



تقدم لجنة EiCoM الاكاديمية

دفتر لمادة:

# آلات كهربائية

جزيل الشكر للطالبة:

## لجين ابو غزالة



ELECTRICAL

MACHINERY

8-6-2014, 9-6-2014 sheet

12-7-2014

2.9 → self study

No.

# 1 Introduction to machinery Principles

## 1.1 Electrical

Machines transformers and daily life.

electrical machine: is a device that convert mechanical energy to electrical energy or electrical energy to mechanical energy.

⊕ motor → convert electrical energy to mechanical energy.

⊖ generator → convert mechanical energy to electrical energy.

when an electrical machine can convert power in either direction it can be used either a generator or a motor.

المشغول → it convert energy from one form to another due to the action of magnetic field  $\Sigma$  الحثية  $\Sigma$  الحثية

\* transformer → convert electrical energy at one level to another level. it work operates on the same way principle as motor and generator due to the action of the magnetic field.

\* Why electrical motor and generator are common??

Power is clean and electrical efficiency is easy to transmit over long distance and easy to control, does not required fuel.

دوولسا كرايين سننلرا ، ال transformer aid ال lossess وبتقل

ال transformer استعمال ال



1.3 Rotational motion, Newton's Law and Power Relations: -

→ All electrical machine rotate about an axis is called the shaft of the machine.

machine normally turn on a fixed shaft. so their rotation is restricted to one angular dimension. Relative to the given end of the machine shaft the rotation can be

CCW (counterclockwise) → positive.

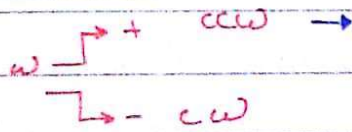
CW (clockwise) → negative.

The major concept of angular motion: -

1) Angular Position  $\theta$  measured from a reference point in degree or radian. *personal or random.*

2) Angular velocity  $\omega$  is the rate at change in angular position with respect to time.

$$\omega = \frac{d\theta}{dt}$$



$\theta$  → radian → radian/second.

$\omega_m$  → angular velocity expressed in radian/sec

$f_m$  → angular velocity expressed in revolutions/sec

$n_m$  → angular velocity expressed in revolutions/min

*m → it indicates mechanical quantities*

*طابع ميكانيكي*

*دور في الدقيقة*

$$\begin{aligned} n_m &= 60 f_m \\ f_m &= \frac{\omega_m}{2\pi} \end{aligned}$$

$$n_m = \frac{60 \omega_m}{2\pi}$$

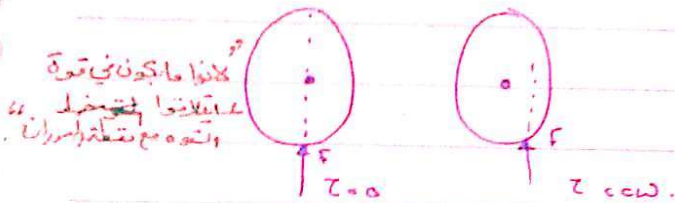
العلاقة ←



3) Angular acceleration is the rate of change in velocity in respect to time.

→ + if the angular speed is increasing in an algebraic sense

$$\alpha = \frac{d\omega}{dt} \quad \text{unit is radian/sec}^2$$



**Torque  $\tau$**  → Force to rotate an object about an axis.

→ Force applied to an object cause it velocity to change. When absence of force the velocity is constant, the more force is applied to move rapidly velocity change. the same when object is rotating the angular speed is constant when a torque is more the more rapidly the angular velocity change. [it is depended on the magnitude of applied force and the distance between the axis of rotation and the line of the action force]

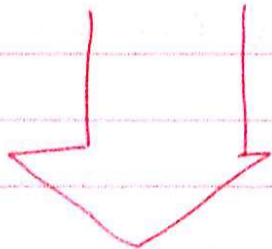
→ the torque is the product of the force applied to the object and the smallest distance between the line of the action force and the object's axis of rotation.

$$\tau = rF \sin\theta$$

المسافة الزاوية

→ angle between vector  $r$  and vector  $F$ .

