

" Power Amp's (Large Signal Amp)"

• Compared to S-S Amp :-

1) Deal with Large Signals.

2) The power devices have large size, high power dissipation, high rating :-

For ex.	S-S Tran.	Power Tran.
$I_{C\max}$	0.8 A	7 A
$V_{CE\max}$	40 V	250 V
$P_o\max$	1.2 W	45 W
B	100 → 30	20 → 70

بأنها كبيرة
لذلك يصعب نعمل
تبريد للجهاز عنده
ما يتخوفه

* Note :- Some times, heat sink is used to dissipate the excessive heat and make the device work in safe operating Region (S.O.R)

3) The most important parameters in P.A. is conversion efficiency (η)...

$$* \eta \% = \frac{\text{Signal Load power}}{\text{DC. source power}} \times 100\% = \frac{\bar{P}_L}{\bar{P}_S} \times 100\%$$

\bar{P}_L : Ave. Ac. load power delivered to load

\bar{P}_S : Ave. Ac. power supply by the DC. source (V_{CC})

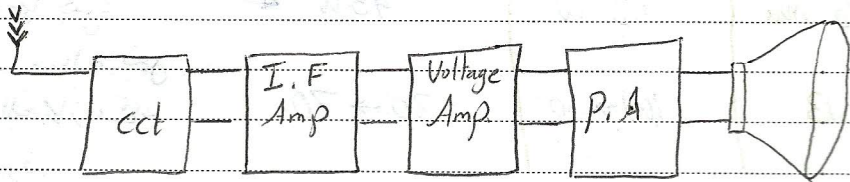
ال P.A يتسبب Power loss ال DC

ويتسبب بها ال

Ac load power (or p) ①

resistors ال و Tran. ال power dissipation ②

4) Normally, P.A is located as ~~first~~ Final stage in electronic sys. such as radio receiver...



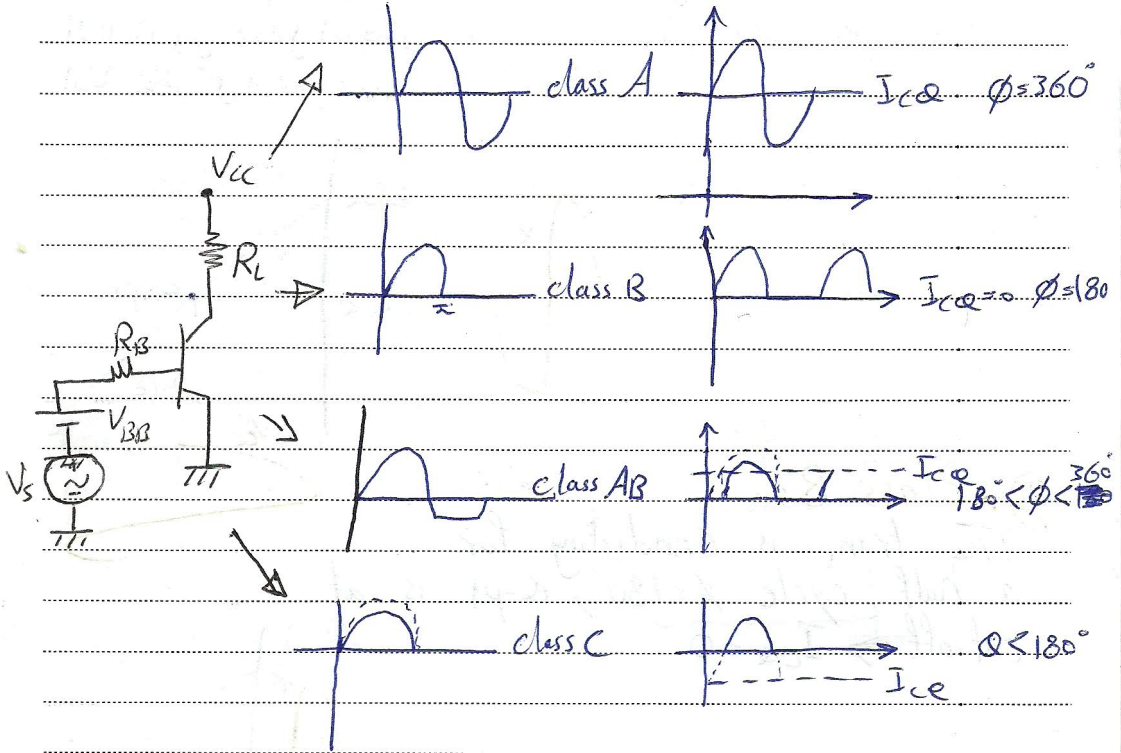
• يكون عادة الود (load) ال عليه تسبب ال كثير

* Classification of power Amp's 1- تصنيف على اساس

انه كم الفعة الزمنية ال يكون

نوع ال Tran. شغال (on) ..

بعض أنواع ال class في موقع ال Q-point

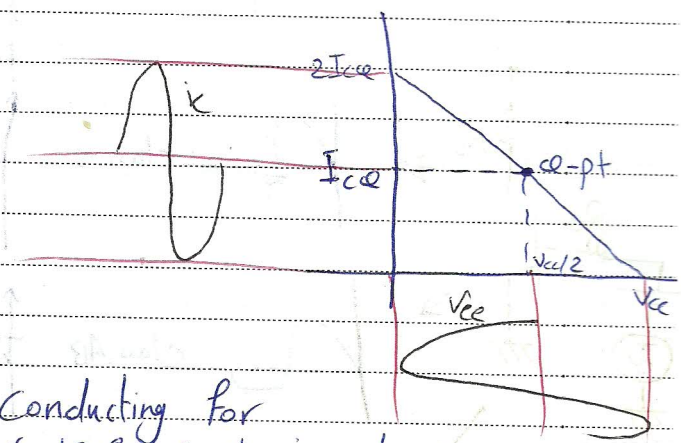


• There are four main classes according to percentage time for the conducting transistor for sinusoidal signal.

1) **Class A**:- The tran. is conducting for a full cycle i.e. the conducting angle $\phi = 360^\circ$. Ideally the Q-pt must be in the center of the D.C.LL

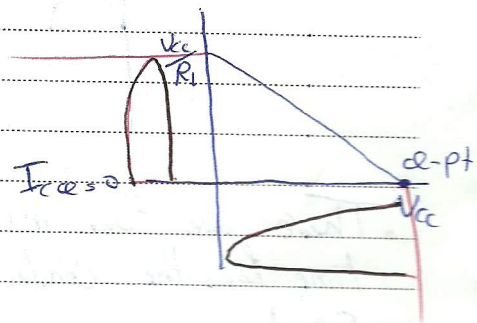
and must $i_{cp} < I_{ce}$
 class AB \Rightarrow $I_{ce} > 0$

طباً احنا بنعطي ideally
 انه ال Q-pt, I_{ce} يكون بنصف
 ال I_{ce} بس الافضل انه بنعطي
 ايضاً بنعطي كل ال signal ...



2) class B:-

The tran. is conducting for
 a half cycle $\phi = 180^\circ$, Q-pt is at
 cut-off $\Rightarrow I_{ce} = 0$



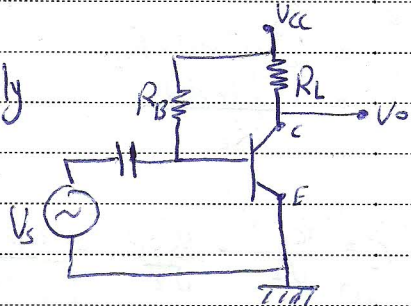
" Class A " power Amp's "

- The o/p is present for 360° i.e., the o/p will be a complete signal.
- Ideally, the Q-pt is at the center of D.C.L.L

Q-point at the center of D.C.L.L

Direct coupled load (series-fed-type):

The load is connect directly between V_{CC} and collector.



• D.C.L.L

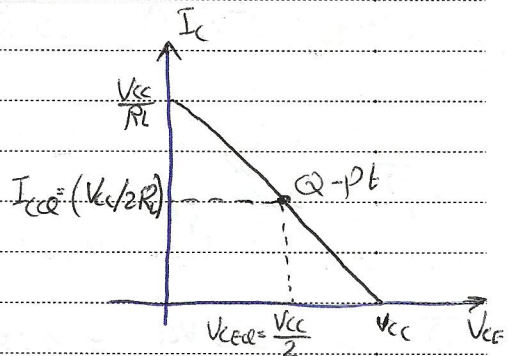
$$V_{CE} = V_{CC} - I_C R_L$$

for $V_{CE} = 0 \Rightarrow I_C = \frac{V_{CC}}{R_L}$, for $I_C = 0 \Rightarrow V_{CE} = V_{CC}$

• Ideally, when the Q-pt at the center of D.C.L.L :-

$$I_{CQ} = V_{CC} / 2R_L$$

$$V_{CEQ} = V_{CC} / 2$$



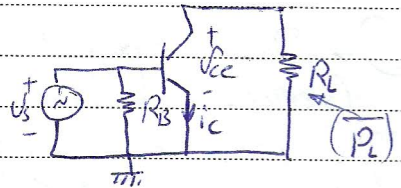
• $\eta\% = \frac{\bar{P}_L}{\bar{P}_S} \times 100\%$

* $\bar{P}_S =$ Dc. power drawn from V_{CC}

$$\bar{P}_S = I_{CQ} \cdot V_{CC}$$

* $\bar{P}_L =$ Ac load power delivered to R_L

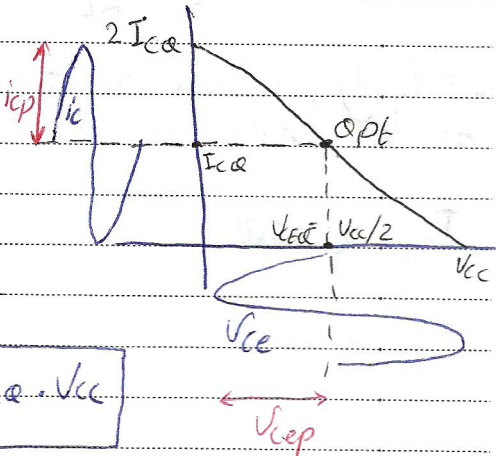
$\bar{P}_L = i_c(\text{RMS}) \cdot V_{ce}(\text{RMS})$
 $= i_c^2(\text{RMS}) \cdot R_L$
 $= \frac{V_{ce}^2(\text{RMS})}{R_L}$



$\Rightarrow \bar{P}_L = \frac{I_{cp}}{\sqrt{2}} \cdot \frac{V_{cep}}{\sqrt{2}} = \frac{I_{cp} \cdot V_{cep}}{2}$ (for sinusoidal wave)

OR $\frac{\bar{P}_L}{R_L} = \frac{(I_{cp})^2}{2} = \frac{I_{cp}^2 R_L}{2}$

OR $\frac{\bar{P}_L}{R_L} = \frac{(V_{cep})^2}{2 R_L} = \frac{V_{cep}^2}{2 R_L}$



• \bar{P}_{Lmax} ~~is~~ $I_{cp} = I_{CQ}$
 $V_{cep} = V_{ceQ} = \frac{V_{CC}}{2}$

$$\bar{P}_{Lmax} = \frac{I_{CQ} \cdot V_{CC}}{2 \times 2} = 0.25 I_{CQ} \cdot V_{CC}$$

∴ $\eta_{max} = \frac{0.25 V_{CC} \cdot I_{CQ}}{V_{CC} \cdot I_{CQ}} \times 100\% = 25\%$

∴ $\eta_{max} = 25\%$ when the Q-pt. at center of D.C.L.L.
 i.e. $I_{CQ} = \frac{V_{CC}}{2R_L}$, $V_{CEQ} = \frac{V_{CC}}{2}$

كفاءة عالية في class A direct coupled
 هي ربع ال DC من ال VCC

∴ كفاءة ال اقصى على كفاءة ال AC
 و اذا جوبنا على كفاءة ال AC من 25%

⇒ $\bar{P}_L = 0.25 \bar{P}_S$

\bar{P}_S no. 125. \bar{P}_S is Ac. load power
 power of \bar{P}_S dissipated in transistor
 power dissipated in R_L على شحنة
 و اقل من \bar{P}_S

∴ اذا ما كان في AC signal
 بعض ال اقوى و اقل من \bar{P}_S بقى
 ال $\bar{P}_{P_{tran}}$

1) For No AC signal ($V_S = 0$)

$\bar{P}_S = V_{CC} \cdot I_{CQ} = I_{CQ}^2 R_L + I_{BQ}^2 R_B + I_{CQ} V_{CEQ}$

\bar{P}_S in R_L as heat
 \bar{P}_S in R_B
 \bar{P}_S in Tran.
 but it can be neglected cause it's very small

2) When AC signal is applied, the \bar{P}_S is redistributed as :-

$\bar{P}_S = V_{CC} \cdot I_{CQ} = \bar{P}_L + I_{CQ}^2 R_L + \bar{P}_{P_{tran}} + I_{BQ}^2 R_B$

where $\bar{P}_{P_{tran}} = \bar{P}_S - \bar{P}_{RL} - \bar{P}_{RB} - \bar{P}_L$

it's very small
 so we neglect it...

• Transistor Rating :-

$$V_{CE} = V_{CC} - I_C R_C \quad (D.C. \text{ L.L.})$$

1) $V_{CE \text{ max}}$:

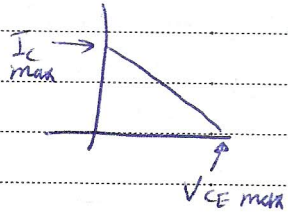
For $I_C = 0 \Rightarrow V_{CE} = V_{CC}$

ال rating يعني حساب
 الحد الأقصى لتيار و الجهد
 و الحد الأقصى P.D. يتحملها ال Trans.

taken from Dc.lil.

2) $I_{C \text{ max}}$:

For $V_{CE} = 0 \Rightarrow I_{C \text{ max}} = V_{CC} / R_C$



3) $P_{O \text{ max}}$:-

P_O in Tran. is max when there is not Ac signal

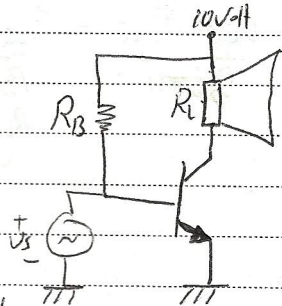
$\Rightarrow P_{O \text{ max}} = I_{CC} \cdot V_{CE \text{ max}}$

Ex. A class (A) using a BJT with $B = 25$,

$V_{BE} = 0.6$ Volt, with a speaker of 10Ω and $R_B = 0.5 \text{ k}\Omega$ as shown in the figure:

If the Ac derives a peak collector current of (0.4 A) ?

- 1) Find Q-pt position?
- 2) Calculate $\bar{P}_S, \bar{P}_L, \eta, P_{DR}, P_{D \text{ tran.}}$?
- 3) Draw Dc.lil & Ac.lil with output Voltage & current swing?
- 4) specified tran. rating?



Sol

$I_{BQ} = \frac{10 - 0.6}{0.5K} = 18.8 \text{ mA}$

$I_{CQ} = \beta I_{BQ} = (25)(18.8 \text{ mA}) = 0.47 \text{ A}$

$V_{CEQ} = V_{CC} - I_{CQ} R_L = 5.3 \text{ Volt}$

$\bar{P}_S = I_{CQ} \cdot V_{CC} = 4.7 \text{ W}$

$\bar{P}_L = \left(\frac{i_{cp}}{\sqrt{2}}\right)^2 R_L = 0.8 \text{ W} = \frac{V_{cep}^2}{R_L} = i_{cp} \cdot V_{cep}$

$\eta\% = \frac{P_L}{P_S} \times 100\% = \frac{0.8}{4.7} \times 100 = 17\%$

$P_{DRL} = I_{CQ}^2 \cdot R_L = (0.47)^2 \times 10 = 2.2 \text{ W}$

$P_{Dtran.} = \bar{P}_S - \bar{P}_L - P_{DRL} = 4.7 - 0.8 - 2.2 = 1.7 \text{ W}$

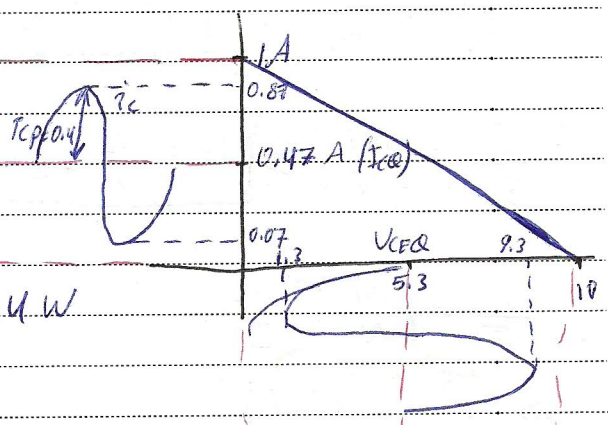
$V_{CEmax} = 10 \text{ Volt}$

$I_{Cmax} = \frac{10}{10} = 1 \text{ A}$

$P_{Dmax} = I_{CQ} \cdot V_{CEQ} = 2.4 \text{ W}$

AC power
 AC voltage
 BJT is PNP

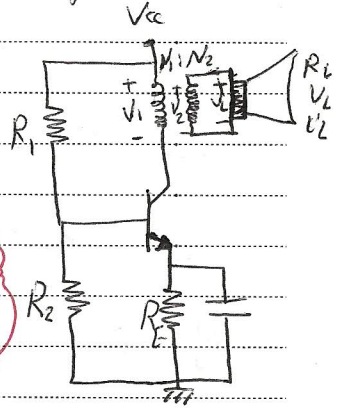
$i_{cp} = 0.4 \text{ A}$
 $V_{cep} = i_{cp} \cdot R_L = 4 \text{ Volt}$



Q-point is at $V_{CEQ} = 5.3 \text{ V}$
 $I_{CQ} = 0.47 \text{ A}$
 DC power is 4.7 W
 AC power is 0.8 W
 Efficiency is 17%

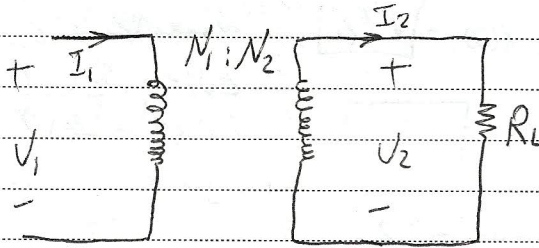
"Class (A) Transformer coupled Amp"

* Compared to direct coupled:
 For the same \bar{P}_L , the transformer coupled requires less \bar{P}_S (No power dissipated as $I_{CQ}^2 \cdot R_L$)
 and since $\frac{\bar{P}_L}{\bar{P}_S} = \eta \uparrow$ so $\eta_{transform} > \eta_{direct}$



secondarily load

• For Ideal transformer :-



• Power loss in transformer is negligible
 • حرارة R_L بجز R_L سے باقی تمام P_S R_L پہنچتی ہے
 • $I_{CQ}^2 R_L$ سے P_S بچتی ہے

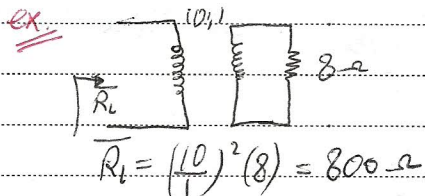
$$\frac{V_1}{V_2} = \frac{N_1}{N_2} \Rightarrow \boxed{V_1 = \frac{N_1}{N_2} V_2}$$

$$\frac{I_1}{I_2} = \frac{N_2}{N_1} \Rightarrow \boxed{I_1 = \frac{N_2}{N_1} I_2}$$

$$\frac{V_1}{I_1} = \left(\frac{N_1}{N_2}\right)^2 \frac{V_2}{I_2}$$

$$\Rightarrow \boxed{R_L = a^2 R_L}$$

As reflected impedance $\frac{N_1}{N_2}$ is seen from primary side



$$R_L = \left(\frac{10}{1}\right)^2 (8) = 800 \Omega$$

D → DC analysis:-

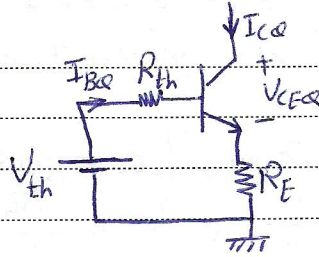
• $R_{th} = R_1 // R_2$

• $V_{th} = \frac{V_{cc} R_2}{R_1 + R_2}$

• $I_{BQ} = \frac{V_{th} - V_{BE}}{R_{th} + (\beta + 1)R_E}$

• $I_{CQ} = \beta I_{BQ}$

• $V_{CEQ} = V_{cc} - I_{CQ} r_{dc} - I_E R_E$
 ↙ resistance for the inductor (primary coil)



For a very small R_E & negligible r_{dc}

$V_{CEQ} = V_{cc}$

• DC L.L

$V_{CE} = V_{cc} - I_C r_{dc} - I_E R_E$

For $V_{CE} = 0 \Rightarrow I_C = \frac{V_{cc}}{r_{dc} + R_E} \approx \infty$ (For negligible r_{dc} & R_E) (0, ∞)

For $I_C = 0 \Rightarrow V_{CE} = V_{cc}$ ($V_{cc}, 0$)

For output si de jesi nime o

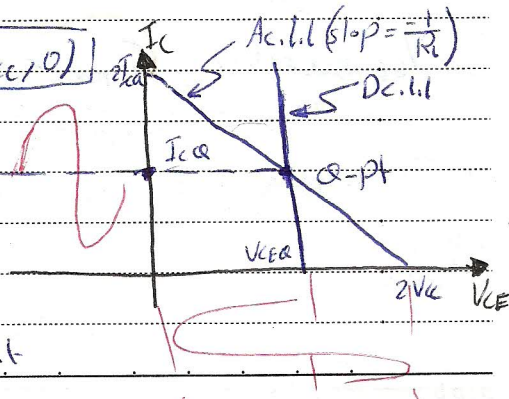
2Vcc Ac.lil il qor il qor si
 2Vcc lid si jesi jesi

me qor coil il air output il

Vcc kis qor Vcc nijiz storage element

nipb

--- 2Vcc jani source il ni



• Dc and Ac intersect at Q-point.

⇒ at Q-point, $I_{CQ} = \frac{V_{CEQ}}{R_L} = \frac{V_{CC}}{R_L}$

• $I_{CQ} = \frac{V_{CC}}{R_L}$, $V_{CEQ} = V_{CC}$, $R_L = \frac{V_{CC}}{I_{CQ}}$

• η max :-

$\eta = \frac{\bar{P}_L}{\bar{P}_S} \times 100$ سکون سے پیدا ہونے والا primary اور secondary کی طاقت

$\bar{P}_S = V_{CC} \cdot I_{CQ}$, $\bar{P}_L = \text{from primary} = \frac{V_{CP}}{\sqrt{2}} \cdot \frac{I_{CP}}{\sqrt{2}}$

⇒ $\bar{P}_{Lmax} = \frac{V_{CC}}{\sqrt{2}} \cdot \frac{I_{CQ}}{\sqrt{2}} = \frac{I_{CQ} \cdot V_{CC}}{2}$

⇒ $\eta_{max} = \frac{\bar{P}_{Lmax}}{\bar{P}_S} = \frac{I_{CQ} \cdot V_{CC}}{2 I_{CQ} \cdot V_{CC}} \times 100 = 50\%$

• Tran. rating :

ان سوچنا ہے کہ یہ کب کب کی بات ہے

$V_{CEmax} = 2V_{CC}$, $I_{Cmax} = 2I_{CQ}$, $P_{Dmax} = V_{CC} \cdot I_{CQ}$

• $V_{CE} > 0.8 V_{CC}$ اور $I_C > 0.5 I_{CQ}$

• $\eta > 20\%$

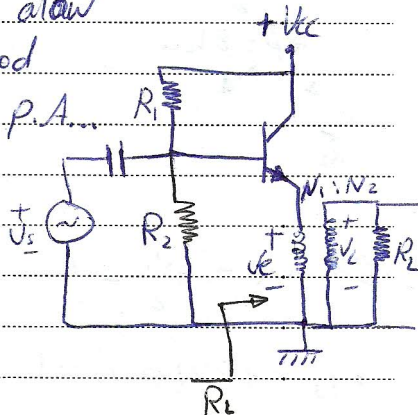
• $\eta > 50\%$ اور $\eta > 50\%$

• $\eta > 50\%$ اور $\eta > 50\%$
 • peak collector voltage = V_{CC}

Transformer-coupled Emitter follower class A P. Amp^s

• Since Emitter follower (c.c.) has a low output resistance so it is very good c.c.t. to be used as an o/p stage P.A.

