leq t \leq 0m \\ 4000t - 4, & 0 \leq t \leq 2m \\ 4 & , 2 \leq t \leq \infty m \end{cases}$$

مناهل الزمن :

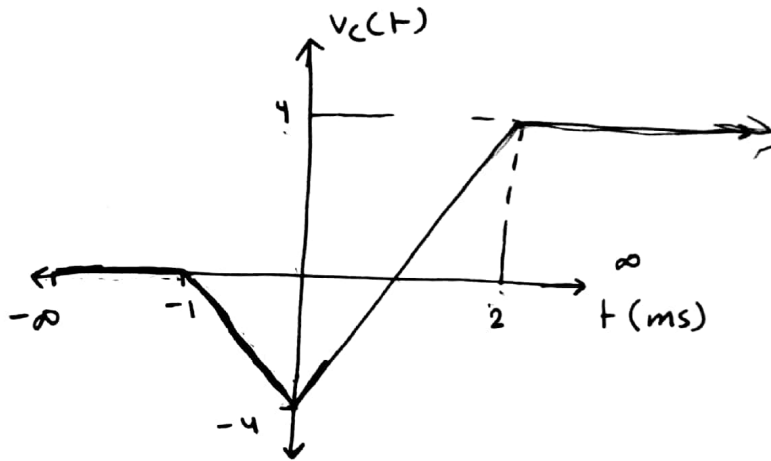
$$-\infty \rightarrow V = 0V$$

$$-1ms \rightarrow V = 0V$$

$$0 \rightarrow V = -4V$$

$$2ms \rightarrow V = 4V$$

$$\infty \rightarrow V = 4V$$



* energy $\rightarrow \frac{1}{2} C V_C^2(t)$

* change in energy $\rightarrow \frac{1}{2} C [V_C(t)^2 - V_C(t_0)^2]$

$\frac{1}{2} C [\dots]$ (بداية التفرع في الحركة)
اد $\rightarrow -\infty$

* اذا كانت معطاه نجعلها 0

* الى هنا مادة الكند