Newton's law of Rotation  $F = ma \rightarrow m/s^2 / \text{ft}/s^2$



Newton kilograms  
pounds slugs

$I$  moment of inertia [kilograms-meter<sup>2</sup> or slug-foot<sup>2</sup>]

$$\tau = J \alpha \rightarrow \text{angular acceleration [rad/s]}$$

net applied torque [foot-pound-foot]

**Work**

application of force through distance.

$$W = \int f ds$$

$$W = \int T d\theta$$

Tolues or foot-pound.

$$W = Fr$$

$$W = T\theta$$

work rotational.

**Power**

rate at ~~the~~ doing work

$$P = \frac{dW}{dt}$$

$$= Fv$$

[power]

watts horse power

foot-pound / second.

$$P_{\text{horse}} = T\omega$$

velocity

$$\text{power horse} = 746 \text{ kW}$$

$$1 \text{ kW} = 1.34 \text{ hp}$$

#### 1.4 The Magnetic Field:

تيار يولد مجالاً مغناطيسياً بالحقبة

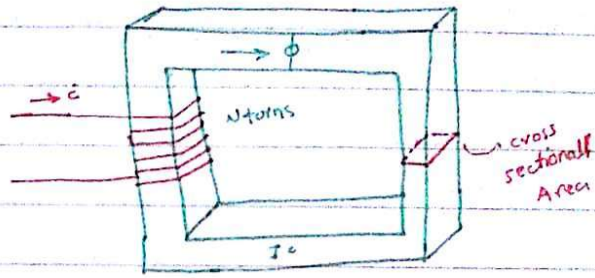
- time changing magnetic field induces a voltage coil of wire if it passes through that coil [This is the transformer action].  $\text{emf} = -\frac{d\phi}{dt}$  إذا كان بداراً مغناطيسياً يولد تياراً
- A current-carrying wire in the presence of magnetic field has a force induce on it [This is the basis of motor action].  $F = (\vec{I} \times \vec{B})$
- A moving wire in the presence of magnetic field has a voltage induced in it [This is the basis of generator action].  $\vec{E} = (\vec{v} \times \vec{B})$  إذا كان بداراً مغناطيسياً يولد تياراً



Production of magnetic field:

$$\oint H \cdot dI = I_{net}$$

$\downarrow$  magnetic field intensity  
 $\downarrow$  length  $dl$



$$H I_c = N i$$

$$H = \frac{N i}{I_c}$$

$$B = \mu H$$

$\downarrow$  magnetic flux density

$\mu$  permeability of material

magnetic motive force =  $N I$

عن الكلف بالتيار

بالتالي  
 ينشأ تدرج مغناطيسي ( $\phi$ ) نتيجة مرور التيار في الملف  
 الشحنة

لحساب الجهد الكهربائي  
 التيار

$$\phi = \frac{\text{mmf}}{R}$$

$$R \text{ (Reluctance)} = \frac{L}{\mu A}$$

$\downarrow$  طول الملف  
 $\downarrow$  permeability  
 $\downarrow$  مساحة المقطع العرضي

[A.turns. / wp]

$$\frac{A \cdot \text{turns} \cdot H}{m}$$

$$\frac{A \cdot \text{turns} \cdot H \cdot L}{m}$$

magnetic field strength [intensity]:  $H = \text{mmf} / L$  [K/m]

magnetic Flux density =  $B = H \cdot \mu$  [T weber] [wp/m<sup>2</sup>]

Flux =  $B \cdot A$  [wp] if flux density constant,  $\propto LA$

$$\mu \text{ (permeability)} = \mu_{relative} \cdot \mu_{free}$$

$\downarrow$  relative permeability  
 $\downarrow$  permeability of free space  $4\pi \times 10^{-7}$

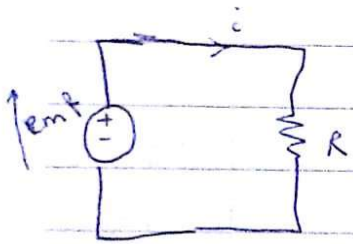
[Heres / m]



If we say that the steel has a ~~permeability~~ permeability of 2000 to 6000 or more <sup>2000 to 6000 times</sup> more flux is established in a piece of steel than an corresponding area of air.