• Given V_{CC} , β , V_{BE} , T_o Design acct for a certain specification.



Ex. Design a class A transformer

Coupled E.F to deliver 4 Watt to 8Ω load.

Use a BJT with $\beta = 50$, $V_{BE} = 0.6V$, the available $V_{CC} = 25V$, the peak emitter current i_{ep} Not more than $0.8 I_{CQ}$ ($i_{ep} = 0.8 I_{CQ}$) & peak emitter Voltage $V_{ep} = 0.8 V_{CC}$.

1) Draw the cct diagram.

2) Calculate the turn ratio $a = \frac{N_1}{N_2}$, \bar{P}_s , η % ?

3) Specified the required tran. rating? (I_{Cmax} , V_{CEmax} , P_{Dmax})

4) Draw Dc & Ac load line with emitter Voltage & current Swing?

we will use this

$$a = \frac{N_1}{N_2} = \frac{V_c}{V_e} = \frac{I_L}{i_e} = \frac{\sqrt{R_L}}{R_L}$$

$$V_{ep} = 0.8 V_{CC} = (0.8)(25) = 20V$$

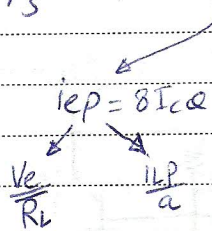
$$\bar{P}_s = \frac{V_{ep}^2}{2R_L} \Rightarrow V_{ep} = \sqrt{R_L \bar{P}_s \cdot 2}$$

$$= \sqrt{(8)(4)(2)}$$

$$= 8V$$

$$\Rightarrow a = \frac{V_{ep}}{V_c} = \frac{20}{8} = \frac{2.5}{1} = 2.5:1$$

• $\bar{P}_S = V_{CC} \cdot I_{CQ}$, $I_{CQ} = \frac{i_{eP}}{0.8}$, $\frac{i_{eP}}{I_{LP}} = \frac{N_2}{N_1} = \frac{1}{a}$



$\Rightarrow i_{eP} = \frac{I_{LP}}{a}$

• $I_{LP} = \frac{V_{LP}}{R_L} = \frac{8}{8} = 1A$

$\Rightarrow i_{eP} = \frac{1}{2.5} = 0.4A$

$\Rightarrow I_{CQ} = \frac{0.4}{0.8} = \frac{1}{2} = 0.5A$

• $\bar{P}_S = (25)(0.5) = 12.5 \text{ Watt}$

• $\eta = \frac{P_L}{P_S} \times 100\% = \frac{4}{12.5} \times 100 = 32\%$

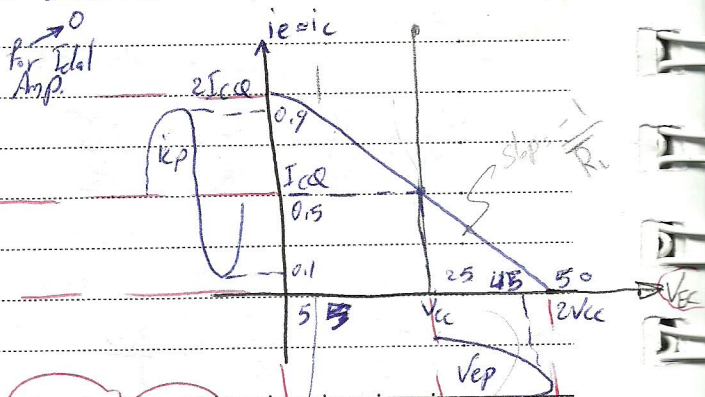
• $V_{CEmax} = 2V_{CC} = 50 \text{ V}$, $I_{Cmax} = 2I_{CQ} = 1A$

• $P_{Dmax} = \bar{P}_S = V_{CC} \cdot I_{CQ} = 12.5 \text{ Watt}$

• $V_{CC} - V_{CE} - I_F R_{dc} = 0$

For $I_F = I_C$, $I_C = 0 \Rightarrow V_{CE} = V_{CC}$

$V_{CE} = 0 \Rightarrow i_C = \frac{V_{CC}}{R_{dc}} = \frac{V_{CC}}{5} = 20$



$$R_i = a^2 R_L = (2.5)^2 (8) = 50 \Omega$$

• if $R_{th} = 2K\Omega$ find R_1 & R_2 :

$$V_{th} = \frac{V_{cc} R_2 R_1}{R_1 + R_2 R_1} \Rightarrow \boxed{V_{th} = \frac{V_{cc} R_{th}}{R_1}}$$

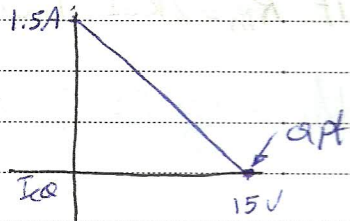
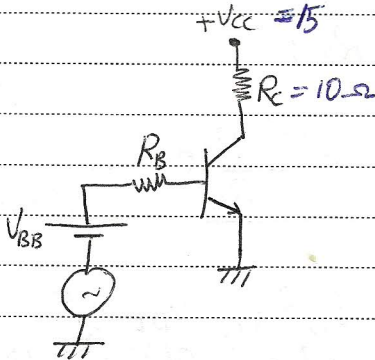
$$R_{th} = \frac{R_1 R_2}{R_1 + R_2}, \quad V_{th} - I_B R_{th} - V_{BE} = 0$$
$$V_{th} = (0.7) + (0.01)(2) = 0.72$$

$$R_1 = \frac{V_{cc} R_{th}}{V_{th}} =$$

$$R_2 = \frac{R_1 R_{th}}{R_1 - R_{th}} =$$

~~~~~ \* ~~~~~

# "Class (B) power Amp's"

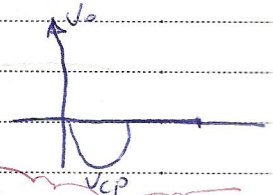
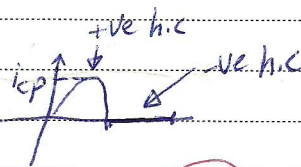
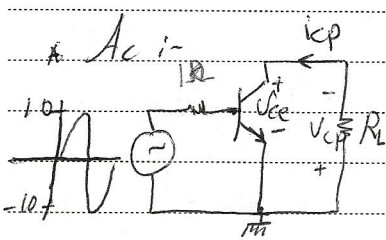


Q-Point is at cutoff region (B)   
 ق-نقطه در منطقه قطع

$$I_B = \frac{V_{BB} - V_{BE}}{R_B}$$

When  $V_{BB} = V_{BE} \Rightarrow I_B = 0 \Rightarrow I_C = 0, V_{CE} = V_{CC}$

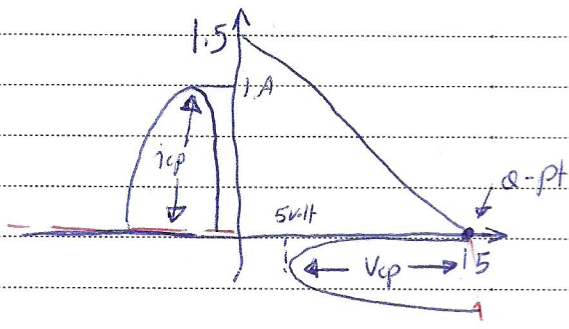
$\Rightarrow$  The Q-pt is cutoff...



half wave rectification   
 نیمی موج مستقیم کننده

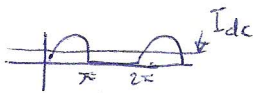
$V_{CP} = 10 \text{ Volt.}$

$i_{CP} = \frac{V_{CP}}{R_L} = 1 \text{ A}$





Subject .....



$$\bullet \bar{P}_s = V_{cc} \cdot I_{dc}$$

$I_{dc}$  is half wave  $\Rightarrow$  ~~not~~

$$I_{dc} = \frac{i_{cp}}{\pi} = \text{Dc. Value} = \text{avg. Value}$$

$$\bullet \bar{P}_L = i_c(\text{rms}) \cdot v_{cp}(\text{rms})$$

$$= \frac{i_{cp}}{2} \cdot \frac{v_{cp}}{2} = \frac{i_{cp} \cdot v_{cp}}{4}$$

$$I_{c(\text{rms})} = \frac{i_{cp}}{\sqrt{2}} \text{ full wave}$$

But

$$i_c(\text{rms}) = \frac{i_{cp}}{2} \text{ half wave}$$

$$\Rightarrow \eta\% = \frac{\bar{P}_L}{\bar{P}_s} \times 100\%$$

partially, class B single stage is not used, So ~~two~~ two transistors are used in push-pull arrangement to process the whole input signal.

These trans can be:

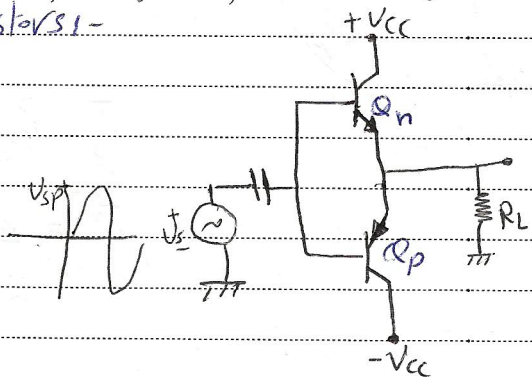
- 1) Complementary (NPN with PNP) (p channel with N channel)
- 2) The same type but it is required to use a phase splitting ckt.

\* Complementary class-B push-pull power Amp. :-  
 • assuming Ideal transistors :-

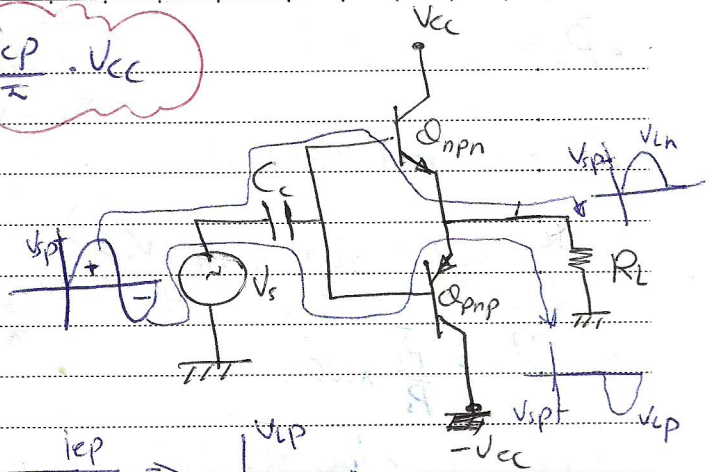
• in +ve h.c.

$$\bullet V_{Ln} = v_{sp} \quad (V_{BE} = 0)$$

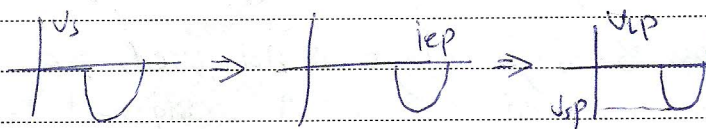
$$\bullet i_{cn} = \frac{V_{Ln}}{R_L} = \frac{v_{sp}}{R_L}$$



$$\bar{P}_{S\oplus} = I_{dc} \cdot V_{cc} = \frac{i_{cp}}{\pi} \cdot V_{cc}$$

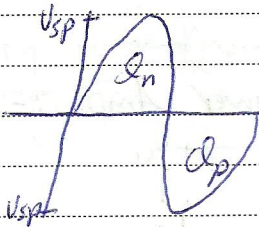


• in -ve h.c. :-



$$P_{S\ominus} = \frac{-i_{ep}}{\pi} \cdot -V_{cc} = \frac{i_{ep}}{\pi} V_{cc}$$

\* For a whole input cycle :-



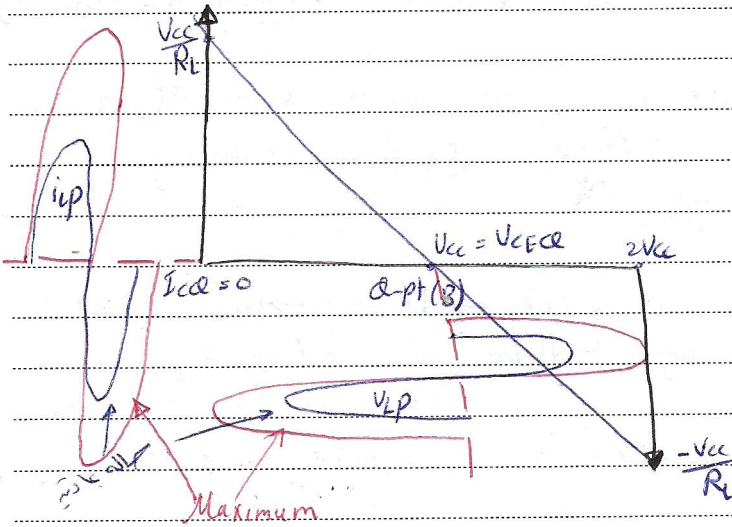
$$\bar{P}_L = \frac{V_L^2 (rms)}{R_L} = \frac{(V_{ip}/\sqrt{2})^2}{R_L}$$

$$\bar{P}_L = \frac{V_{ip}^2}{2 R_L}$$

$$\bar{P}_S = \bar{P}_{S\oplus} + \bar{P}_{S\ominus}$$

$$\bar{P}_S = \frac{2 i_{cp} \cdot V_{cc}}{\pi}$$





$$\eta\% = \frac{\bar{P}_L}{\bar{P}_S} \times 100\% \rightarrow \frac{V_L^2}{R_L}, I_L^2 R_L, V_L \cdot I_L$$

$$\bar{P}_L = \frac{V_{L(rms)}^2}{R_L} = \frac{V_{LP}^2}{2R_L}$$

$$\bar{P}_S = \bar{P}_{S0} + \bar{P}_{S\infty}$$

$$= \frac{i_{LP}}{\pi} \cdot V_{CC} + \frac{-i_{LP}}{\pi} \cdot -V_{CC}$$

$$\boxed{\bar{P}_S = \frac{2V_{LP} V_{CC}}{\pi R_L}}$$

\* For max  $\eta_{max}$ ,  $V_L$  must be equal  $V_{CC}$

پہلے  $\bar{P}_L$  سے  $\eta_{max}$  کی طرف سے  $V_{CC} = V_{Lp}$  کی صورت میں  $V_{Lp}$  کی صورت میں

$$\bar{P}_{Lmax} = \frac{V_{CC}^2}{2R_L}$$

$$\bar{P}_S = \frac{2V_{CC}^2}{\pi R_L}$$

$$\eta_{max} = \frac{\bar{P}_{Lmax}}{\bar{P}_{Smax}} = \frac{V_{CC}}{2R_L} \times \frac{\pi R_L}{2V_{CC}} = \frac{\pi}{4} \times 100 = 78.5\%$$

$$P_D \text{ (each tran)} = \frac{\bar{P}_S - \bar{P}_L}{2}$$

\* Notes:-

1) The cct. is (C.C) (E.F)  $\Rightarrow A_v = 1 = \frac{V_L}{V_i}$

$$\Rightarrow V_L = V_i \text{ (for } V_{BE} = 0)$$

$$P_L \text{ (max)} \Rightarrow R_L \text{ (max)} \Rightarrow V_L = V_i \leftarrow 10 = V_i$$

$$V_L = V_i \leftarrow V_L \leftarrow R_L \& R_L \text{ (max)}$$

2) For max  $\bar{P}_L$ ,  $V_{ip} = V_{CC}$  with measure  $V_{peak} = V_{CC}$

Ex. For the cct shown,  $V_{CC} = \pm 6V$ ,  $R_L = 4\Omega$ ,  $V_S = 5\sin\omega tV$ ,

1) calculate  $\bar{P}_L$ ,  $\bar{P}_S$ ,  $\eta$ ,  $P_{D \text{ (each tran)}}$ ?

2) sketch, Ac & Dc. w.  $V_i$ , i.e. swings?

3) what must be the peak ip voltage for max  $\eta$ ?



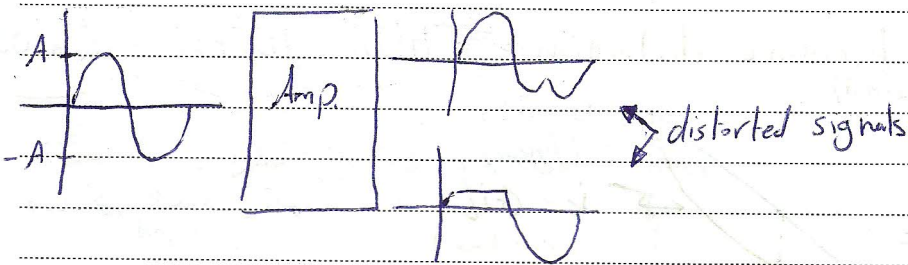
\* Note  $\bar{P}_S$  (class B) <  $\bar{P}_S$  (class A) [for the same  $P_L$ ]

## "Distortion in power Amp's"

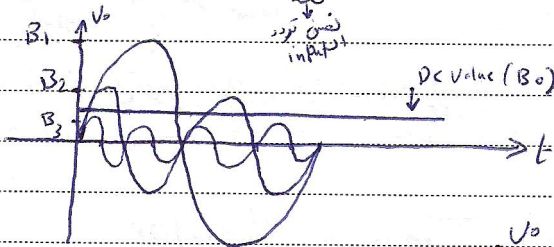
• Deformation in the shape of o/p signal.

1) Non linear distortion: -

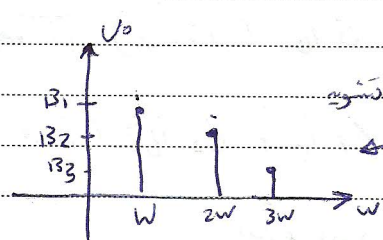
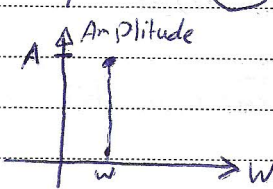
• Due to the non linear device c/c when it's driven by a large signal.



$$V_o(t) = B_0 + B_1 \sin \omega t + B_2 \sin 2\omega t + B_3 \sin 3\omega t \dots$$



Handwritten note in a cloud:   
 1. DC value (B<sub>0</sub>)  
 2. Fundamental (B<sub>1</sub>)  
 3. Higher order harmonics (B<sub>2</sub>, B<sub>3</sub>)



Handwritten note:   
 1. DC value (B<sub>0</sub>)  
 2. Fundamental (B<sub>1</sub>)  
 3. Higher order harmonics (B<sub>2</sub>, B<sub>3</sub>)

n/pb (spectrum of  $V_i$ )

Amplitude versus Frequency (spectrum of  $V_o$ )





Now let  $i_b = I_{bm} \cos \omega t$

1) For linear operations  $\Rightarrow i_c = (i_b \cos \omega t) G_1 = B_1 \cos \omega t$

2) For non linear,

$$i_c = G_1 I_{bm} \cos \omega t + G_2 I_{bm}^2 \cos^2 \omega t$$

$$= B_1 \cos \omega t + G_2 I_{bm}^2 \frac{1}{2} (1 + \cos 2\omega t)$$

$$= B_1 \cos \omega t + \underbrace{\frac{G_2 I_{bm}^2}{2}}_{B_0 \text{ (D.C.)}} + \underbrace{\frac{G_2 I_{bm}^2}{2}}_{B_2 = B_0} \cos 2\omega t$$

$$\Rightarrow i_c = B_0 + B_1 \cos \omega t + B_2 \cos 2\omega t$$

↓  
Dc

↓  
1<sup>st</sup> harmonic

↓  
2<sup>nd</sup> harmonic

Ex. For a certain P.A., the o/p current is given by  
 $i_c = 2 + 5 \sin \omega t + 4 \sin 2\omega t + 3 \sin 3\omega t$  (A),  $R_L = 10 \Omega$

1) Find  $D_2$  %,  $D_3$  %, T.H.D. %

2) Find  $\bar{P}$

$$B_0 = 2, B_1 = 5, B_2 = 4, B_3 = 3$$

$$D_2 = \frac{B_2}{B_1} \times 100 \% = \frac{4}{5} \times 100 = 80 \%$$

$$B.D_3 = \frac{B_3}{B_1} \times 100 = \frac{3}{5} \times 100 = 60\%$$

$$T.H.D\% = \sqrt{D_2^2 + D_3^2} \times 100\% = 100\%$$

$$2) P_n = I^2 R = \left(\frac{I_m}{\sqrt{2}}\right)^2 \cdot R = \frac{B_n^2}{2} \times R_L$$

$$\Rightarrow \bar{P} = P_1 + P_2 + P_3$$

power of Fundamental  
" " 2<sup>nd</sup>  
" " 3<sup>rd</sup>

$$\bar{P}_L = \frac{B_1^2}{2} R_L + \frac{B_2^2}{2} R_L + \frac{B_3^2}{2} R_L$$

$$= \left(\frac{25}{2} + \frac{16}{2} + \frac{9}{2}\right)(10) = \boxed{250 \text{ W}}$$

$$\text{OR } P = \frac{B_1^2}{2} R_L + \frac{B_2^2}{2} R_L + \frac{B_3^2}{2} R_L$$

$$= \frac{B_1^2}{2} R_L \left(1 + \frac{B_2^2}{B_1^2} + \frac{B_3^2}{B_1^2}\right)$$

$$= P_1 (1 + T.H.D) = \frac{25}{2} \times 10 (1 + 1)$$

$$= \boxed{250 \text{ W}}$$

لو كان صفا  
T.H.D 0%

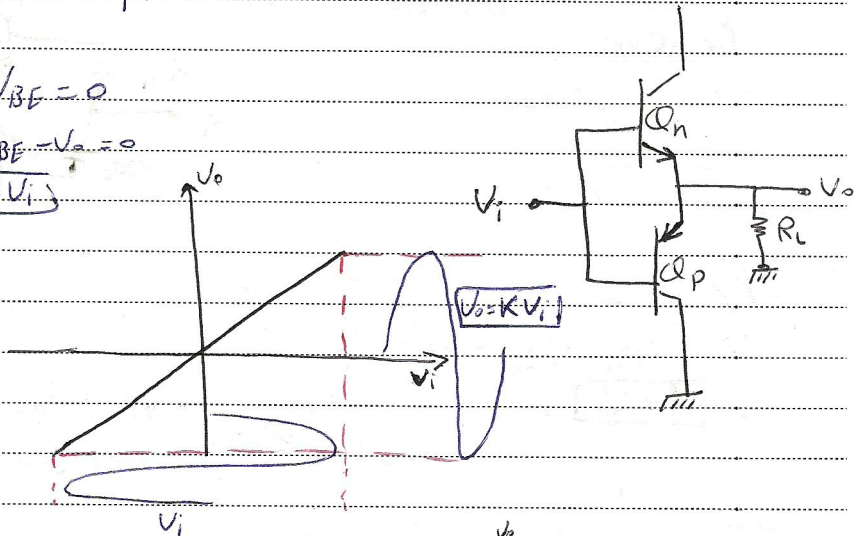
2) Cross over distortion :-

occur only on class B, but non linear occur in any power amp.

Ⓐ For  $V_{BE} = 0$

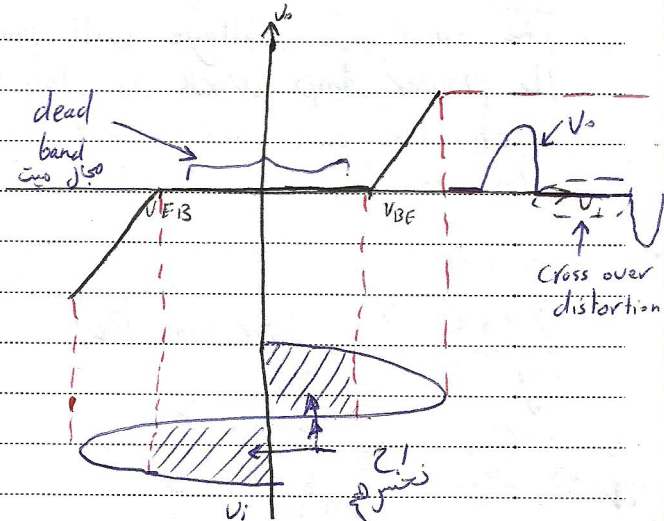
$$V_i - V_{BE} - V_o = 0$$

$$\Rightarrow V_o = V_i$$



Ⓑ For  $V_{BE} \neq 0$

A distortion happen in class B only because the Q-pt is at the origin.



It's due to the finite value of  $V_{be}$  which is inherent in BJT.

• وجود  $V_{BE}$  في كل الترانزستوريات

• مثالي في class A ال Q-pt يتكون من قبة. في وجود  $V_{BE}$  القليل لا يؤثر أي شيء في class B

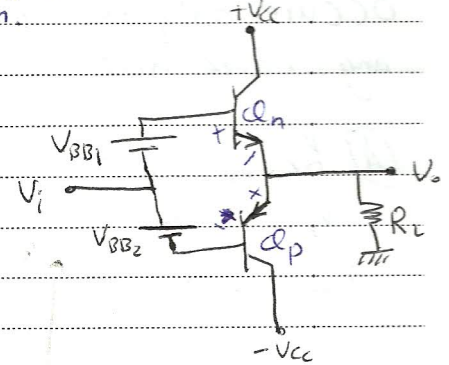
• It can be eliminated by applying a small Dc Voltage equal & opposite to  $V_{be}$  as shown.

• For  $Q_n$ :

$$-V_i - V_{BB1} + V_{be} + V_o = 0$$

$$\Rightarrow V_o = V_i$$

∴ No C.R.D.



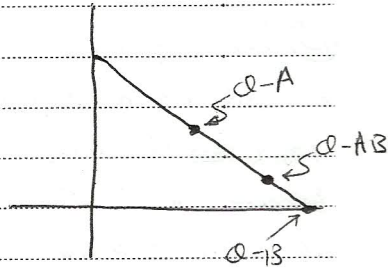
• For  $Q_p$  :-

$$V_i - V_{BB2} + V_{EB} - V_o = 0$$

$$\Rightarrow V_i = V_o$$

• هذا ما يميز  $V_{BB}$  مع  $I_B$  و  $I_C$  و  $I_E$  و  $I_{pt}$  و  $I_{شوية}$  لغوة.

• The small Dc Voltage will make the power Amp. work as class (AB) which has a conversion eff. very close to class B.



$$\eta_{AB} < \eta_B \text{ (For same } R_L)$$

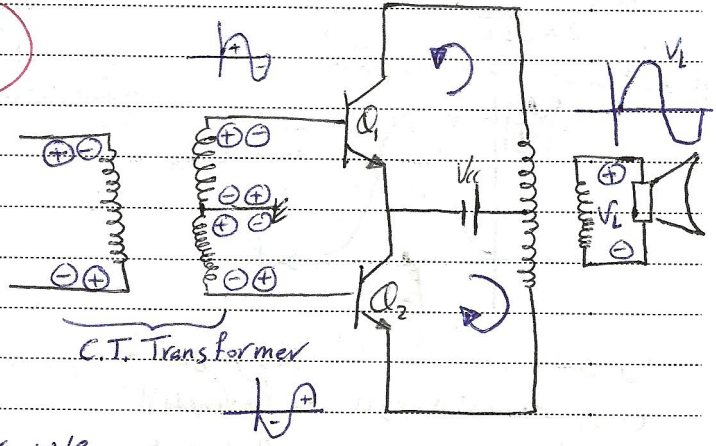
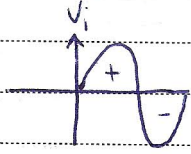
• بعد class B في class AB. distortion.

$\bar{P}_s$  لا تسحب  $\bar{P}_s$  لا تسحب  
 $\eta < \bar{P}_s$  لا تسحب  $\eta < \bar{P}_s$  لا تسحب  
 لا تسحب  $\bar{P}_s$  لا تسحب signal

"Class B Using Same type of Tran."

By Using "Transformer coupled class B push-pull P.A"

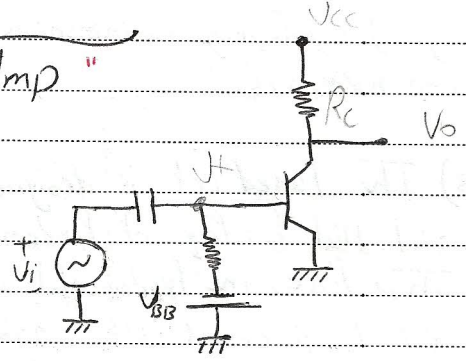
$\eta_{max} = 78.5\%$



- $Q_1$  will process +ve H.c of  $V_i$ .
- $Q_2$  will process -ve H.c of  $V_i$ .

"Class-C power Amp"

The BJT will be on for a small conduction angle  $\phi_c < 180^\circ$  and only when  $V_i > V_{BE} + V_{BB}$



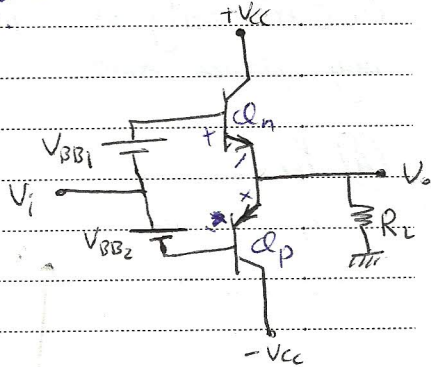
• It can be eliminated by applying a small Dc. Voltage equal & opposit to  $V_{be}$  as shown.

• For  $Q_n$ :

$$-V_i - V_{BB1} + V_{be} + V_o = 0$$

$$\Rightarrow V_o = V_i$$

∴ no C.R.D.



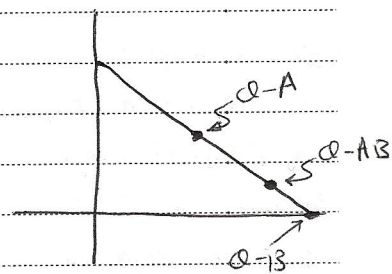
• For  $Q_p$  :-

$$V_i - V_{BB2} + V_{EB} - V_o = 0$$

$$\Rightarrow V_i = V_o$$

• هذا ما يخلق  $V_{BB}$  مع  $I_B$  متساوية  
 وخرج  $I_C$  وخرج  $I_E$  متساوية لغوة

• The small Dc. Voltage will make the power Amp. work as class (AB) Wich has a conversion eff. very close to class B.



$$\eta_{AB} < \eta_B \quad (\text{For same } R_L)$$

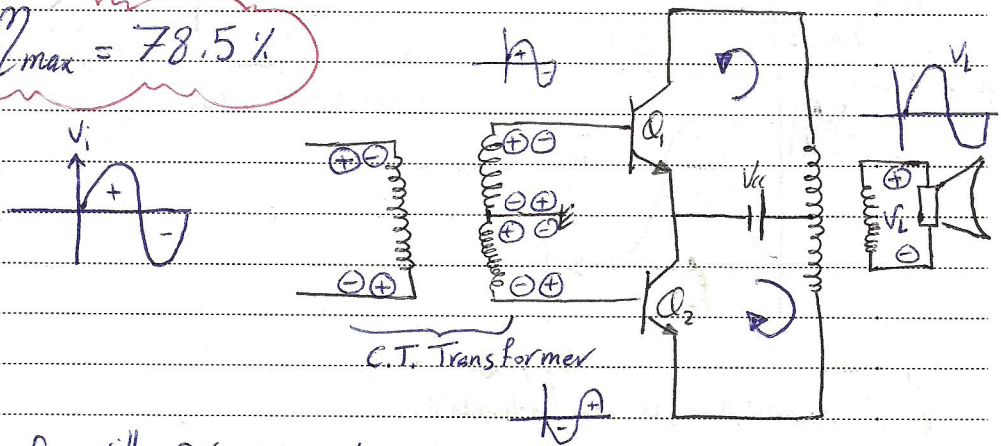
• يعني class AB فيه distortion  
 class B فيه distortion

$\bar{P}_s$  لا تسحب  
 $\eta_{AB} < \eta_B$  يعني  
 $\bar{P}_s$  لا تسحب  
 signal لا تسحب

"Class B Using Same type of Tran."

By Using "Transformer coupled class B push pull P.A"

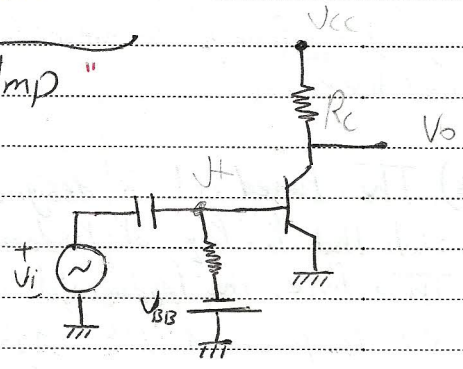
$\eta_{max} = 78.5\%$



- $Q_1$  will process +ve H.c of  $V_i$ .
- $Q_2$  will process -ve H.c of  $V_i$ .

"Class C power Amp"

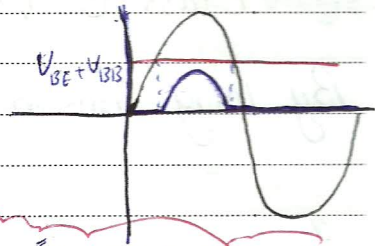
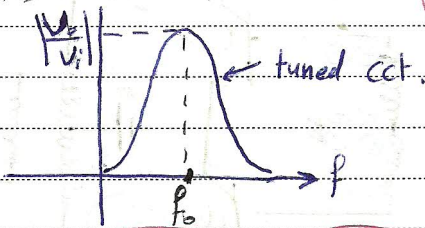
- The BJT will be on for a small conduction angle  $\phi_c < 180^\circ$  and only when  $V_i > V_{BE} + V_{BB}$



1) normally, class c is used in Radio freq. Amp's. where the load is parallel tuned cct. with a resonant freq.

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

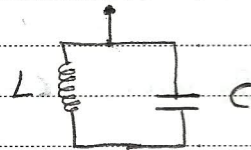
بطل  
انظر شكله على امثلة كتاب الـ P.T  
- في تردد  $f_0$



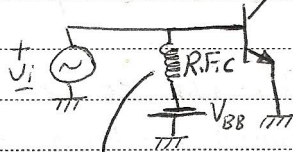
• لهاي موجة مشوية وعلاياً بيستة موجة  
• R.F. وليس بالـ Radio Freq. وكتايشها و power  
• كريان

• بنقل design بحيث  $f_0$  لـ  $f_0$  في تردد  
• الـ Fundamental تحت الموجة المشوية يعني  
• Pund. كبر الـ harmonik

2) The o/p of class (C) is very distorted signal (Less than half cycle) containing fundamentals and harmonics.



3) The tuned cct. is designed such that  $f_0 =$  freq. of fundamental. There fore, the fundamental component will be processed with a high power and high conversion eff. (%)

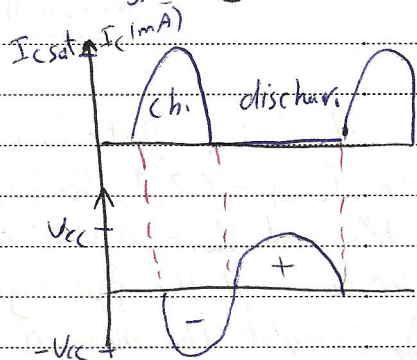
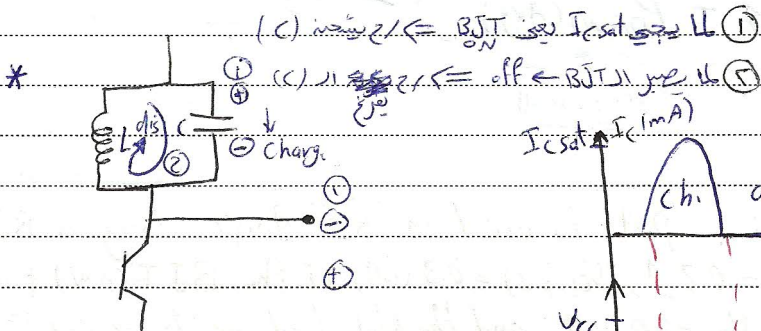
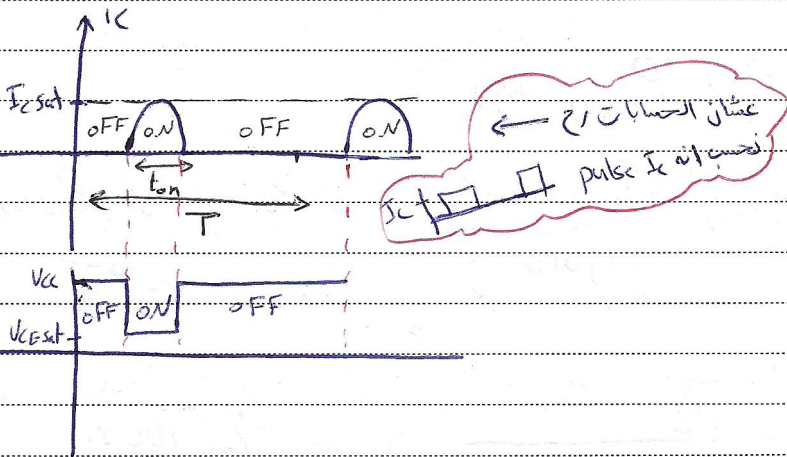


Radio freq. check  
⇒ short for Dc  
⇒ open for Ac



4) The BJT will ~~be~~ be on for a very short time ( $t_{on}$ ).

5) The ( $i_c$ ) waveform will be similar to a small pulse of magnitude  $\approx |i_{c,sat}|$  and  $V_{CE} = V_{CE,sat}$



6) The energy will be transferable bet. C&L resulting in a sinusoidal o/p Voltage of freq. = freq. of fundamental.

$$P_{Lmax} = \left(\frac{V_{CC}}{\sqrt{2}}\right)^2 / R_L = \frac{V_{CC}^2}{2R_L}$$

$$P_s = P_L + P_{D(on)}(Avg)$$

$$P_{D(on)} = I_{C(sat)} \cdot V_{CE(sat)} \Rightarrow P_{D(on)}(Avg) = P_{D(on)} \frac{t_{on}}{T}$$

التي في حالة التجهة
التي في حالة التجهة

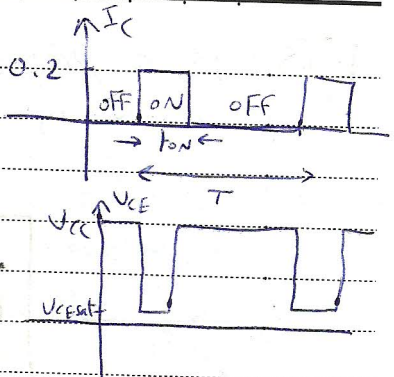
$$\Rightarrow \eta_c = \frac{P_L}{P_L + P_{D(on)}(Avg)} \Rightarrow \eta_c = 100\%$$

↑  
very small

Ex. A class C pA is used in R.F. Amp. Using a BJT with  $I_{C(sat)} = 0.2A$ ,  $V_{CE(sat)} = 0.3$  Volt, if the BJT(on) time is  $1\mu s$  and  $V_{CC} = 20$  Volt, and the total Load are tuned cct is  $100\Omega$ , and the input signal has a freq. of 100 KHz

- 1) Calculate the max. eff.
- 2) Design the tuned cct. to process the fundamental components?

$$\eta \% = \frac{\bar{P}_{Lmax}}{\bar{P}_{Lmax} + P_{D(ON)AVG}}$$



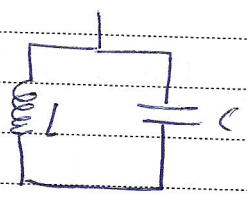
$$T = \frac{1}{f} = \frac{1}{100 \times 10^3} = 10 \mu s$$

$$P_{D(ON)} = V_{CEsat} \cdot I_{Csat} = 0.06 \text{ W}$$

$$P_{D(AVG)} = P_{D(ON)} \frac{t_{ON}}{T} = (0.06) \left( \frac{1}{10} \right) = 0.006 \text{ W}$$

$$P_L = \frac{V_C P^2}{2 R_L} \Rightarrow P_{Lmax} = \frac{V_{CC}^2}{2 R_L} = \frac{400}{(2)(100)} = 2 \text{ watt}$$

$$\eta \% = \frac{2}{2 + 0.006} \times 100 = 99 \%$$



$$f_0 = \frac{1}{2\pi\sqrt{LC}}, \quad LC = \frac{1}{4\pi^2 f_0^2}$$

$$\Rightarrow LC = \frac{1}{(4)(10)(4 \times 10^{10})} = 2.5 \times 10^{-12}$$

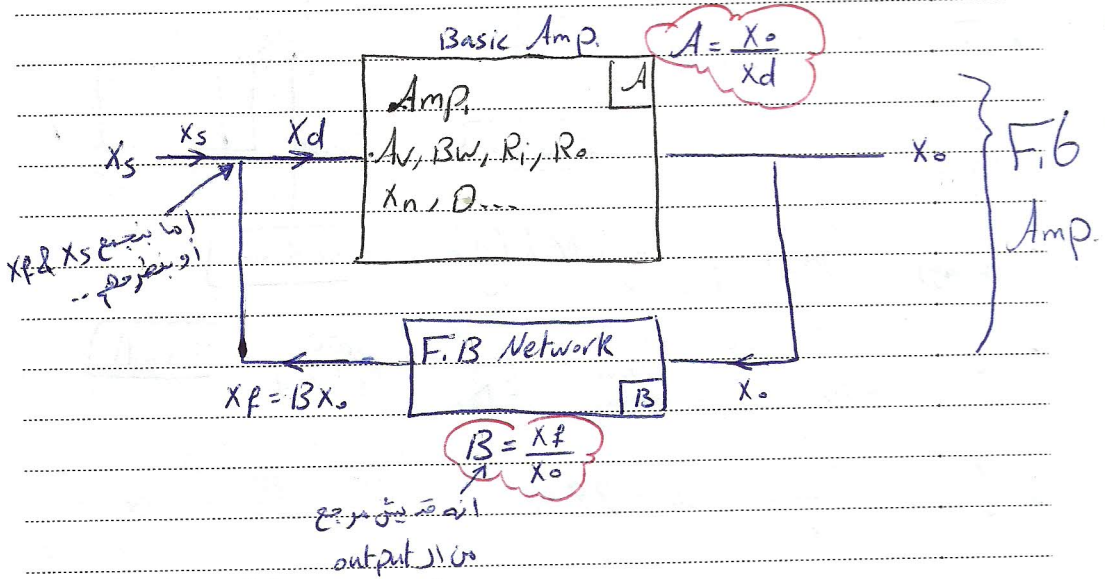
$$\text{Let } C = 1 \text{ nF} \Rightarrow L = 0.633 \text{ mH}$$

# Ch 12: "Feedback and Stability"

Subject .....

1 1

FB: is a process of returning back a portion of o/p to the input, to modify Amp. parameters.



\* For the fib sys. shown:-

•  $A$  → Transfere gain (Voltage or current) of the basic Amp.

•  $A = \frac{X_o}{X_d}$  ← output signal

• difference signal (Error signal),  $X_d = X_s - X_p$

•  $X_s$ : external source signal

•  $X_p$ : feed back signal,  $X_p = B X_o$

•  $B$ : F.B. Factor (ratio) for feed back Net.  $1 > B > 0$

+ve F.B. ← plus sign

-ve F.B. ← minus sign

\* Types of F.B :-

① +ve f.b: when  $x_f$  aids (added) to  $x_s$ , then  $x_d = x_s + x_f$  and this is called +ve f.b.

This type of F.B is used in oscillator (signal generator)

② -ve f.b: when  $x_f$  opposes  $x_s$  resulting in  $x_d = x_s - x_f$ , used to modify Amp. parameters.

\* Negative Feedback :-

This f.b happen when  $x_f$  opposes  $x_s$  resulting in

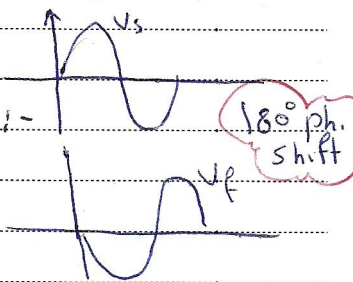
$x_d = x_s - x_f$

- Types of -ve F.B (Topology) (Connection) :-

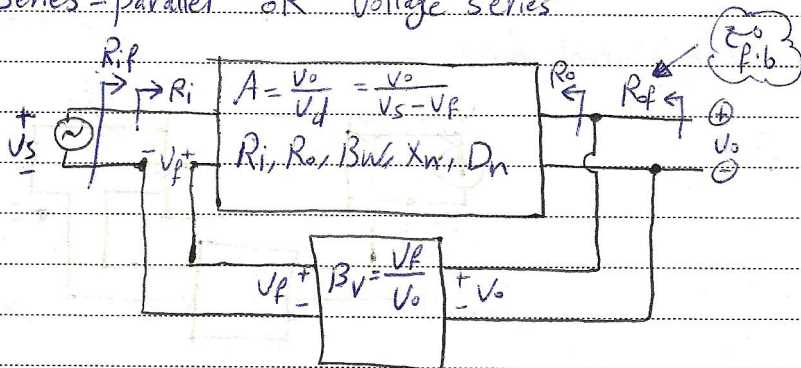
• Since  $x_s$  &  $x_o$  can be Voltages ( $V_s, V_o$ ) or currents ( $I_s, I_o$ ), there are 4

Possibilities of connection

i.e four Types of -ve f.b.



1) When  $x_s = V_s$ ,  $x_o = V_o$ , this topology is called "series-parallel" or "Voltage series"



Without FB:  $V_d = V_s$

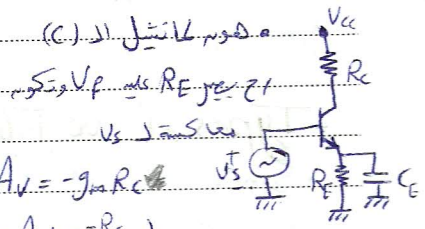
With F.B.:-

$$-V_s + V_s + V_f = 0 \Rightarrow V_d = V_s - V_f$$

i.e  $V_f$  oppose  $V_s$ ,  $V_f = \beta V_o$

$$\frac{V_o}{V_s} = A_{vf} \text{ gain of F.B. Amp.}$$

ex. of -ve f.b.:-

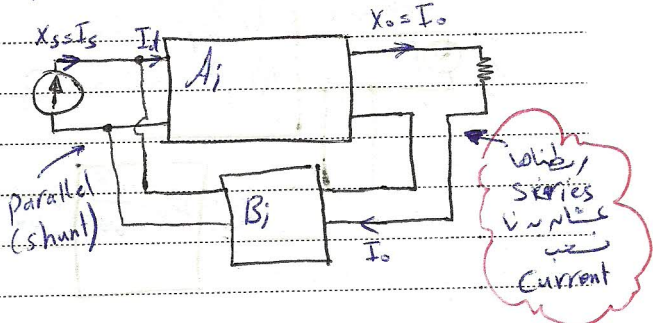


- with (f.b.)  $A_v = -g_m R_c$
- without (f.b.)  $A_v = -\frac{R_c}{R_E}$
- $R_i = R_c$
- $R_i = R_c + (\beta + 1) R_E$

2)  $X_s = I_s$ ,  $X_o = I_o$ , It is called (parallel-series) (current-shunt) <sup>opp</sup> I/P

Used with current Amp.

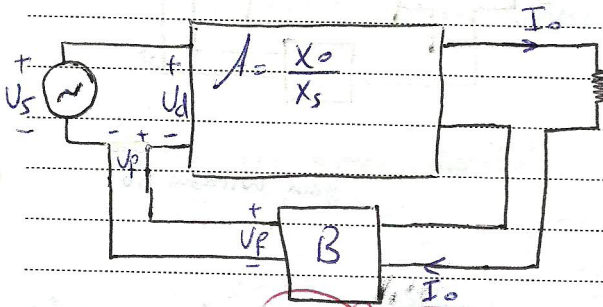
$R_{if} \downarrow$ ,  $R_o \uparrow$



لواظب / Series voltage feedback current

3)  $X_s = V_s, X_o = I_o$ , called  
(current-series) (series-series)

Used with: Transconductance Amp.,  $R_i \uparrow$  &  $R_o \uparrow$



series

بشكل عام التوازي يقلل  $R_i$  و التوازي يزيد  $R_o$

في كل ما يكون ال loop مغلقة عن طريق التيار

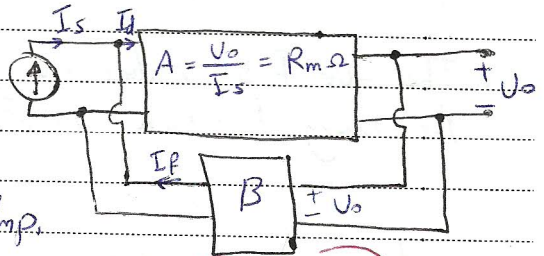
$B = \frac{V_f}{I_o} (\Omega)$

$A = \frac{I_o}{V_s} \Omega = G_m$

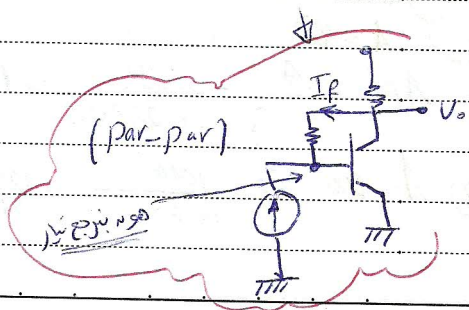
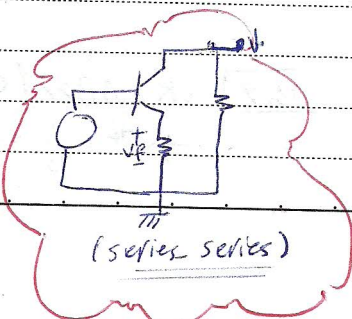
4)  $X_s = I_s, X_o = V_o$   
(parallel-parallel) (voltage-shunt)

Used with transresistance Amp.

$R_i \downarrow, R_o \downarrow$

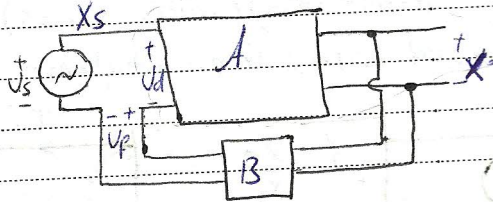


$B = \frac{I_f}{V_o} \Omega$



## " Effects of -ve feedback on Amp. parameters "

① Reduce Amp. gain:-



$$X_o = A X_d$$

$$X_d = X_s - X_p$$

$$X_p = B X_o$$

$$\Rightarrow X_o = A (X_s - B X_o)$$

$$X_o = A X_s - A B X_o$$

$$X_o (1 + A B) = A X_s \Rightarrow$$

$$\frac{X_o}{X_s} = \frac{A}{1 + A B} = A_f$$

F.B. factor

gain without F.B

gain with F.B

- $A_f \rightarrow$  gain with F.B. (closed loop gain)
- $A \rightarrow$  " without " (open " " " " )
- $B \rightarrow$  F.B. factor

• The -ve F.B. reduce the gain.

• for heavy feedback  $A B \gg 1 \Rightarrow A_f = \frac{1}{B}$

Ex. An Amp. has 9% -ve F.B. ( $B = 0.09$ ), calculate the gain after F.B. when

①  $A = 100$

$$A_f = \frac{A}{1 + A B} = \frac{100}{1 + 0.09 \times 100} = 10$$

②  $A = 1000$   $A_f = \frac{1000}{1 + 0.09 \times 1000} = \frac{1000}{91} = 10.9$  OR  $A B \gg 1 \ll 90$

$$\Rightarrow A_f = \frac{1}{B} = \frac{1}{0.09} = 10.9$$



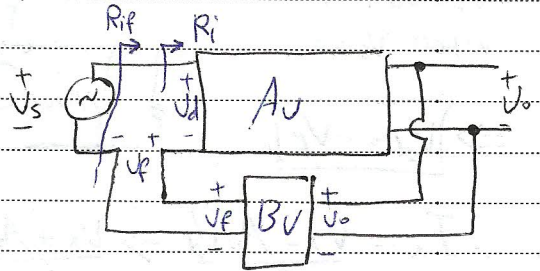
② Controll the input and output impedance:-

• It can dict or inc↑ the Amp. impedance depending on the topology (connection). where the series connection inc↑ the imp. & The parallel (shunt) dict the imp.

• Consider the series-parallel connection:-

•  $V_s = V_p + V_d$   
 $= V_d + B_v V_o$   
 but  $V_o = A_v V_d$

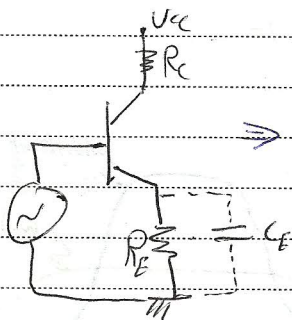
⇒  $V_s = V_d + B_v A_v V_d$   
 $= V_d (1 + B_v A_v)$



Divided by  $I_i$  ⇒  $\frac{V_s}{I_i} = \frac{V_d}{I_i} (1 + B_v A_v)$

⇒  $R_{iF} = R_i (1 + A_v B_v)$

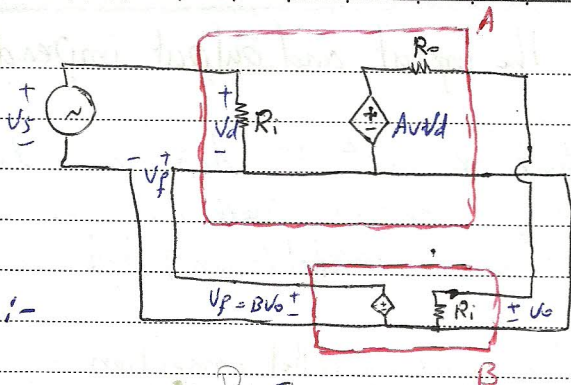
\* Note :-



•  $A_v = -g_m R_c$  } CE present (no P.B.)  
 $R_i = R_B$

⇒ •  $A_v = -\frac{R_c}{R_E}$  } without CE  
 •  $R_{iF} = R_B + (1 + \beta) R_E$  } -ve P.B. series connection

$A_v, R_{iF}$

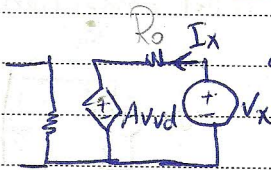


- to find  $R_{of}$  :-

•  $v_s = v_d + v_f$

when  $v_s = 0$

$\Rightarrow v_d = -v_f$



output  $v_x$  &  $R_o$   $\Rightarrow R_o = \frac{v_x}{I_x} \Big|_{v_s=0}$

$I_x = \frac{v_x - A_v v_d}{R_o} \Rightarrow \frac{v_x + A_v v_f}{R_o} = \frac{v_x + v_o B A_v}{R_o}$

$I_x = \frac{v_x (1 + B A_v)}{R_o}$

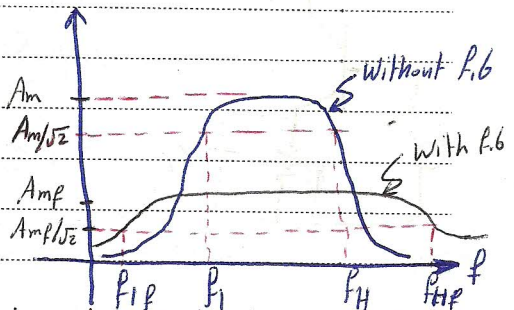
$\Rightarrow R_{of} = \frac{v_x}{I_x}$

$R_{of} = \frac{R_o}{1 + B A_v}$

∴ Shunt Connection Reduce impedance...

③ Extend the Bandwidth of Amp. :-

• Since -ve f.b. reduces the gain, so it inc<sup>r</sup> the B.W.





⑤ Reduce Amp. Internal Noise and Improve S/N ratio:

$$X_{nf} = \frac{X_n}{1 + \beta A}$$

$X_{nf}$  → internal noise with f.b.  
 $X_n$  → internal noise without f.b.  
 ← unwanted signal

- Thermal noise is generated in Active and passive devices such as resistors.
- ① داخلية (حرارة، المقاومة)  $\rightarrow$  BJT
- ② ظاهرة مثل اختلاف تركيز الهواء، والغيبار

⑥ Increase Amp. gain stability:

$$\frac{dA_f}{A_f} = \frac{dA/A}{1 + \beta A}$$

- $A \rightarrow$  Amp. gain without f.b.
- $A_f \rightarrow$  " " " with "
- $\frac{dA}{A} \rightarrow$  Fractional change in gain without f.b.
- $\frac{dA_f}{A_f} \rightarrow$  " " " with "

• Due to ageing and temp. effect the Amp. gain deviate or change but if -ve F.b. is used it can stabilize Amp. gain.

• يعني لو صممتنا Amp. gain = 100

لو صممتنا بعد سنة ربع نلا فيه 90. كذا زياد عمر Component وكثرة الاستعمال تؤدي إلى ازدياد الحرارة. فرق يختلف  $\Delta A = 100 - 90 = 10$  أما لو عملنا نفس ال Amp مع -ve f.b.

$$\frac{\Delta A_f}{A_f} = \frac{100 - 98}{100} \text{ gain} = 98$$

لو صممتنا بعد سنة ربع نلا فيه 98.  $\rightarrow$  gain stability = 0.02

Ex. An Amp. has again of 100, if for a certain reason the gain reduce to 80., Now if -ve f.b. of  $B=9\%$  is Used Calculate  $dA_f$  ?

$$\bullet \frac{dA}{A} = \frac{100-80}{100} = 20\%$$

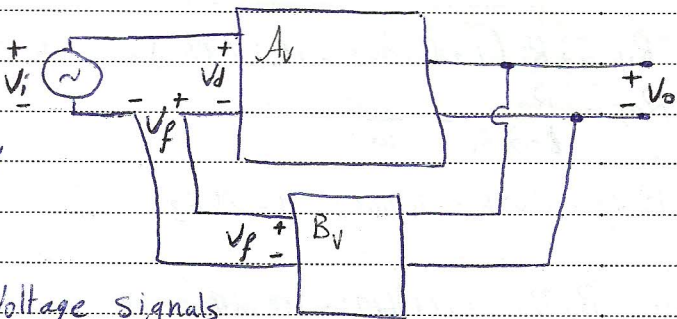
$$\bullet \frac{dA_f}{A_f} = \frac{dA/A}{1+BA}$$

$$\bullet 1+BA = 1+(0.09)(100) = 10$$

$$\Rightarrow \frac{dA_f}{A_f} = \frac{20\%}{10} = 2\%$$

① Series shunt F.B:-

• Used with Voltage Amp.'s



•  $X_s, X_o, X_f, X_d \rightarrow$  Voltage signals

$$\bullet A = A_v = \frac{V_o}{V_d}$$

$$\bullet B = B_v = \frac{V_f}{V_o} \text{ (Voltage ratio)}$$

$$\bullet A_{v_f} = \frac{A_v}{1 + B_v A_v}$$

$$\bullet D_f = \frac{D}{1 + B_v A_v}$$

$$\bullet X_{n_f} = \frac{X_n}{1 + B_v A_v}$$

$$\bullet (B.W)_f = (B.W)(1 + B_v A_v)$$

$$\bullet R_{if} = R_i (1 + B_v A_v)$$

$$\bullet R_{of} = \frac{R_o}{1 + B_v A_v}$$

Ex: An Amp. has  $A_v = 10^5$ ,  $A_{vP} = 100$ ,  $R_i = 10k\Omega$ ,  $R_o = 20\Omega$ ,  $B.W = 200\text{ KHz}$ . When series shunt f.b. is applied

1) Find Amp. parameters after feed back.

2) If  $V_o = 10\text{ V}$ , find  $V_d$ ,  $V_s$ ,  $V_p$ ?

Sol:

$$\textcircled{1} 100 = \frac{10^5}{1 + B_v A_v} \Rightarrow 1 + B_v A_v = 1000$$

$$\Rightarrow B_v A_v = 999 \Rightarrow B_v = \frac{999}{10^5} \approx 0.00999$$

$$\bullet R_{if} = R_i (1 + B_v A_v) = 10k(1000) = 10\text{ M}\Omega$$

$$\bullet R_{of} = \frac{R_o}{1 + B_v A_v} = \frac{20k}{1000} = 20\Omega$$

$$\bullet B.W_f = (100\text{ KHz})(1000) = 100\text{ MHz}$$

$$\textcircled{2} \bullet V_p = B_v V_o = (0.01)(10) = 100\text{ mV}$$

$$\bullet V_d = \frac{V_o}{A_v} = \frac{10}{10^5} = 100\text{ }\mu\text{V} = 0.1\text{ mV}$$

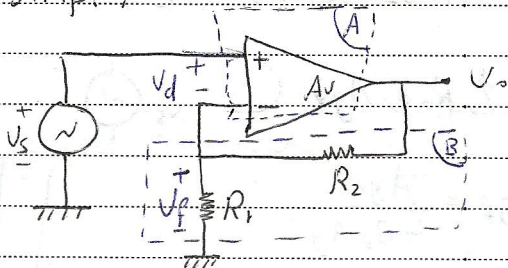
$$\bullet V_s = V_d + V_p = 0.1\text{ mV} + 100\text{ mV} = 100.1\text{ mV}$$

• Series-شنت نوع  
Voltage Amp.  
طول shunt

\* Series-shunt in op. Amp. Amp. :-

$$V_p = \frac{V_o R_1}{R_1 + R_2}$$

$$\frac{V_p}{V_o} = \frac{R_1}{R_1 + R_2} = \beta$$



$V_s$  is in series  $V_p$  is in shunt f.b. -ve f.b.

open loop gain =  $A_v = A_o \times 10^5$

$$A_{vf} = \frac{A_v}{1 + \beta A_v} \approx \frac{1}{\beta} \Rightarrow A_{vf} = \frac{R_1 + R_2}{R_1} = \left(1 + \frac{R_2}{R_1}\right)$$

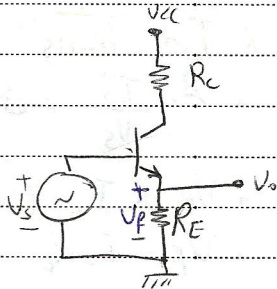
\* Series-shunt in transistors cct :-

$$\beta = \frac{V_p}{V_o} = 1$$

here  $V_p$  is in series with  $V_s$  & opposite in sign  $\Rightarrow$  -ve f.b.

$V_p$  is depend on  $V_o$  (if  $V_o = 0 \Rightarrow V_p = 0$ )

$\therefore$  series-shunt



here  $V_p$  is opposite  $V_o \Rightarrow$  -ve f.b.

$$\beta = \frac{V_p}{V_o} = \frac{R_2}{R_1 + R_2}$$

ex. if  $R_1$  is grows from (1  $\rightarrow$  5) find  $R_1, R_2$ ?

$$R_1 \cdot \beta = R_1 (1 + \beta A_v) \Rightarrow \beta = \left[ \frac{R_1 \beta}{R_1} - 1 \right] / A_v$$

njb • Sied's - shunt

$R_1, R_2, A_v, \dots$

$$\beta = \frac{R_2}{R_1 + R_2} \text{ Assuming } R_1 = \dots \Rightarrow R_2 = \dots$$

if  $V_o = 0 \Rightarrow V_p = 0$

② Series-Series F.B :-

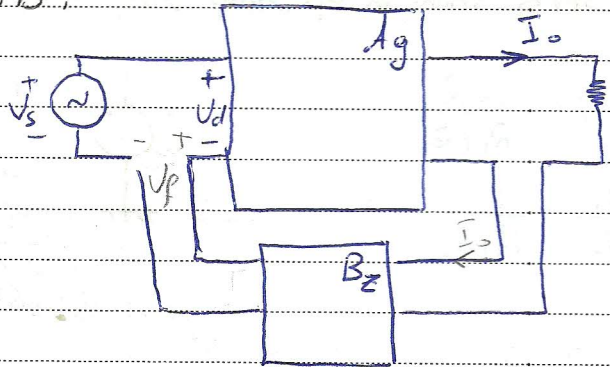
•  $R_i \uparrow, R_o \downarrow, A_g \downarrow$

•  $A_{gf} = \frac{A_g}{1 + B_z A_g}$

•  $A = \frac{I_o}{V_d} = A_g \Omega$

•  $\beta = \frac{V_f}{I_o} = B_z \Omega$

• A.B (Unitless)



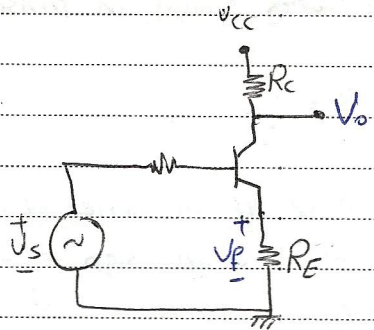
\* In Trans's cct's :-

•  $A = \frac{I_o}{V_s} = G_m = A_{gf} \Omega$

•  $V_f \propto I_o$  (When  $I_E = 0 \Rightarrow V_f = 0$ )

•  $V_f = I_o R_E$

•  $\beta = \frac{V_f}{I_o} = R_E \Omega$



•  $R_{if} = R_i (1 + B_z A_g)$

•  $R_{of} = R_o (1 + B_z A_g)$

~~$R_{of} = \frac{R_o}{1 + B_z A_g}$~~   
 •  $V_f \neq 0 \leftarrow I_o = 0 = V_o \frac{V_f}{V_o}$   
 •  $V_f = 0 \leftarrow I_o = 0$  (المواكبت)

•  $A_{gf} = \frac{A_g}{1 + B_z A_g} \rightarrow \frac{I_o}{V_d}$

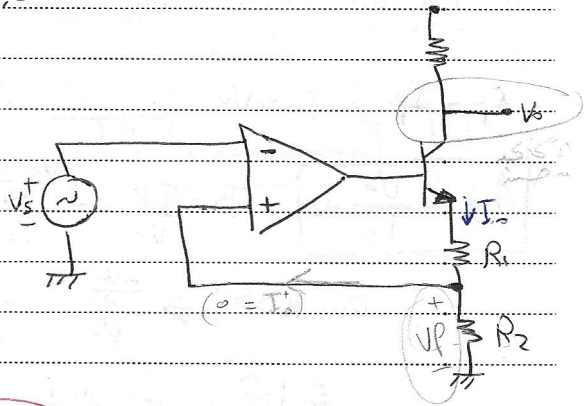


\* In op Amp. ckt :-

•  $V_p$  &  $I_o$

$$B = \frac{V_p}{I_o} = \frac{R_2 I_o}{I_o} = R_2 \Omega$$

$$A_{gf} = \frac{I_o}{V_s}$$



• شکل عام اولی بتوضیح نوع  $V_p$   
 • اذا كنت مرجع الحمل توای اذاً مرجع فولتیة و اذا كنت مرجع الحمل توای اذاً مرجع تيار  
 • بالنسبة لـ output اذا ماخذت من لوپ توای اذاً ماخذت تيار و اذا كنت ماخذت من نوډ توای اذاً ماخذت فولتیة

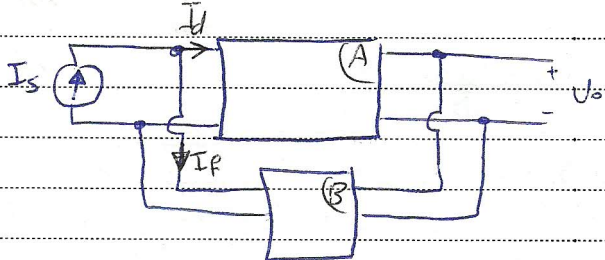
•  $V_p$  بتعريف على  $I_o$  و  $V_o$  لانه لو شورتنا  $V_o$  ارج  $V_p \neq 0$  اما لو صارت  $I_o = 0 \leftarrow V_p = 0$

③ Shunt - Shunt F.b :-

$$A = \frac{V_o}{I_i} = A_z \Omega$$

$$B = \frac{I_f}{V_o} = B_g \Omega$$

•  $B \cdot A$  (Unitless)



$$A_{zf} = \frac{A_z}{1 + B_g A_z}$$

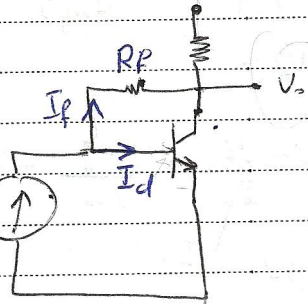
$$R_{if} = \frac{R_i}{1 + B_g A_z}$$

$$R_{of} = \frac{R_o}{1 + B_g A_z}$$

\* In Fan's ckt<sup>s</sup> :-

$x_p = I_p$  ,  $x_o = V_o$

$A_z = \frac{V_o}{I_s} \cdot B = \frac{I_p}{V_o} = \frac{V_{RE} - V_o}{R_F} \cdot I_s$



but  $V_o \gg V_{RE} \Rightarrow \frac{-V_o}{R_F} = \frac{-1}{R_F}$

$B = \frac{-1}{R_F}$

•  $I_s$  فعل و  $I_p$  راجع  
 •  $I_p$  راجع  $I_s$  راجع  
 •  $I_s$  فعل و  $I_p$  راجع

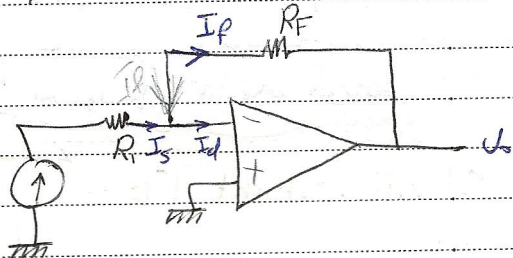
• مارجع  $I_s$  راجع  
 • مارجع  $I_p$  راجع

\* In op-Amp ckt<sup>s</sup> :-

$I_d = 0$

$I_s = I_p$

$A_z = \frac{1}{B}$



$A_{zf} = \frac{V_o}{I_i} = \frac{V_o}{I_p}$

$= \frac{V_o}{B V_o} = \frac{1}{B} = A_{zf}$

$A_{zf} = \frac{V_o}{I_i} = \frac{-I_p \cdot R_F}{I_i} = -R_F$

$B = \frac{-1}{R_F}$

**4** Shunt-Series F.b. :-

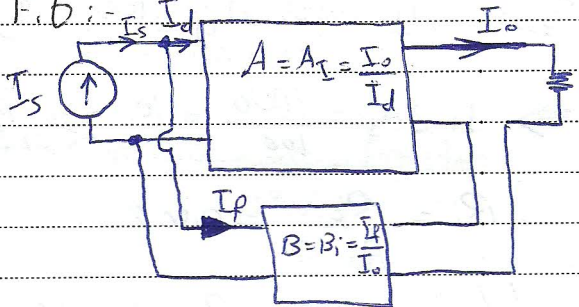
• Used with current Amp.

•  $A_{If} = \frac{I_o}{I_s}$

•  $R_i \downarrow, R_o \uparrow, A_{If} \downarrow$

•  $A_I = \frac{I_o}{I_d}$

•  $A_{If} = \frac{A_I}{1 + \beta_i A_i}$



~~$I_f = I_o$~~

x In Trans. cct's :-

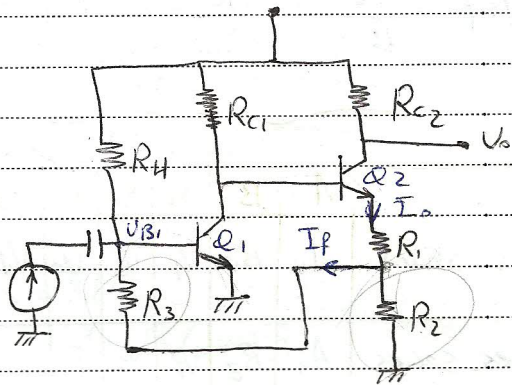
$I_f = \frac{I_o R_2}{R_2 + R_3}$

here we assume that

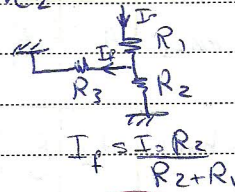
$R_3 \parallel R_2$  because:

$V_{c1} \gg V_{B1}, V_{e2} \approx V_{c1}$

$\Rightarrow V_{e2} \gg V_{B1} \Rightarrow V_{B1} \approx 0$  compared with  $V_{e2}$



$\therefore \frac{I_f}{I_o} = \beta = \frac{R_2}{R_2 + R_3}$



Ex. The cct shown has  $R_1 = 10k\Omega$ ,  $R_o = 1k\Omega$ ,  $A_I = 1000$ , it's required to make the gain = 100, find  $R_2, R_3$  are requires to that, also find  $R_{if}, R_{of}$  ?

$R_1$  ~~is~~  $\beta$

Subject .....

Sol.  $A_I = 1000, A_{IF} = 100, A_{IF} = \frac{A_I}{1 + B_i A_i}$

$\Rightarrow 1 + B_i A_i = \frac{1000}{100} = 10 \Rightarrow B_i = 0.009$

$B_i = \frac{R_2}{R_2 + R_3} = 0.009$

let  $R_2 = 9 \text{ K}\Omega, R_3 = 991 \text{ K}\Omega$

$R_{if} = \frac{10}{10} = 1 \text{ K}\Omega, R_{of} = 1 \times 10^4 = 10 \text{ K}\Omega$

| F.B.T         | A     | B     | $X_p$ | $X_s$ | $X_o$ | $X_d$ | $R_{if}$                   | $R_{of}$                | Amp.                  |
|---------------|-------|-------|-------|-------|-------|-------|----------------------------|-------------------------|-----------------------|
| Series-shunt  | $A_v$ | $B_v$ | $V_p$ | $V_s$ | $V_o$ | $V_d$ | $R_i(1+B_i A_i)$           | $\frac{R_o}{1+B_v A_v}$ | Voltage Amp.          |
| Series-series | $A_g$ | $B_z$ | $V_p$ | $V_s$ | $I_o$ | $V_d$ | $R_{xp}(1+B_z A_g)$        |                         | Transconductance Amp. |
| shunt-series  | $A_i$ | $B_i$ | $I_p$ | $I_s$ | $I_o$ | $I_d$ | $\frac{R_i}{1+B_i A_i}$    | $R_o(1+B_i A_i)$        | Current Amp.          |
| shunt-shunt   | $A_z$ | $B_g$ | $I_p$ | $I_s$ | $V_o$ | $I_d$ | $\frac{R_{xp}}{1+B_g A_z}$ |                         | Trans.resistance Amp. |

## " Oscillators (signal generator) "

D) Sinusoidal oscillator :-

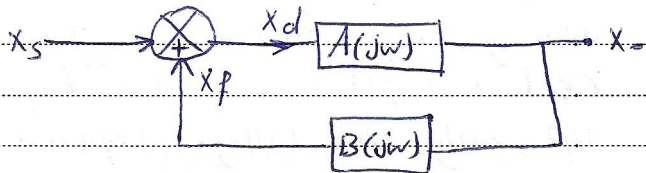
پیشانی F.b Amp. عن بارة ع.ع. +ve F.b

- $A(j\omega)$

- A & B is fn. of freq.

- $B(j\omega)$

- Amplitude & freq. of A.C. input signal



- $X_o = A(j\omega) X_d$

- $X_d = X_s + X_p$

- $X_p = X_o B(j\omega)$

$$\Rightarrow X_o = A(j\omega) [X_s + X_p]$$

$$X_o = A(j\omega) [X_s + X_o B(j\omega)]$$

$$X_o = A(j\omega) X_s + A(j\omega) X_o B(j\omega)$$

$$X_o - A(j\omega) B(j\omega) X_o = A(j\omega) X_s$$

$$X_o (1 - A(j\omega) B(j\omega)) = A(j\omega) X_s$$

$$A_f = \frac{X_o}{X_s} = \frac{A(j\omega)}{1 - A(j\omega) B(j\omega)}$$

- when  $|A(j\omega) B(j\omega)| = 1$

- $A_f = \frac{X_o}{X_s} = \infty$  (but  $X_o \neq \infty$  (finite) So  $A_f = \infty$  means

that  $X_s = 0$  i.e. no input signal)

• This condition will be satisfied at a certain value of  $(\omega)$  called  $\omega_0$  (Frequency of oscillation) i.e. the F.B Amp. will give an o/p Ac signal with a certain Amplitude and a certain freq. without any input i.e. it will work as an oscillator...

• Oscillator : a F.B a Amp use +ve feed.b and gives periodical Ac output signal with a certain Amplitude & certain freq. without any Ac inp, only Dc. Voltage required for basic Amp.

• Oscillation conditions (Barkhausen Condition):

1) Magnitude Condition :-

$$|A(j\omega) B(j\omega)| = 1$$

⇒ loop gain = 1 ,  $A_{min} = \frac{1}{B}$  ,  $A > 1$  Amp ,  $B < 1$  passive cct.

مقدار أكبر من 1 (5%)

Two conditions at single freq.

2) Phase condition :-

$$\angle A(j\omega) B(j\omega) = 0^\circ, 360^\circ = 2\pi n \quad , \quad n = 0, 1, 2, \dots$$

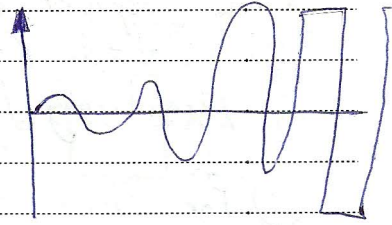
Two conditions at single freq.  $\omega_0$

1)  $\angle A = 0^\circ$  ,  $\angle B = 0^\circ \Rightarrow \angle A, B = 0^\circ$

2)  $\angle A = 180^\circ$  ,  $\angle B = 180^\circ \Rightarrow \angle A, B = 360^\circ$

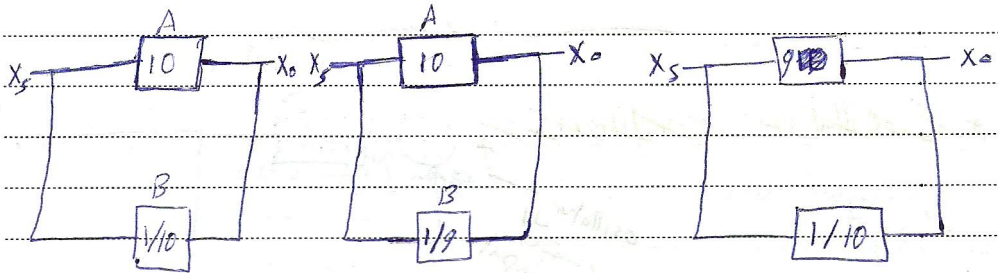
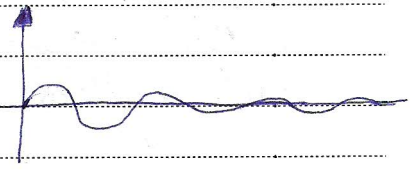
• If  $BA \gg 1$ :

This will give uncontrolled o/p and drives the Amp. into Saturation



• If  $BA \ll 1$ :

The osc. will start and will be clamped (die)



$AB = 1$

$AB > 1$

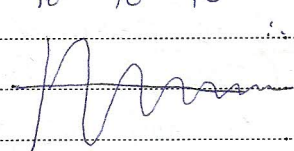
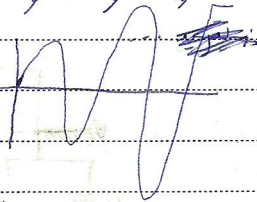
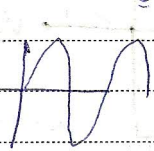
$AB < 1$

∴ stable

المدخل 10 في 10  
المخرج 10 في 10  
كل مرة  
10/9

المدخل 10 في 10  
المخرج 10 في 10  
كل مرة  
 $\frac{10}{9} \times \frac{10}{9} \times \frac{10}{9}$

المدخل 9 في 9  
المخرج 10 في 10  
كل مرة  
 $\frac{9}{10} \times \frac{9}{10} \times \frac{9}{10}$



\* The required conditions :-

①  $|BA| = 1$  (magnitude condition)

practically  $|BA| = 1 + 5\%$

② For phase condition :-

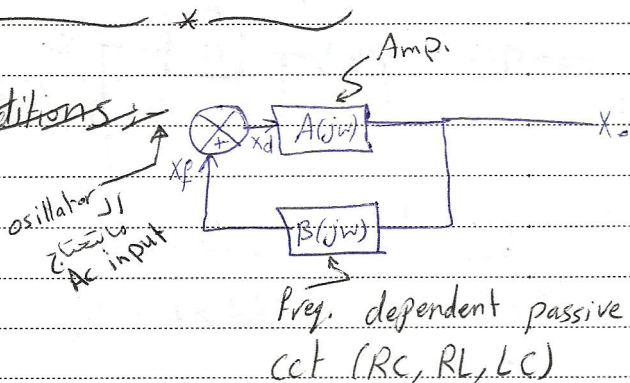
Either Both Amp. & B- Network has  $180^\circ$  phase

~~$\angle BA = 0, 360$~~

shift or Both Amplifier & B-Net. has Zero phase

i.e. A & B inverting or A & B non-inverting

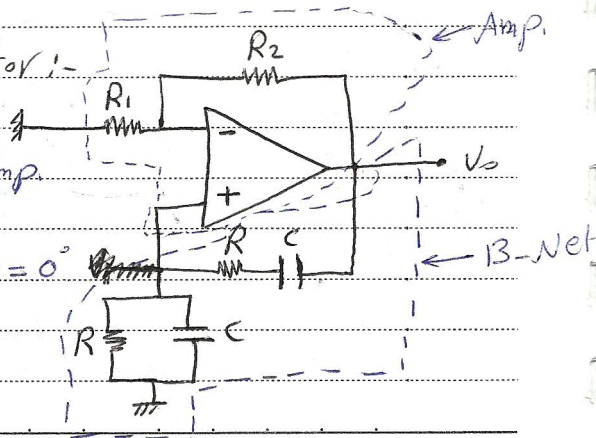
\* Oscillation conditions :-



① Wien-Bridge oscillator :-

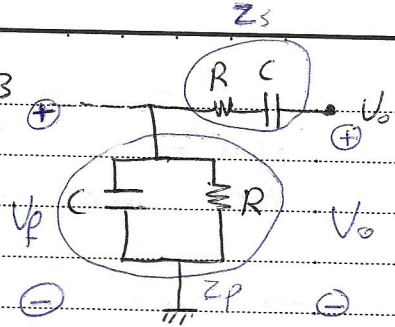
A is non-inverting Amp.  
(zero ph. shift)

$\Rightarrow$  B must give ph. shift =  $0^\circ$   
to satisfy  $\angle BA = 0^\circ$





\* derive an expression for  $\beta$



$$V_p = V_o \frac{Z_p}{Z_p + Z_s}$$

$$\frac{V_p}{V_o} = \frac{Z_p}{Z_p + Z_s} = \beta$$

$$\bullet Z_p = \frac{R \cdot \frac{1}{j\omega C}}{R + \frac{1}{j\omega C}} = \frac{R}{1 + j\omega RC}$$

$$\bullet Z_s = R + \frac{1}{j\omega C}$$

$$\Rightarrow \beta = \frac{(R/1 + j\omega RC)}{(R + \frac{1}{j\omega C}) + (R/1 + j\omega RC)} = \frac{R}{(1 + j\omega RC) \left[ \left( R + \frac{1}{j\omega C} \right) + (R/1 + j\omega RC) \right]}$$

$$= \frac{\cancel{R}}{\cancel{3R} + \cancel{2j\omega R^2 C}} = \frac{R}{R + \frac{1}{j\omega C} + j\omega R^2 C + R + R}$$

$$= \frac{R}{3R + j\omega R^2 C + \frac{1 \times j}{j\omega C}} = \frac{R}{3R + j\omega R^2 C + \frac{j}{\omega C}}$$

$$\beta = \frac{R}{3R + j(\omega R^2 C - \frac{1}{\omega C})}$$

∴ The  $B$  will give zero phase when (J) term = 0

$$\text{i.e. } \omega_0 R^2 C = \frac{1}{\omega_0 C} \Rightarrow \omega_0^2 R^2 C^2 = 1$$

$$\Rightarrow \omega_0 = \frac{1}{RC} \quad \text{"Freq. of Oscillation"}$$

$$f_0 = \frac{1}{2\pi RC}$$

$$\text{At this freq } B = \frac{\frac{2}{3}R}{3R + j0} = \frac{R}{3R} = \frac{1}{3}$$

$$\& \text{ ph. shift} = 0$$

$$\angle B = 0^\circ, |B| = 1/3$$

$$\text{To satisfy } |BA| = 1 \quad A_{\min} = 3$$

$$\text{For non inverting Amp } A = 1 + \frac{R_2}{R_1}$$

$$1 + \left(\frac{R_2}{R_1}\right)_{\min} = 3 \Rightarrow \boxed{R_{2,\min} = 2R_1}$$

Ex. Design a Wien-Bridge oscillator to give a freq of oscillation of 10K-Hz?

$$\text{let } C = 0.1 \mu\text{F}, \quad R = \frac{1}{2\pi f C} = \frac{1}{(2)(\pi)(10^4)(10^{-6})}$$

$$\boxed{R = 160 \Omega}$$

To satisfy magnitude condition  $A_{min} = 3, R_2 = 2R_1$

let  $R_1 = 1K\Omega, \Rightarrow R_2 = 2K\Omega$

• إذا كان  $A_{min}$  يعني  
 $A_c$  input signal  
 بين  $V_{cc}$  و  $V_{ee}$  على  
 ال op Amp  
 نشغل ال Transistors

\* Note :-

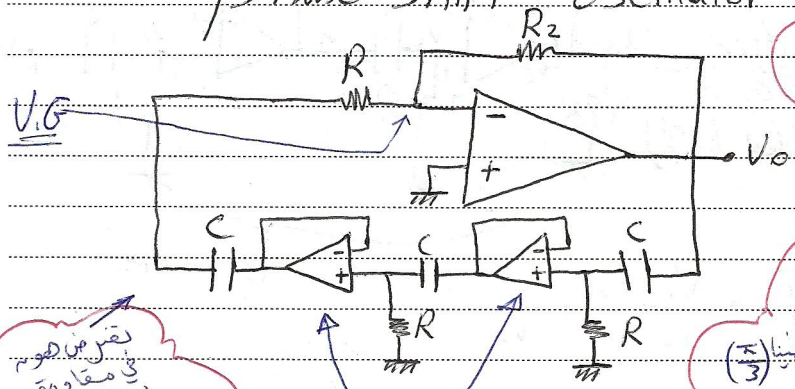
if we want to use BJT or Mosfet insted of the op Amp in Wien bridg we must use :-

- Common base for BJT
- Common Gate " Mosfet
- & non inverting for op-Amp

• ممكن بظنك cot  
 و يكون  $R_2 \neq 2R_1$  وانت  
 تحل زي ال آخر وبالآخر  
 يطالع غلط

To give ph-shift = 0° From Amp.

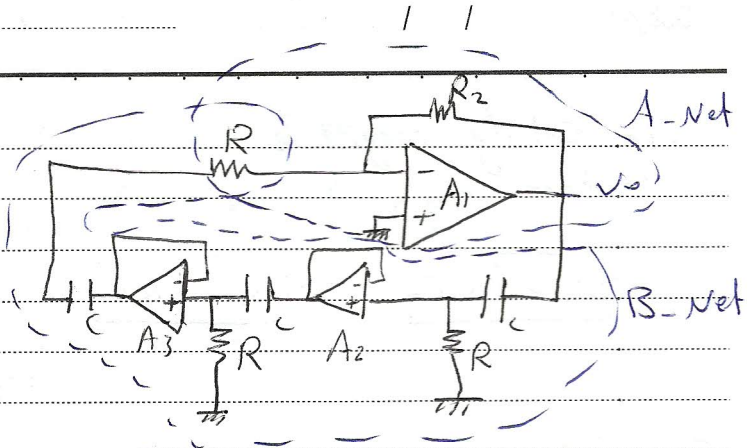
" Phase shift oscillator "



• أكبر زاوية بين R و C  
 هو  $\frac{\pi}{2}$  ملا يكونوا  
 Ideal و اما على  
 باي R, C يكونوا  
 Ideal فنتاهم فصل  
 على زاوية 180° مستقيم  
 3 R, C وكل واحد يعطى  $(\frac{\pi}{3})$

تفضل من هو  
 في مقادير  
 في  
 n j p b  
 تضاهي R التي توف  
 ضاهي R التي توف  
 ال (R) ال  
 ال (C) ال

Buffers  
 عندهم نشيل ال  
 loading affect



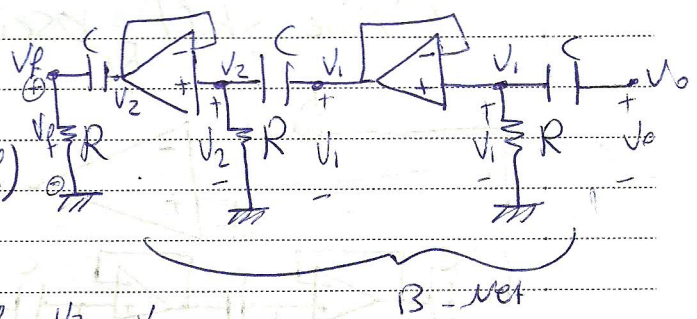
• Amp. gives  $180^\circ$  (Inverting)  
 ∴ B-net must give also  $180^\circ$ .

• each RC section can give  $60^\circ$  at certain freq

•  $A_1$  is basic Amp.  
 •  $A_2, A_3$ , is Buffers used to solve loading problem...

دائرة التذبذب  
 expression  
 لل B-net  
 phase shift  
 180 degrees  
 and the  
 condition of oscillation  
 B-net gain (V2/V1) is  
 equal to 1/3

• Remember that for buffer ( $R_i = \infty, R_o = 0, A_v = 1$ ) (Ideal buff.)



$$B = \frac{V_p}{V_o} = \frac{V_p}{V_2} \frac{V_2}{V_1} \frac{V_1}{V_o}$$

B-net

$$\beta = \left( \frac{R}{R + \frac{1}{j\omega C}} \right) \left( \frac{R}{R + \frac{1}{j\omega C}} \right) \left( \frac{R}{R + \frac{1}{j\omega C}} \right)$$

$\cdot V_1$  on  $R_1$   
 $\cdot V_0$  on  $R_1 \& C_1$

$$= \left( \frac{Rj\omega C}{j\omega RC + 1} \right)^3$$

$$\Rightarrow V_1 = \frac{V_0 R_1}{R_1 + \frac{1}{j\omega C}}$$

$$= \frac{-j\omega^3 R^3 C^3}{(1 + j\omega RC)(1 + j\omega RC)^2}$$

$$\Rightarrow \frac{V_1}{V_0} = \frac{R}{R + j\omega C}$$

$$= \frac{-j\omega^3 R^3 C^3}{(1 + j\omega RC)(1 + 2j\omega RC + j^2 \omega^2 R^2 C^2)}$$

$\cdot V_1$  on  $R_1 \& C_2$   
 $\Rightarrow V_2$  on  $R_2$   
 $\Rightarrow \frac{V_2}{V_1} = \frac{R_2}{R + \frac{1}{j\omega C}}$

$$= \frac{-j\omega^3 R^3 C^3}{1 + 2j\omega RC - \omega^2 R^2 C^2 + j\omega RC - 2\omega^2 R^2 C^2 - j\omega^3 R^3 C^3}$$

$$= \frac{-j\omega^3 R^3 C^3}{1 - \omega^2 R^2 C^2 - 2\omega^2 R^2 C^2 + j(2\omega RC + \omega RC - \omega^3 R^3 C^3)}$$

$$= \frac{j^3 \omega^3 R^3 C^3}{(1 - 3\omega^2 R^2 C^2) + j(3\omega RC - \omega^3 R^3 C^3)}$$

~~For~~  $\beta$  to give ph-shift = 180 the Real part

must equal zero ...

$$1 - 3\omega^2 R^2 C^2 = 0 \Rightarrow \omega_0^2 R^2 C^2 = \frac{1}{3}$$

$$\Rightarrow \omega_0 = \frac{1}{\sqrt{3}RC}$$

$$\frac{R^3}{\left( R^3 - \frac{R}{\omega C^2} - \frac{2R}{\omega C^2} \right) + j \left( \frac{-2R^2}{\omega C} - \frac{R^2}{\omega C} + \frac{1}{\omega C^3} \right)}$$

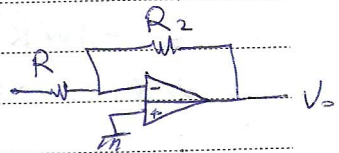
$$\Rightarrow f_0 = \frac{1}{2\pi\sqrt{3}RC} \quad \text{"freq. of oscillation"}$$

At this freq. 
$$\beta = \frac{j^2 W^3 R^3 C^3}{3WRC - W^3 R^3 C^3}$$

$$= \frac{j W^2 R^2 C^2}{3 - W^2 R^2 C^2}$$

$$\Rightarrow \beta = \frac{j \left( \frac{1}{3RC^2} \right) R^2 C^2}{3 - \frac{1}{3RC^2} R^2 C^2} = \frac{j^2 (1/3)}{3 - 1/3} = \frac{-1/3}{3 - 1/3} = \frac{-1}{8}$$

$$\Rightarrow \angle \beta = 180^\circ, |\beta| = \frac{1}{8}$$



To satisfy  $|\beta A| = 1 \Rightarrow |A_{min}| = 8$

For inverting Amp.  $|A| = \left( \frac{R_2}{R_1} \right)_{min} = 8 \Rightarrow \boxed{R_2 = 8R_1}$

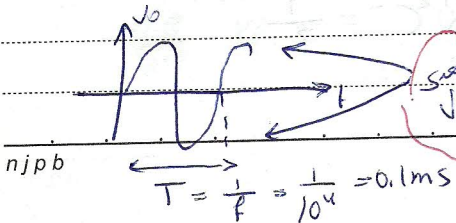
Ex. Design the ph-sh. oscillator shown in fig. to have  $f_0 = 10\text{KHz}$ ?

$$f_0 = \frac{1}{2\pi\sqrt{3}RC} \quad \text{let } C = 0.01 \mu\text{F}$$

$$\Rightarrow R = \frac{1}{2\pi\sqrt{3} \times 0.01 \times 10^{-6} \times 10^4} = \frac{10^4}{2\pi \times 1.73} = 920 \Omega$$

For the oscillator  $A_{min} = 8 = \frac{R_2}{R_1} \Rightarrow R_2 = 8R_1$

$$= 8 \times 920 \Omega = 7.4 \text{K}\Omega$$



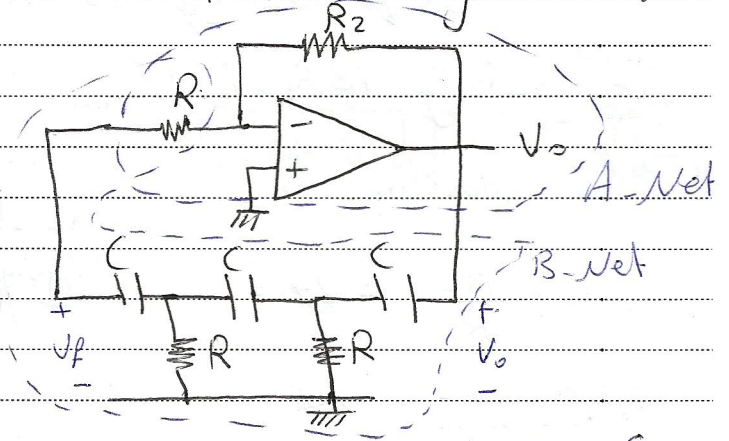
لا تفسد  
لا تفسد  
OP-AMP

دو بJT كزوج  
بند  
Vz سعيك يه 21



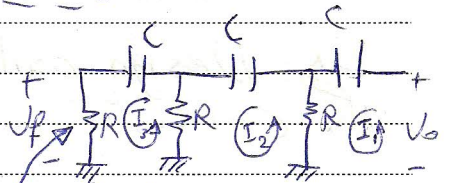
# \* Phase Shift Oscillator (Without Using Buffers)

• The same as the last oscillator but here we don't use buffers in B-Network



To find expression for B

$$B = \frac{V_p}{V_0}$$



• مع العلاقة التي سوف نشتقها  
 مع المعادلات التي سوف نشتقها  
 مع المعادلات التي سوف نشتقها

$$I_1 \frac{1}{j\omega C} + (I_1 - I_2)R - V_0 = 0$$

$$V_0 = I_1 \left( \frac{1}{j\omega C} + R \right) - I_2 R \quad \text{--- (1)}$$

$$\left( \frac{1}{j\omega C} + 2R \right) I_2 - I_1 R - I_3 R = 0 \quad \text{--- (2)}$$

$$\left( \frac{1}{j\omega C} + 2R \right) I_3 - I_2 R = 0 \quad \text{--- (3)}$$



by setting J-term = 0 to give 180° This will give

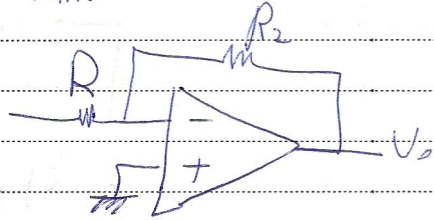
$$\omega_0 = \frac{1}{\sqrt{6}RC} \Rightarrow \boxed{f_0 = \frac{1}{2\pi\sqrt{6}RC}}$$

• At this freq.  $\beta = \frac{-1}{29} \Rightarrow |\beta| = \frac{1}{29}$  and  $\angle\beta = 180^\circ$

• To satisfy  $|\beta A| = 1$ ,  $|A_{min}| = 29$

• For inverting Amp.

$$|A| = \frac{R_2}{R_1} = 29$$

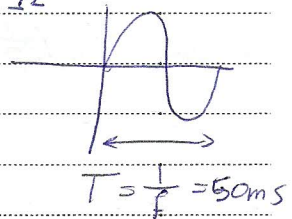


$$\Rightarrow R_{2min} = 29 R_1$$

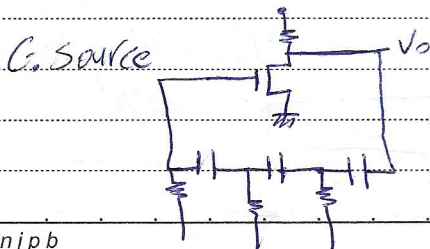
Ex. Design oscillator shown, to have  $f_0 = 20 \text{ kHz}$   
Use  $C = 0.01 \mu\text{F}$

$$R = \frac{1}{2\pi f_0 C} = \frac{1}{2\pi \times 20 \times 10^3 \times 0.01 \times 10^{-6}} = 324 \Omega$$

$$\frac{R_2}{R} = 29 \Rightarrow R_2 = 29 \times 324 = 9.4 \text{ K}\Omega$$



• if we want to replace the op-amp by Mosfet: or by CIE in BJT.



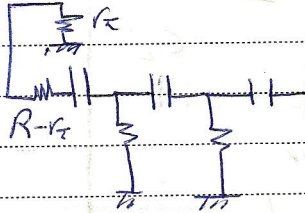
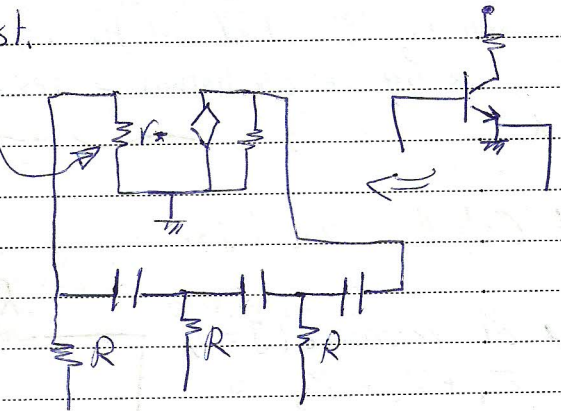
njpb

$$A = \frac{V_o}{V_{gs}} = g_m R_D \Rightarrow |g_m R_D| = 29$$



if we use C.E we will face a problem that is  $(r_x)$  is exist.

To solve this problem we connect the 3rd capacitor directly with  $r_x$  & put between them a resistor its value is  $R - r_x$



$$\Rightarrow R - r_x + r_x = R \quad \checkmark$$

## " Tuned Oscillators "

Use Amplifiers and LC cct's

op-Amp, BJT, Mosfet

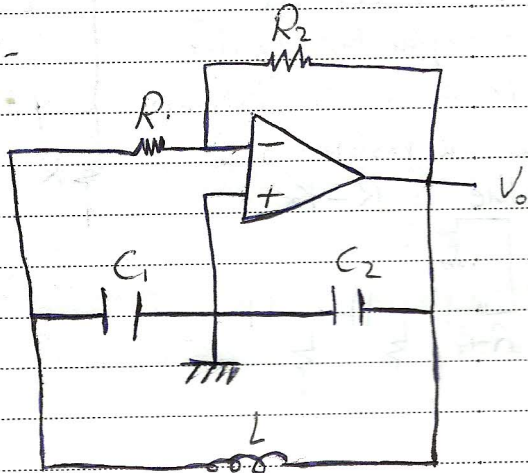
\* There are Two kinds of Tuned oscillators :-

1) Colpitts oscillator ( $2C + 1L$ )

2) Hartly oscillator ( $2L + 1C$ )

\* In the Tuned oscillators the phase condition will be satisfied at the resonant freq of the tuned ckt.  
 so freq of oscillation = resonance freq.

\* Colpitts oscillator:-



\* at resonance ( $\angle = 0$ )

$$Z_1 + Z_2 + Z_3 = 0$$

$$\frac{1}{j\omega C_1} + \frac{1}{j\omega C_2} + j\omega L = 0$$

$$-j\omega L = \frac{1}{j\omega C_1} + \frac{1}{j\omega C_2}$$

$$-j\omega L = \frac{1}{j\omega} \left( \frac{1}{C_1} + \frac{1}{C_2} \right)$$

$$\Rightarrow \omega L = \frac{1}{\omega} \left( \frac{1}{C_1} + \frac{1}{C_2} \right) \Rightarrow \omega^2 = \frac{1}{L} \left( \frac{1}{C_{eq}} \right)$$

$$\Rightarrow \omega_0 = \frac{1}{\sqrt{L C_{eq}}}$$

where  $C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$

$$\frac{1}{C_1} + \frac{1}{C_2} = \frac{C_1 + C_2}{C_1 C_2} = \frac{1}{C_{eq}}$$

$$\Rightarrow f_0 = \frac{1}{2\pi \sqrt{L C_{eq}}}$$

(Frequency of oscillation)

$$\beta = \frac{V_f}{V_0} = \frac{1/j\omega C_1}{1/j\omega C_2} = \frac{C_2}{C_1}$$

to have  $|\beta| = 1 \Rightarrow A_{min} = \frac{C_1}{C_2}$

∴ This in inverting op. Amp  $|A| = \frac{R_2}{R_1}$

$$\Rightarrow \boxed{\frac{R_2}{R_1} = \frac{C_1}{C_2}}$$

Ex. Design a Colpitts oscillator to give  $f_o = 100\text{kHz}$   
Use Mosfet biased at  $I_D = 1\text{mA}$ ,  $K_n = 1\text{mA/V}^2$ , Assume  
( $C_1 = 4C_2$ ) Find  $L$ ,  $R_D$ ?

$$\bullet f_o = \frac{1}{2\pi\sqrt{LC_{eq}}}, \quad C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

$$\bullet \beta = \frac{V_f}{V_o} = \frac{1/j\omega C_1}{1/j\omega C_2} = \frac{C_2}{C_1}$$

$$\beta = \frac{C_2}{C_1} = \frac{C_2}{4C_2} = \frac{1}{4}$$

$|A\beta| = 1 \Rightarrow A$  must be 4.

$$A_{min} = 4 \text{ and } |A| = |g_m R_D|$$

$$|A| = |g_m R_D| = 4$$

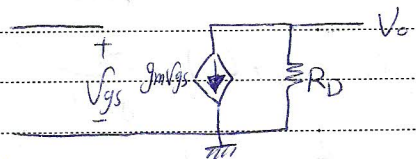
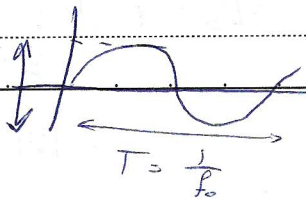
$$g_m = 2\sqrt{K_n I_D} = 2\sqrt{1} = 2\text{mA/V}$$

$$\therefore \boxed{R_D = 2\text{k}\Omega}$$

$$\text{let } L = 1\mu\text{H} \Rightarrow C_{eq} = \frac{1}{4\pi^2 f_o^2 L} = \frac{1}{4 \times 10^4 \times 10^6 \times 10^{-6}} = \frac{10^{-5}}{4}$$

$$= 0.25 \times 10^{-5} \text{F} = 2.5\text{pF}$$

Maximum  
output  
Voltage  
is  $V_{DD}$



ممكن يصحح سوال حل هاي السويكيت  
بتحل ك oscillator ولا لا وما بيا انا  $R_D = 4$  مثلاً

$A = 4.2$   $C = R_D = 21 \mu S$  اذا

$A_{min} = \frac{1}{B} = 4$

but  $A = 4.2 = 4 + 5\%$

$|A| = 1.05$  ✓

بتنطبق بعض oscillator  
بزيادة كوكم عن 5%

بتطلع  $\frac{1}{4} = \beta = \frac{C R_D}{C}$   
 $A = gm R_D$

$AB = 2 \text{ not } 1$   $= 2 \times 4 = 8$

so it doesn't work as an oscillator, the solution is decr the value of  $R_D$

\* Hartly oscillator :-

• In resonance freq  
J term of  $Z_{eq} = 0$

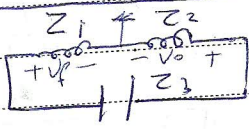
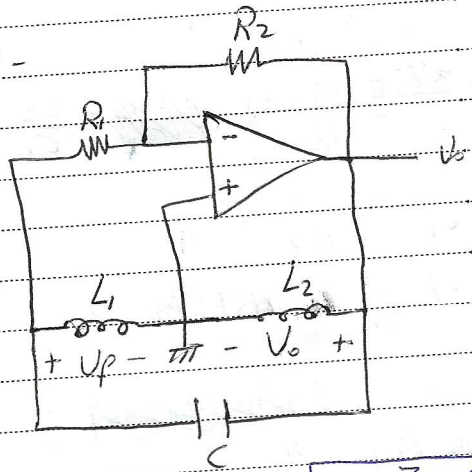
$j\omega L_1 + j\omega L_2 + \frac{1}{j\omega C} = 0$

$j\omega_0 (L_1 + L_2) = \frac{1}{j\omega_0 C}$

$\omega_0^2 = \frac{1}{C(L_1 + L_2)} \Rightarrow \omega_0 = \frac{1}{\sqrt{C(L_1 + L_2)}}$

•  $f_0 = \frac{1}{2\pi \sqrt{C(L_1 + L_2)}}$

•  $\beta = \frac{V_F}{V_0} = \frac{Z_1}{Z_2} = \frac{j\omega L_1}{j\omega L_2} = \frac{L_1}{L_2}$



$V_F = \frac{V_0 Z_1}{Z_1 + Z_2}$

$\frac{V_F}{V_0} = \frac{Z_1}{Z_1 + Z_2}$

$\beta = \frac{Z_1}{Z_2}$

•  $|\beta| = \frac{Z_1}{Z_2}$

To satisfy  $|AB| = 1$ ,  $A_{\min} = \frac{L_2}{L_1}$

For inverting Amp.  $A = \frac{R_2}{R_1}$

$$\Rightarrow \left(\frac{R_2}{R_1}\right)_{\min} = \frac{L_2}{L_1}$$

\* If  $L_1$  &  $L_2$  has Mutual inductance  $M$ , then the frequency of oscillation will be

$$f_o = \frac{1}{2\pi \sqrt{C(L_1 + L_2 \pm M)}} \quad , \quad \text{where } M: \text{ Mutual inductance}$$

$$M = K \sqrt{L_1 L_2}$$

$$K = \text{Coupling Coeff.}$$

Ex. Use An Ideal op-Amp. to design A hartly osc. to oscillate at (200KHz)

The max. gain for Amp. must not exceed 10. ?

$$P_{\text{for}} A = 10$$

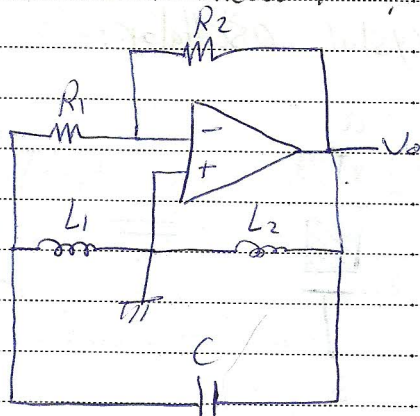
to satisfy  $|AB| = 1$

$$\Rightarrow B = \frac{1}{10}$$

$$B = \frac{V_f}{V_o} = \frac{L_2}{L_1} = \frac{1}{10}$$

$$L_1 = 10L_2$$

$$\text{let } L_2 = 1 \mu\text{H} \Rightarrow L_1 = 10 \mu\text{H}$$



$$p.e. C = \frac{1}{4\pi^2 f_0^2 (L_1 + L_2)^2} = \frac{1}{4\pi^2 (200)^2 (11)^2} = 5.2 \text{ mF}$$

•  $A = 10 = \frac{R_2}{R_1}$ , let  $R_2 = 5 \text{ K}\Omega \Rightarrow R_1 = 0.5 \text{ K}\Omega$

## " CRYSTAL Oscillator "

### ★ Frequency Stability :-

$$F.S = \frac{\Delta F}{F_0}$$

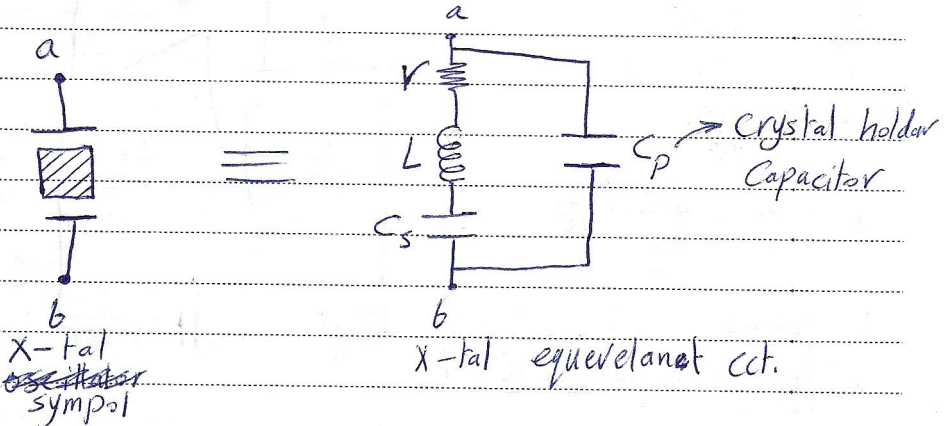
•  $\Delta F$  is Deviation in Frequency

•  $\Delta F$  is due to

- 1) Temp.
- 2) aging effect

• كل أنواع الـ oscillators  
 اس دقة يتأثر بالحرارة  
 والزمن ويتغير فيها الـ (f)  
 لذلك اذا اردنا ما ثابت  
 نستخدم crystal  
 oscillator

### ★ Crystal oscillator :-



\* It is based on using quartz crystal which is a piezoelectric material works as a series resonant ckt.

\* The parameters  $r, L, C_s$  depend on crystal dimensions and polarization.

\* When a voltage is applied across the crystal it will give an a.c. input signal of frequency:

$$f_0 = \frac{1}{2\pi\sqrt{LC_s}}$$

•  $L$  : in order of tens of Heneries.

•  $C_s$  : (series cap.) in the range of 0.001 pF.

• This oscillator has a very high quality factor

$$Q = \frac{\omega_0 L}{r} \text{ in the order of } 10^4$$

\* Advantages and disadvantages of X-tal osc. :-

1) high freq.

1) Fixed freq. →

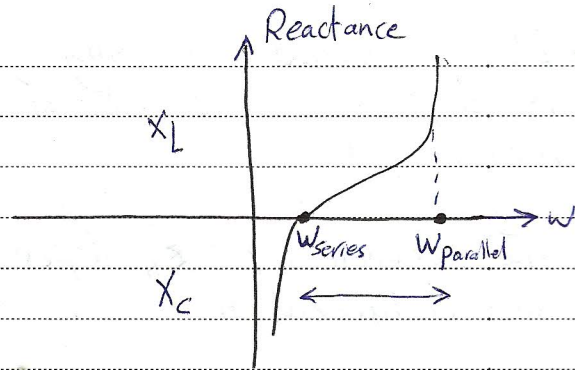
X-tal. oscillator.  $\int$   $C_s$  (pF)  $\int$

2) Very stable freq.

2) Fragile →  $\int$   $\int$   $\int$

والتذبذب

•  $\omega_0 = \frac{1}{\sqrt{L C_{s,p}}}$



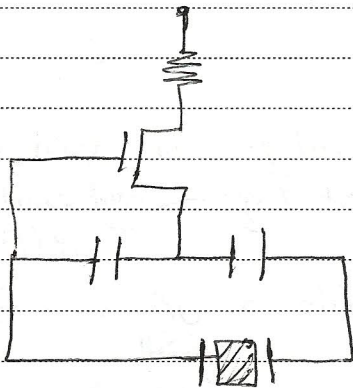
• When series (S) ( $\omega_s$ )  
Reactance = 0

• When parallel (P) ( $\omega_p$ )  
Reactance =  $\infty$

- When  $\omega$  between  $\omega_s$  &  $\omega_p$  the Reactance is inductive  
So the cryst. can be substituted as inductance.
- when  $\omega$  between 0 &  $\omega_s$  the Reactance is capacitive  
So the cryst. can be substituted as capacitance

Note :-

The x-tal can be behaves as an inductive or capacitive element. So it can be used to replace Inductor in ColPits osc. or capacitor in hartly osc.



Let's P as load  
if  $\omega$  is inductive  
if  $\omega$  is Cap. Coupled p. is  
(S.O. 4.1.2 (M.P.))





Ex. Derive an exp. for the Transfer Factor  $\beta$ -Net ( $\beta = \frac{V_f}{V_o}$ ) and find expression for oscillation freq ( $f_o$ ) and min. gain required by the Amp. to oscillation and use  $C = 0.01F$  to design the ckt to give  $f_o = 10KHz$  (find  $R_1, R_2, R_3$ )?

$$\bullet V_o - RI_1 - (I_1 - I_2) \frac{1}{j\omega C} = 0$$

$$\Rightarrow V_o = I_1 \left( R + \frac{1}{j\omega C} \right) - I_2 \frac{1}{j\omega C} \quad (1)$$

$$\bullet I_2 \left( R + \frac{2}{j\omega C} \right) - I_1 \frac{1}{j\omega C} = 0 \quad (2)$$

$$\bullet RI_2 = V_f, \Rightarrow I_2 = V_f / R$$

$$\bullet I_1 = I_2 (2 + j\omega RC)$$

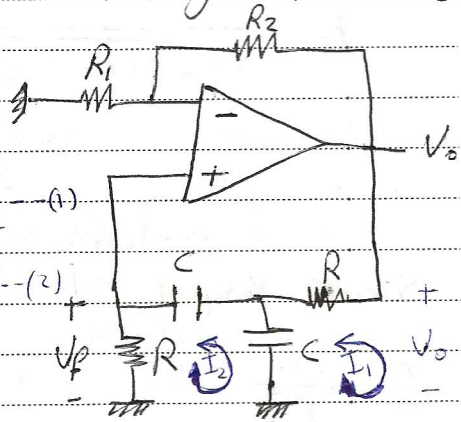
$$\Rightarrow \left( R + \frac{1}{j\omega C} \right) (2 + j\omega RC) \frac{V_f}{R} - \frac{V_f}{(R)(j\omega C)} = V_o$$

$$\Rightarrow \left[ \left( \frac{2R}{R} + \frac{2}{Rj\omega C} + \frac{j\omega RC^2}{R} + \frac{R}{R} \right) - \frac{1}{j\omega RC} \right] V_f = V_o$$

$$\Rightarrow \beta = \frac{V_f}{V_o} = \frac{1}{3 + \frac{2}{j\omega RC} + j\omega RC - \frac{1}{j\omega RC}}$$

$$\beta = \frac{1}{3 + j\omega RC - j \frac{2}{\omega RC} + j \frac{1}{\omega RC}}$$

$$\beta = \frac{1}{3 + j(\omega RC - \frac{2}{\omega RC} + \frac{1}{\omega RC})}$$



$$\therefore \left| \beta = \frac{1}{3 + j(\omega RC - \frac{1}{\omega RC})} \right|$$

• The Amp. is non-inverting Amp. (ph-shift = 0)  
So  $\beta$  will give zero phase shift if (J Term = 0)

$$\therefore \omega RC = \frac{1}{\omega RC} \Rightarrow \omega_0^2 = \frac{1}{R^2 C^2} \Rightarrow \omega_0 = \frac{1}{RC}$$

$$\therefore \left| \beta_0 = \frac{1}{2\pi RC} \right|$$

• in this freq  $\beta = \frac{1}{3} \Rightarrow$  to give  $|BA| = 1$

$$\left| A_{min} = 3 \right|$$

$$\therefore R = \frac{1}{(2\pi)(f_0)(C)} = \left| 795.77 \Omega \right|$$

•  $|A|_{(non\ inverting)} = \frac{R_2}{R_1} \Rightarrow \left( \frac{R_2}{R_1} + 1 \right) = 3$  "Non inverting op-Amp"

let  $\left[ R_1 = 1K\Omega \right] \Rightarrow \left[ R_2 = 2K\Omega \right]$

# "NON Sinusoidal oscillators (Relaxation osc<sup>ns</sup>)"

It depends on charging & discharging of cap.

- 1) Astable MTV    2) Monostable MTV    3) Bistable MTV
- multivibrator

## \* Astable MTV :-

• The op-Amp work as a comparator

• The comparator :-

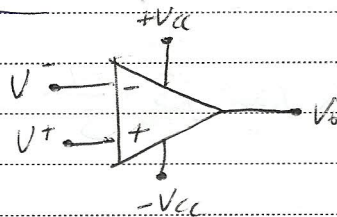
$$V_o = A_o (V^+ - V^-)$$

$$V_{o(max)} = +V_{cc}$$

• For Ideal op-Amp ( $A_o = \infty$ ):

1) if  $V^+ > V^- \Rightarrow V_o = +V_{cc}$

2) if  $V^- > V^+ \Rightarrow V_o = -V_{cc}$

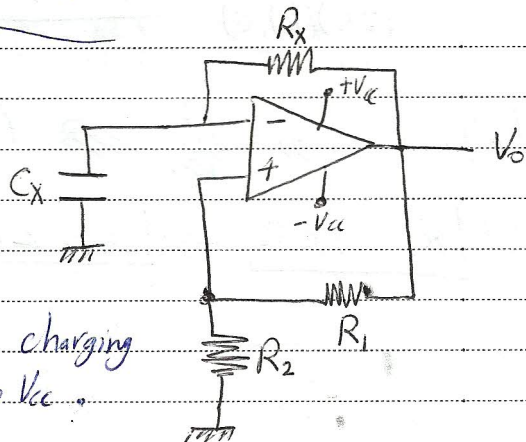


① When  $V_o = +V_{cc}$ ;

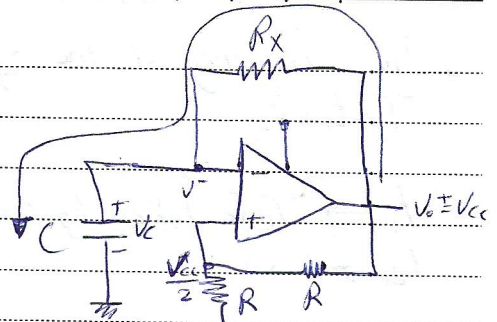
$$V^+ = \frac{V_{cc} R_2}{R_1 + R_2} \quad (\text{if } R_1 = R_2)$$

$$\Rightarrow V^+ = \frac{V_{cc}}{2}$$

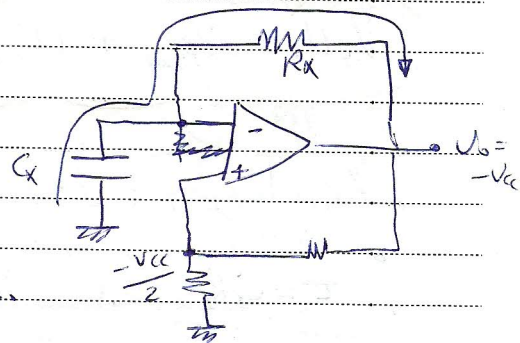
• The cap.  $C_x$  start charging through  $R_x$  aiming to  $V_{cc}$ .



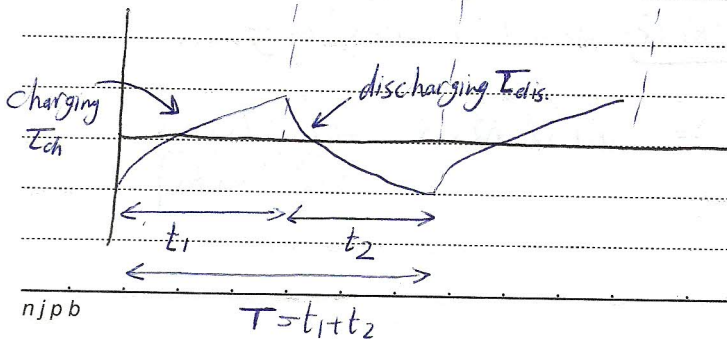
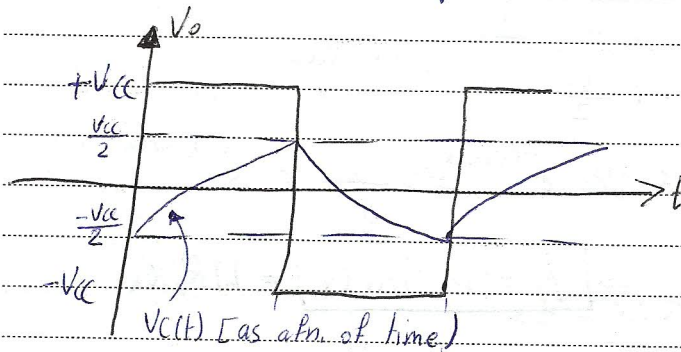
• But when  $V_c$  exceed  $\frac{V_{cc}}{2}$   
 then  $V^- \rightarrow V^+$  and the  
 Comparator change the state  
 and gives  $V_o = -V_{cc}$



• Now when  $V_o = -V_{cc}$ ,  $V^- = -\frac{V_{cc}}{2}$   
 and  $C_x$  will discharging through  
 $R_x$  aiming to  $-V_{cc}$  but when  
 $V_c$  exceed  $-\frac{V_{cc}}{2}$ , the Comp.  
 will change the state  
 and gives  $V_o = +V_{cc}$



∴ The cct will be repeated...



$$T = t_1 + t_2$$





\* Monostable (MMTV) :- (one shot ckt) :-

① When  $V_0 = +V_{CC}$

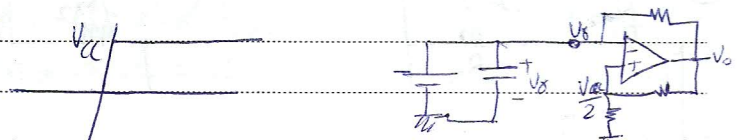
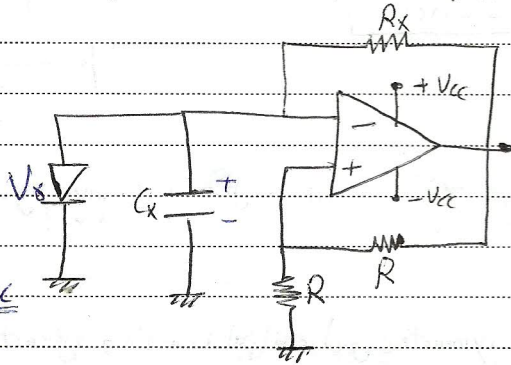
$$V^+ = \frac{V_{CC}}{2}$$

$C_x$  will start charging aiming  $V_{CC}$  but when  $V_c = V_x$ ,

The diod will be on so

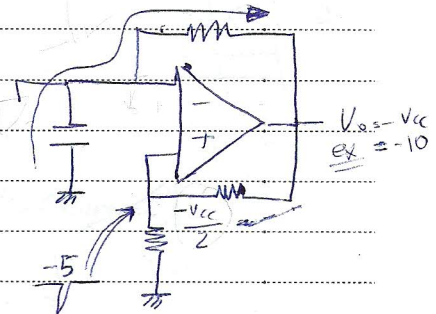
$V_c = V_x$  and if  $\frac{V_{CC}}{2} > V_x$  i.e.  $(V^+ > V^-)$ , the output stay at  $+V_{CC}$  and the ckt remains in this state.

i.e.  $V_0 = +V_{CC}$



② if a  $-V_e$  Trigger is applied at  $\ominus$  terminal such that to make  $V^+ < V_x$ . The comparator will change the state and make  $V_0 = -V_{CC}$  (i.e.  $V^+ = -\frac{V_{CC}}{2}$ )

③ the Cap.  $C_x$  will discharge through  $R_x$  aiming  $-V_{CC}$  but when  $V_c$  try to exceed  $-V_{CC}$  the Comp. change the state  $V_0 = +V_{CC}$  & The cycle will be repeated. if we applied another  $-V_e$  triggure otherwise the output will be  $+V_{CC}$  ...

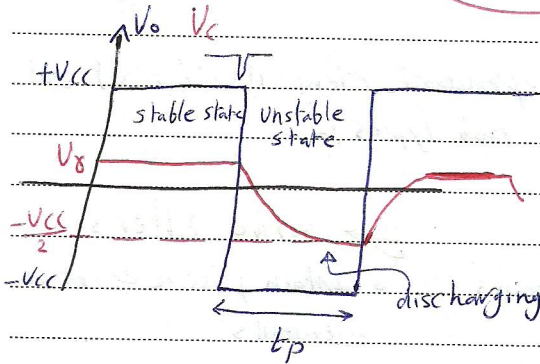


-ve Triggure انا كانه  $V^+ < V_x$   
 (  $V_x = \frac{V_{CC}}{2}$  )  $V^+ < V_x$

يعني لو عصبت  $V$  مقارنتها  $-1$  Volt  
 / ح تعني  $V^+ = 4$  لسا  $V^+ > V_x$  انا لا يعطيه  $-5$   
 / ح  $V = 0$   $V^+ < 0 < V_x$  ح يتكبر ال Comp



عشان نستعمل ال comp. 0 ام 1 يكون  $V^+ < V^-$  او  $V^+ > V^-$  و  $V^+$  و  $V^-$  هيا +ve trigger و -ve trigger  
 ال  $V^-$  كارج زيدي لا ياربوط مع diode و ال voltage هيا ثابت زي  $V_0$   
 و ال  $V^+$  و  $V^-$  هيا -ve trigger و +ve trigger



\* The pulse duration ( $t_p$ ) can be found as follow:-

$$V_c(t) = V_f + (V_{in} - V_f) e^{-t/\tau}$$

when  $t = t_p$ ,  $V_c(t) = \frac{-V_{cc}}{2}$ ,  $V_{initial} = V_0$ ,  $V_f = -V_{cc}$

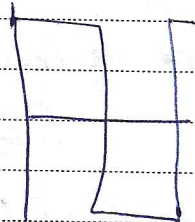
$$\frac{-V_{cc}}{2} = -V_{cc} + (V_0 + V_{cc}) e^{-t_p/\tau}, \text{ for } V_{cc} \gg V_0$$

$$\Rightarrow \frac{1}{2} = e^{-t_p/\tau} \Rightarrow t_p = \tau \ln 2$$

$$t_p = 0.69 R_x C_x$$

خروج ال pulse

$$\text{let } C_x = - \\ R_x = -$$



تغير ال output  
 بعد من هاي  
 عن طريق  
 $R_x, C_x$

$$P_{\text{output}} = P_{\text{trigger}}$$

عشان احصل على موجة كالموجة بـ (one trigger per cycle)

\* Active Filters :-

• Filters :- selective cts. allow certain bands of frequencies to pass (pass band) and reject other bands (stop band).

• It contain a freq. dependent elements (L or C) but In general there are two types :-

D. passive Filters

- have only passive elements
- No gain (max. gain is 1)
- No power supply.
- Suffer From loading.

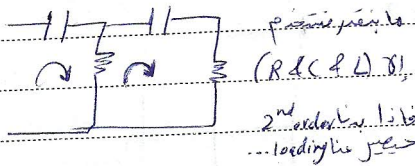
تفاضل  
كبيرة الحجم

Bulky and not integrable

Active filters

- contain passive & Active elements.
- there is a certain gain.
- power supply is required for biasing
- No loading affect
- Integrable...

(Buffers) passive

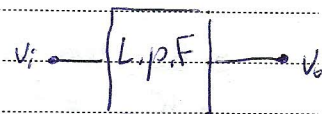


حداثة بكمية كبيرة  
IC's

According to frequency band, it can be classified as:-

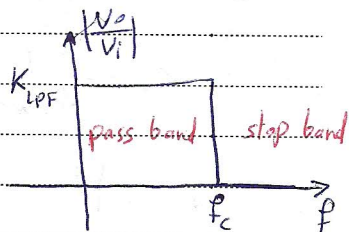
① Low pass Filter:-

- pass band extend from  $(0 \rightarrow f_c)$ , where  $f_c$ : cutoff frequency...



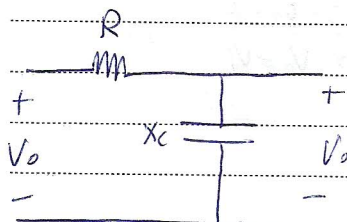
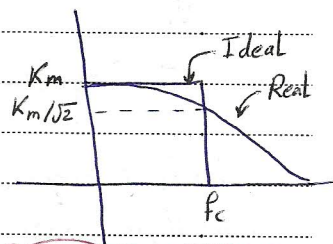
- $K_{LPF(max)} = 1$  For passive filters

- $K_{LPF(max)} > 1$  For Active filters



- $f_c$ : the freq. at which

$\frac{V_o}{V_i} = \frac{K_m}{\sqrt{2}}$ , where  $K_m = |V_o/V_i|_{max}$



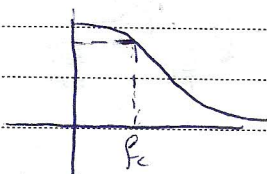
كل الترددات الأقل من  $f_c$  يمر  
الإشارة أما  $f_c$  فما فوق لا يمر

$X_c = \frac{1}{2\pi f c}$  ,  $V_o = \frac{V_i X_c}{X_c + R}$

when  $f = 0 \Rightarrow X_c = \infty \Rightarrow V_o = V_i \Rightarrow \frac{V_o}{V_i} = 1$

when  $f = \infty \Rightarrow X_c = 0 \Rightarrow V_o = 0 \Rightarrow \frac{V_o}{V_i} = 0$

∴ L.P.F



$\frac{V_o}{V_i} = \frac{1}{\sqrt{2}}$  at  $f = f_c$

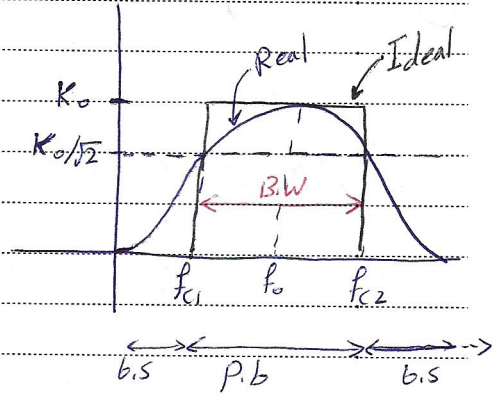


③ Bandpass filter (B.p.F.)

- Freq. Range  $f_{c1} \rightarrow f_{c2}$   
 $B.W = f_{c2} - f_{c1}$

- It has a center freq. ( $f_0$ ) related to B.W by selectivity

$$Q = \frac{f_0}{B.W}$$

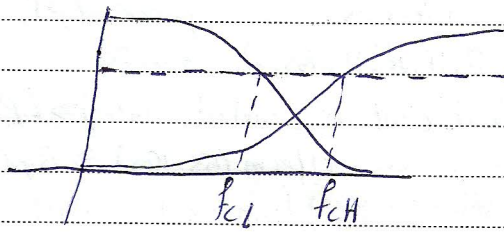


- B.p.F. can be constructed from cascading L.p.F. and H.p.F. such that

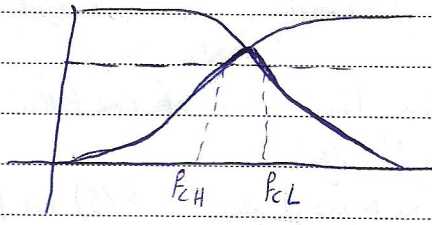
$$f_{cL} > f_{cH}$$

$$K_0 = \left| \frac{V_0}{V_i} \right|_{\omega = \omega_0}$$

$\omega < \omega_0$  (stop)  $\omega > \omega_0$  (stop)  
 $B.W \uparrow \rightarrow Q \downarrow$   
 $B.W \downarrow \rightarrow Q \uparrow$



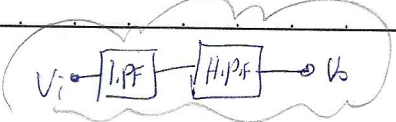
$$f_{cL} < f_{cH} \quad \text{B.p.F. case}$$



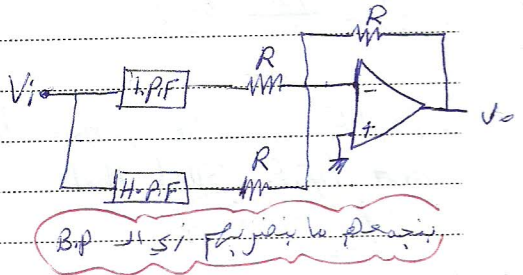
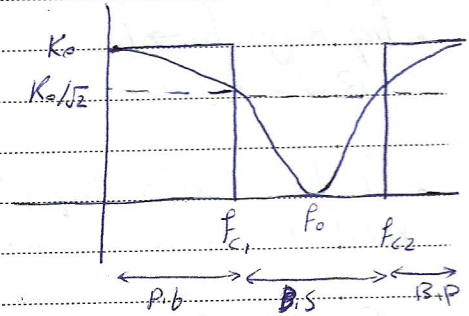
$$f_{cL} > f_{cH} \quad \text{(B.P.F.)}$$

- L.p.F max gain at  $\omega = 0$
- H.p.F " " "  $\omega = \infty$
- B.p.F " " "  $\omega = \omega_0 = 2\pi f_0$

njpb



④ Band stop or Band reject (B.S.F, B.R.F) :-



\* Filter transfer fn. :-  $H(s) = \frac{V_o(s)}{V_i(s)}$

$H(s) = \frac{N(s)}{D(s)}$  ;  $N(s)$  : Indicates filter response (L.P.F, H.P.F, B.P.F, B.S.F).

- (a) if  $N(s)$  contain constant (5, 10, 100)  $\Rightarrow$  L.P.F
- (b) " " " (s) term (5s, 10s)  $\Rightarrow$  B.P.F
- (c) " " " (s<sup>2</sup>) term (10s<sup>2</sup>)  $\Rightarrow$  H.P.F
- (d) " " " (constant + s<sup>2</sup>) term  $\Rightarrow$  B.S.F

(Constant + s)  $\Rightarrow$  L.P. + B.P.  $\Rightarrow$  B.S.F

$D(s)$  : Indicates the order of the filter (1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>) order.  
order: the highest power of (s) in  $D(s)$

ex Indicates the order of  $D(s)$ :

(1)  $D(s) = s^2 + 2s + 1$  : 2<sup>nd</sup> order

(2)  $D(s) = s^3 + 2s^2$  : 3<sup>rd</sup> order

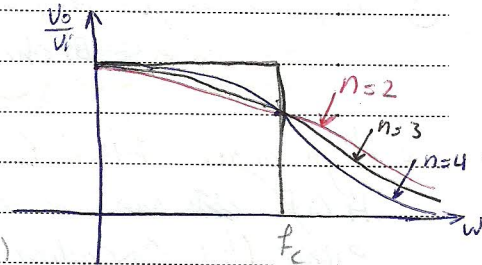
Ex Identify type and order of the following Filter T.F.:-

$H(s) = \frac{5s^2 + 3}{2s^2 + 5s + 1}$  (2<sup>nd</sup> order) (B.P.F.)

$H(s) = \frac{\sqrt{2}s}{s^3 + 2s^2 + 1.5s}$  =  $\frac{\sqrt{2}}{s^2 + 2s + 1.5}$  (2<sup>nd</sup> order) (L.P.F.)

\* Filter's order :-

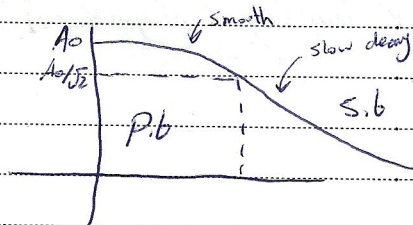
• As filter order  $n$  inc<sup>r</sup>,  
the response will be  
~~close~~ closer to ideal  
response but at the  
of filter complexity. shp 36



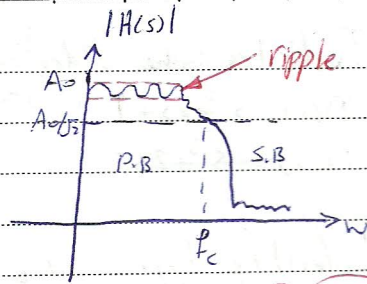
• According to filter response there are two types:-

(1) Butterworth Response:-

Smooth pass band but  
slow decay...



- ② chebyshev response :-  
 Not smooth resp. in p.B.  
 (there is a ripple in p.B.)  
 but it has a sharp decay  
 in s.B.



خود را از جواب ال Ideal

- ① realization: A) passive  
 B) Active

خود را از جواب ال sharp  
 (Butterworth) smooth  
 cutoff را می توانه ال

- ② Freq. range: A) L.P.F.  
 B) H.P.  
 c) B.P d) B.S

- ③ response shape: - A) Butterworth  
 B) chebyshev

\* High order filter realization: -

H.O.F. can be realised  
 either (by cascading 2<sup>nd</sup> order  
 and 1<sup>st</sup> order) or (using a certain  
 configuration such as follow  
 the ladder config. (FLF)  
 or leapfrog configurations)

Cascade 2<sup>nd</sup> + 2<sup>nd</sup> = 4<sup>th</sup> order  
 Cascade 2<sup>nd</sup> + 1<sup>st</sup> = 3<sup>rd</sup> order  
 order سی می تونه  
 1<sup>st</sup> 2<sup>nd</sup> cascade  
 ال order فرقی او  
 ال order ال 2<sup>nd</sup>

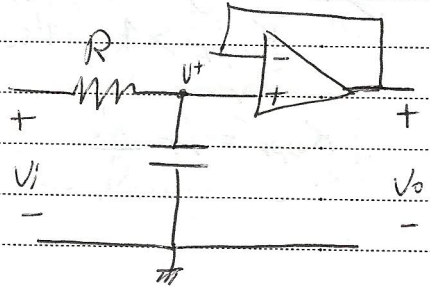


\* 1<sup>st</sup> order Filter (one pole)

① L.P.F :-

A) Unity gain

$$V^+ = V_0 = \frac{V_i \frac{1}{sC}}{R + \frac{1}{sC}}$$



$$\frac{V^+}{V_i} = \frac{1}{1 + sRC} ; s = j\omega, V^+ = V_0 \text{ (buffer)}$$

$$\frac{V_0}{V_i} = T(s) = \frac{1}{1 + sRC} \Rightarrow \text{For } s=0 \Rightarrow |T(s)| = 1$$

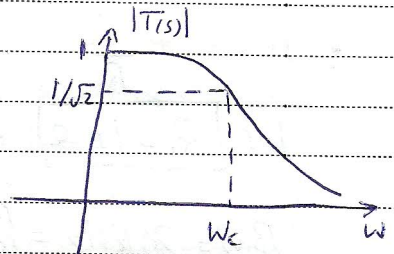
$$\text{For } s=\infty \Rightarrow |T(s)| = 0$$

⇒ L.P.F

$\omega_c \rightarrow$  Freq. at which  $|T(s)| = \frac{K_{OLPF}}{\sqrt{2}}$

$$|T(s)| = \frac{1}{\sqrt{1^2 + (\omega RC)^2}}$$

$$\text{at } \omega = \omega_c \Rightarrow |T(s)| = \frac{1}{\sqrt{2}}$$

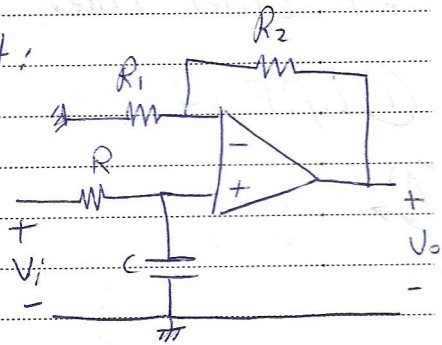


$$\Rightarrow 1 + \omega_c^2 R^2 C^2 = 2 \Rightarrow \omega_c^2 = \frac{1}{R^2 C^2} \Rightarrow \boxed{\omega_c = \frac{1}{RC}}$$

$$\Rightarrow f_c = \frac{1}{2\pi RC}$$

B) For gain  $> 1$  ;  
 $K_{OLPF} > 1$  ; Use this cct:

$$K_{OLPF} = 1 + \frac{R_2}{R_1}$$



Ex. Design a first order L.P.F. with a gain of 20dB and a bandwidth of (20) KHz ?

$$\bullet K(\text{dB}) = 20 \log \frac{V_o}{V_i} \Rightarrow 20 = 20 \log \left( \frac{V_o}{V_i} \right)$$

$$\Rightarrow \log \left( \frac{V_o}{V_i} \right) = 1 \Rightarrow \boxed{\frac{V_o}{V_i} = 10 = |T(s)|}$$

$$\bullet 10 = 1 + \frac{R_2}{R_1}$$

$$\text{let } \boxed{R_1 = 1 \text{ K}\Omega} \Rightarrow \boxed{R_2 = 9 \text{ K}\Omega}$$

$$\bullet \text{B.W.} = 20 \text{ KHz} = f_c ; f_c = \frac{1}{2\pi RC}$$

$$\text{let } \boxed{C = 0.001 \mu\text{F}} \Rightarrow R = \frac{1}{(2\pi)(2 \times 10^4)(0.01 \times 10^{-6})} = \boxed{800 \Omega}$$

\* Note:

(Unity gain)  $\equiv$  (zero dB)  $\equiv$  (max gain = 1)

② High pass filter :-

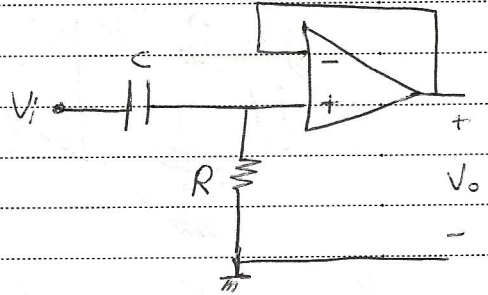
obtained by changing ~~each~~ each (R by C) & each

(C by R) transformation

A) Unity gain :-

$$f_c = \frac{1}{2\pi RC}$$

$$V^+ = V_o ; \quad V^+ = \frac{V_i R}{R + \frac{1}{sC}}$$



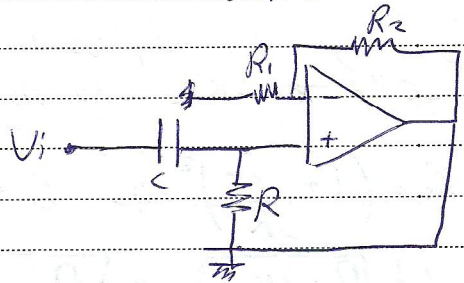
$$\Rightarrow \frac{V_o}{V_i} = \frac{sCR}{1 + sCR} ; \quad \text{When } s = \infty \Rightarrow |T(s)| = 1$$

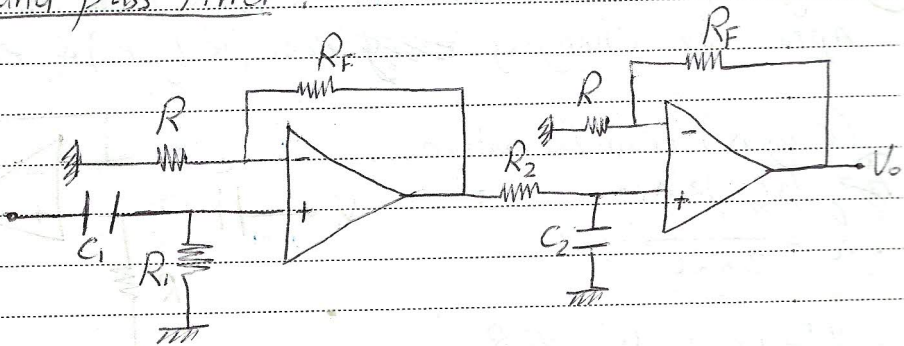
$$\text{When } s = 0 \Rightarrow |T(s)| = 0$$

∴ H.P.F

B) For gain  $> 1$ , use resistors in the buffer :-

$$K_{\text{HP.F}} = \left(1 + \frac{R_2}{R_1}\right)$$



③ Band pass filter:-

$$\bullet K_{OBPF} = K_{OLPF} \cdot K_{OHPF}$$

$$= \left(1 + \frac{R_F}{R}\right)^2$$

$$\bullet f_{CL} > f_{CH}$$

$$\bullet f_{CL} = \frac{1}{2\pi R_2 C_2}$$

$$\bullet f_{CH} = \frac{1}{2\pi R_1 C_1}$$

Ex. Design a band pass to have B.W. Ranging from 20 Hz  $\rightarrow$  20 kHz and max. gain of 25?!

$$\bullet K_o = \left(1 + \frac{R_F}{R}\right)^2 \Rightarrow 5 = 1 + \frac{R_F}{R} \Rightarrow \frac{R_F}{R} = 4$$

$$\text{let } \boxed{R = 1\text{ k}\Omega} \Rightarrow \boxed{R_F = 4\text{ k}\Omega}$$

$$\bullet \text{For H.P.F } f_{CH} = 20\text{ Hz}, f_{CH} = \frac{1}{2\pi R_1 C_1} = 20\text{ Hz}$$

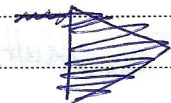
$$\text{let } C_1 = 1\text{ }\mu\text{F} \Rightarrow R_1 = \frac{1}{(2\pi)(1 \times 10^{-6})(20)} = \boxed{8\text{ k}\Omega}$$

• For L.P.F  $f_{c1} = 20\text{KHz} \Rightarrow 20 \times 10^3 = \frac{1}{2\pi R_2 C_2}$

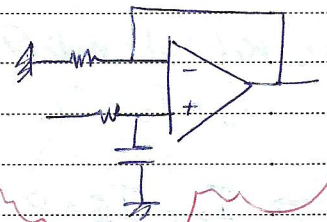
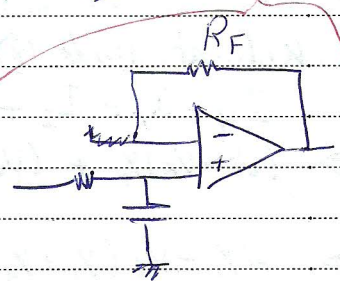
let  $C_2 = 0.01\mu\text{F} \Rightarrow R_2 = \frac{1}{2\pi (20 \times 10^3)(0.01\mu)} = 800\Omega$

\*Note:-

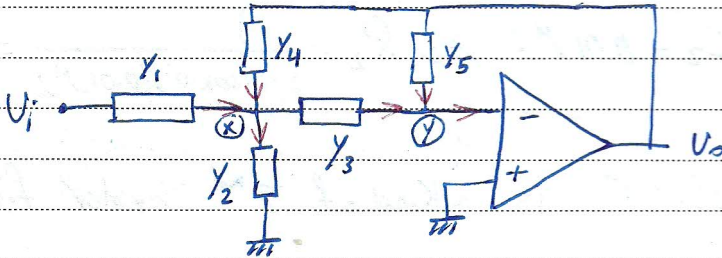
The B.P.F is a kind of 2<sup>nd</sup> order filters...



These 2  
op-Amp's  
are buffers  
not Amplifiers  
i.e. gain = 1



\* Second order filters:- (Two poles)



"General 2<sup>nd</sup> order Filter"

• MLNFB (Multiple loop Negative feedback)

• Kcl at node (X) :-

$$I_4 + I_1 = I_2 + I_3$$

$$\Rightarrow (V_i - V_x)Y_1 + (V_o - V_x)Y_4 = Y_2 V_x + (V_x - V^-)Y_3$$

$$\Rightarrow V_i Y_1 - V_x (Y_1 + Y_4 + Y_2 + Y_3) + V_o Y_4 + V^- Y_3 = 0 \quad \dots \textcircled{1}$$

• Kcl at node (Y) :-

$$I_3 + I_5 = I_{in} ; I_{in} = 0 \text{ for Ideal Amp. } (V^- = 0 \text{ (V.G.)})$$

$$\Rightarrow I_3 + I_5 = 0 \Rightarrow (V_x - V^-)Y_3 + (V_o - V^-)Y_5 = 0$$

$$\Rightarrow V_x = \frac{-Y_5}{Y_3} V_o \quad \dots \textcircled{2}$$

sub ② in ① :-

$$V_o Y_4 + V_o \frac{Y_5}{Y_3} (Y_1 + Y_2 + Y_3 + Y_4) = -V_i Y_1$$

$$V_o (Y_3 Y_4 + Y_5 Y_1 + Y_5 Y_2 + Y_5 Y_3 + Y_5 Y_4) = -V_i Y_1 Y_3$$

$$\Rightarrow \frac{V_o}{V_i} = T(s) = \frac{-Y_1 Y_3}{Y_3 Y_4 + Y_5 (Y_1 + Y_2 + Y_3 + Y_4)}$$

∴ This ckt can be used to realize 2<sup>nd</sup> order L.P.F, H.P.F, B.P.F according to the type of  $Y_1, Y_2, Y_3, Y_4, Y_5$  either resistor or capacitor...

① To realize L.P.F by MLNFB :-

$$T(s) \text{ of L.P.F} = \frac{K_1}{s^2 + K_2 s + K_0} = \frac{-Y_1 Y_3}{Y_3 Y_4 + Y_5 (Y_1 + Y_2 + Y_3 + Y_4)}$$

$$\Rightarrow Y_1 = G_1, Y_3 = G_3, Y_4 = G_4, Y_5 = sC_5$$

$$Y_2 = sC_2$$

$$\Rightarrow T(s) = \frac{-G_1 G_3}{G_3 G_4 + sC_5 (G_1 + G_3 + G_4) + s^2 C_2 C_5}$$

$$\therefore T(s) = \frac{-G_1 G_3}{C_2 C_5} \cdot \frac{1}{s^2 + \frac{G_1 + G_3 + G_4}{C_2} s + \frac{G_3 G_4}{C_2 C_5}}$$

I.P.F  
2<sup>nd</sup> order

$$\bullet K_{olpf} = |T(s)|_{\substack{\omega=0 \\ s=0}}$$

$$\Rightarrow K_{olpf} = \frac{G_1 G_3}{C_2 C_5} \cdot \frac{C_2 C_5}{G_3 G_4} = \frac{G_1}{G_4} = \frac{R_4}{R_1}$$

• Compare (1) with standard 2<sup>nd</sup> order sys. equation.

$$\overline{T(s)} = \frac{K}{s^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$

$\omega_0$  represents:-

- ① cut off freq. ( $f_c$ ) for H.P.F. and L.P.F.
- ② center freq. ( $f_0$ ) for B.P.F.

$$\Rightarrow \omega_0^2 = \frac{G_3 G_4}{C_2 C_5} = \frac{1}{R_3 R_4 C_2 C_5}$$

$$\Rightarrow f_c = \frac{1}{2\pi \sqrt{R_3 R_4 C_2 C_5}} \quad \text{cut off freq. of L.P.F}$$

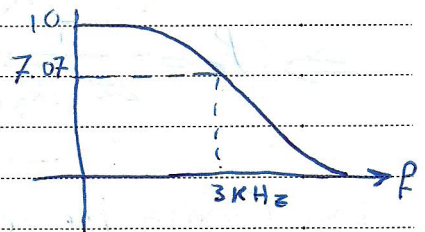


Ex. Design 2<sup>nd</sup> order LPF to have max. gain of 10 and cut off freq. of 3 kHz, plot frequency response?

$$K_o = \frac{R_4}{R_1} = 10, \text{ let } \boxed{R_1 = 1 \text{ k}\Omega} \Rightarrow \boxed{R_4 = 10 \text{ k}\Omega}$$

Use equal. Cap. design,  $C_2 = C_5 = C = 0.01 \mu\text{F}$ .

$$f_o^2 = \frac{1}{4\pi^2 R_3 R_4 C_2 C_5} \Rightarrow R_3 = \frac{1}{4 \times \pi^2 \times 9 \times 10^6 \times 10^4 \times 10^{-16}} = \boxed{2.8 \text{ k}\Omega}$$



② To Redize 2<sup>nd</sup> order H.P.F

Choose  $Y_1 = C_1, Y_3 = C_3, Y_4 = C_4, Y_2 = G_2, Y_5 = G_5$

(oR From  $C \rightarrow R, R \rightarrow C$ ) transformation

$$T(s) = \frac{-C_1 C_3 s^2}{C_3 C_4 s^2 + G_5 (C_1 + C_3 + C_4) s + G_5 G_2}$$

$$= \frac{-\frac{C_1 C_3}{C_3 C_4} s^2}{s^2 + \frac{G_5 (C_1 + C_3 + C_4)}{C_3 C_4} s + \frac{G_5 G_2}{C_3 C_4}}$$

• Compare  $T(s)$  with standard 2<sup>nd</sup> sys. equation...

$$K_{0HPF} = |T(s)|_{\omega \rightarrow \infty} \Rightarrow S = \infty$$

$$\Rightarrow K_{0HPF} = \frac{C_1 C_3}{C_3 C_4} = \frac{C_1}{C_4}$$

لو باني، باني، باني  
equal cap.

design ال  
gain=1 ال

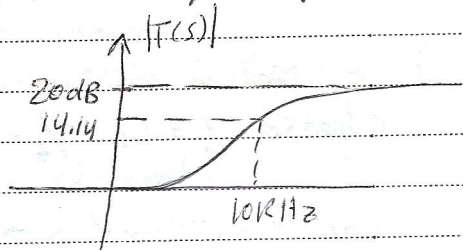
$$\omega_0^2 = \frac{1}{R_5 R_2 C_3 C_4}$$

$$\Rightarrow P_c = \frac{1}{2\pi \sqrt{R_5 R_2 C_3 C_4}}$$

Ex. Design the ckt to give The freq. response shown:-

$$20 = 20 \log_{10} K_0$$

$$\Rightarrow K_0 = 10$$



$$\frac{C_1}{C_4} = 10, \text{ let } C_1 = 10 \mu\text{F} \Rightarrow C_4 = 1 \mu\text{F}$$

$$\text{let } R_5 = R_2 = 1 \text{ k}\Omega \Rightarrow C_3 = \frac{1}{4\pi^2 f_c^2 R_5 R_2 C_4}$$

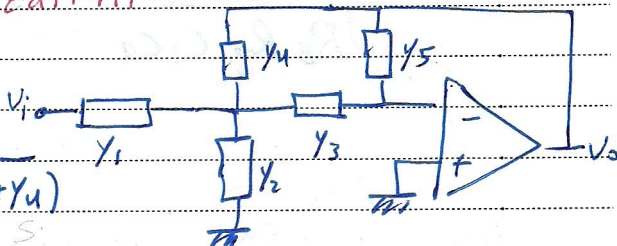
$$= \frac{1}{4\pi^2 (10 \times 10^3)^2 (10^6) (1 \times 10^{-6})}$$

$$= 253.3 \text{ pF}$$

10dB =  $T(s)$  ال  
 $C_1 = C_4$  gain=1 ال

③ For B.P.F Relization:-

$$T(s) = \frac{G_5}{Y_3 Y_4 + Y_5 (Y_1 + Y_2 + Y_3 + Y_4)}$$



•  $Y_1$  or  $Y_3$  must be cap.

$Y_1 = G_1, Y_3 = SC_3, Y_4 = SC_4, Y_2 = G_2, Y_5 = G_5$

$$\Rightarrow T(s) = \frac{-G_1 SC_3}{S^2 C_3 C_4 + G_5 (G_1 + G_2) + SG_5 (C_3 + C_4)}$$

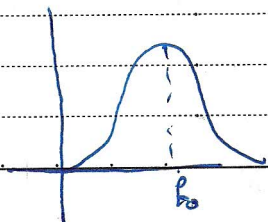
$$\Rightarrow T(s) = \frac{-\frac{G_1}{C_4} S}{S^2 + \frac{G_5 (G_1 + G_2)}{C_3 C_4} + S \frac{G_5 (C_3 + C_4)}{C_3 C_4}}$$

• Compare to standard 2nd order sys. eq<sup>n</sup>

$$H(s) = \frac{Ks}{S^2 + \frac{\omega_0}{Q} S + \omega_0^2}$$

$$\begin{aligned} \text{p.o. } \omega_0^2 &= \frac{G_5 (G_1 + G_2)}{C_3 C_4} = \frac{\left(\frac{1}{R_1} + \frac{1}{R_2}\right)}{R_5 C_3 C_4} = \frac{R_1 R_2}{R_5 C_3 C_4} \\ &= \frac{R_1 R_2}{R_5 C_3 C_4 (R_1 // R_2)} \end{aligned}$$

$\text{p.o. } \omega_0^2 = \frac{1}{R_5 C_3 C_4 R_{eq}}$



$$\Rightarrow \omega_0 = \frac{1}{\sqrt{R_5 R_{eq} C_3 C_4}} \Rightarrow f_0 = \frac{1}{2\pi \sqrt{R_5 R_{eq} C_3 C_4}}$$

$f_0$ : center freq.

$$\bullet \frac{\omega_0}{Q} = \frac{C_3 + C_4}{R_5 (C_3 C_4)} = \text{B.W (band width of filter)}$$

$$\bullet Q = \frac{Q}{\omega_0} \omega_0 = \frac{R_5 (C_3 C_4)}{C_3 + C_4} \cdot \frac{1}{\sqrt{R_5 R_{eq} C_3 C_4}}$$

$$= \frac{\sqrt{R_5 C_3 C_4}}{(C_3 + C_4) \sqrt{R_{eq}}}$$

$$\bullet K_{\text{B.P.F}} = |T(s)|_{\omega=\omega_0}$$

$$= \frac{K Q}{\omega_0}$$

$$= \frac{G_1}{C_4} \cdot \frac{C_3 + C_4}{R_5 (C_3 C_4)} \frac{R_5 C_3 C_4}{C_3 + C_4}$$

$$K_{\text{B.P.F}} = \frac{R_5 C_3}{R_1 (C_3 + C_4)}$$

$$\frac{Q}{\omega_0} + \frac{F}{F} = 1$$

"descent"  
have  
a Unit ✓

$$H(s) = \frac{K s}{s^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$

$$H(s)|_{\omega=\omega_0} = \frac{K s}{(j\omega_0)^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$

$$= \frac{K \omega_0}{-\omega_0^2 + \frac{\omega_0}{Q} \omega_0 + \omega_0^2}$$

$$= \frac{K Q}{\omega_0}$$

• For equal Cap. design ( $C_3 = C_4 = C$ ):

$K_{0BPF} = \frac{R_5}{2R_1}$  ← (20)

$f_0 = \frac{1}{2\pi C \sqrt{R_5 R_4}}$

$Q = \sqrt{\frac{R_5}{4R_4}}$  ← (21)

$\frac{1}{C \cdot R} = \frac{1}{R \cdot F} = f_{req.}$

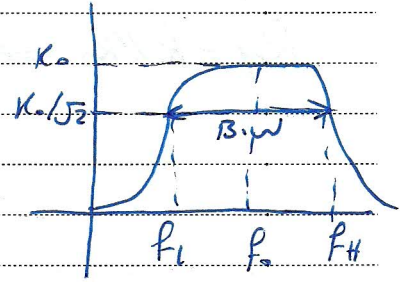
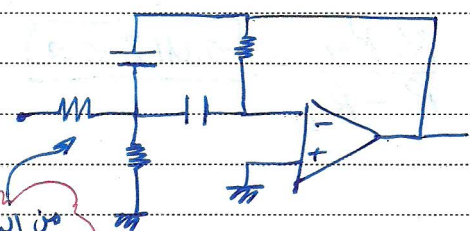
•  $f_0, Q, B.W$  are related by:-

$Q = \frac{f_0}{B.W}$  ; where  $f_H - f_L = B.W$

\* For symmetric response :-

$f_H = f_0 + \frac{B.W}{2}$

$f_L = f_0 - \frac{B.W}{2}$



من الـ input voltage  
العالية لا يتغير  
في تواتر (C)  
عند الـ  
input voltage...

Ex. Design a 2<sup>nd</sup> order B.P.F to give a center frequency,  $f_0 = 20$  KHz,  $Q = 10$ ,  $K = 20$  dB and sketch freq. response (bode plot) Use equal cap. design with  $C = 1$  nF P.P?

$$\bullet \frac{\omega_0}{Q} = \text{B.W} = \frac{C_3 + C_4}{R_5 C_3 C_4} = \frac{2C}{R_5 C^2} = \frac{2}{R_5 C}$$

$$\Rightarrow \frac{2\pi \times 20 \times 10^3}{10} = \frac{2}{10^{-9} R_5} \Rightarrow \boxed{R_5 = 159 \text{ K}\Omega}$$

$$\bullet 20 = K_{dB} = 20 \log K \Rightarrow \boxed{K_0 = 10}$$

$$\bullet K_0 = \frac{R_5}{2R_1} \Rightarrow 10 = \frac{159}{2R_1} \Rightarrow \boxed{R_1 = 7.95 \text{ K}\Omega}$$

$$\bullet Q^2 = \frac{1}{4} \frac{R_5}{R_{eq}} \Rightarrow R_{eq} = \frac{R_5}{4Q^2} = \frac{159}{400} = \boxed{0.397 \text{ K}\Omega}$$

$$R_{eq} = R_1 // R_2 \Rightarrow R_2 = \frac{R_1 R_{eq}}{R_1 - R_{eq}} = \boxed{0.117 \text{ K}\Omega}$$

$$\bullet B.W = \frac{f_o}{Q} = \boxed{2 \text{ KHz}}$$

$$\bullet f_H = f_o + 1 \text{ KHz} = \boxed{21 \text{ KHz}}$$

$$\bullet f_L = f_o - \frac{B.W}{2} = \boxed{19 \text{ KHz}}$$