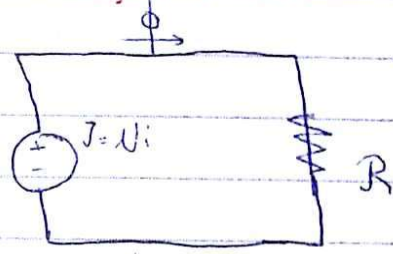
وكلما زاد، المتانة، المغناطيسية مادة يكون، الفيض، أكبر  
 مغناطيسية كبيرة يكون مغناطيسية، المواد عتاد حديد مقدار Flux بدسوا جدا، وكما ان يكون انقل  
 في اختيار المادة بشكل عامل رئيسي، بزيادة او تقليل المجال داخل الملف (core)

Electrical ckt



$I = \frac{V}{R}$  ينشأ تيار يقاس  
 التيار هو تارة فقط للاكثونات

magnetic ckt



$\phi = \frac{J}{R}$

$J \text{ (mmf)} = Ni$  [Amperes-turns] <sup>inductor من صور التيار في ال inductor</sup>

$\rho \text{ (permeance)} = \frac{1}{\mu}$

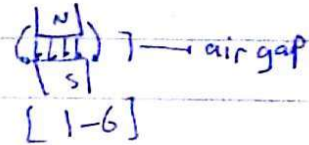
$\phi = Ni \rho$

\* Reluctance obey the same rule of resistance  
 parallel Reluctance =  $\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots$   
 series combination =  $R_1 + R_2 + R_3 \dots$

\* permeance obey the same rule of conductances.

: بعبارة أخرى

1 small flux escapes from the core into surrounding air - low permeability -  
this flux called leakage flux. [1-6]



2 - If there is air gaps in the flux path in a core, the effective cross sectional area of the flux is bigger than the cross sectional area of the iron core  
air gap

it cause by the ~~the~~ fringing effect at the magnetic flux [1-6]

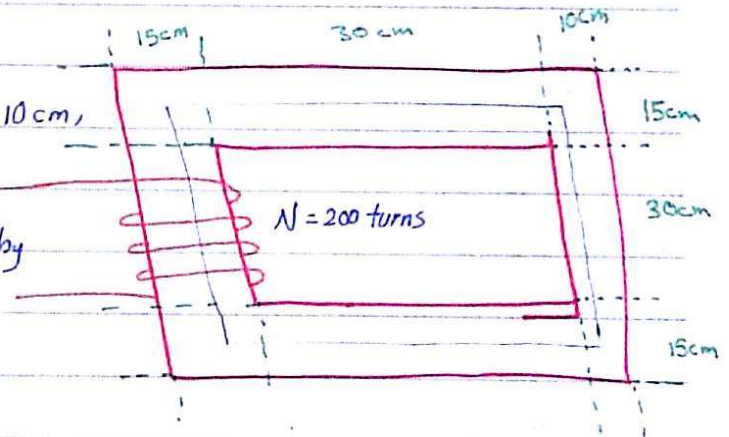
### Example 1-1

the depth of the core (in to the page) is 10 cm,

200 turns it wrapped around left side

$\mu_r = 2500$  how much flux produced by

1-A input current ??



Solution:

$$\phi = \frac{Ni}{R} \quad \text{or} \quad \frac{Ni}{\frac{L}{\mu_r \mu_0}}$$

$$L_1 = \frac{15}{2} + \frac{30}{2} + \frac{15}{2} = 0.45 \text{ m (total length)}$$

$$A_1 = 10 \times 10 = 0.01 \text{ m}^2$$

$$R_1 = \frac{L_1}{\mu_r \mu_0 A_1} = \frac{0.45}{2500 \times 4\pi \times 10^{-7} \times 0.01} = 14323.94 \text{ A.turns/wb}$$

$$L_2 = \left(\frac{15}{2} + \frac{10}{2} + 30\right) \times 2 + 45 = 130 \text{ cm} = 1.3 \text{ m}$$

$$A_2 = 15 \times 10 = 0.015 \text{ m}^2$$

$$R_2 = \frac{1.3}{0.015 \times 2500 \times 4\pi \times 10^{-7}} = 27586.8568 \text{ A.turns/wb}$$

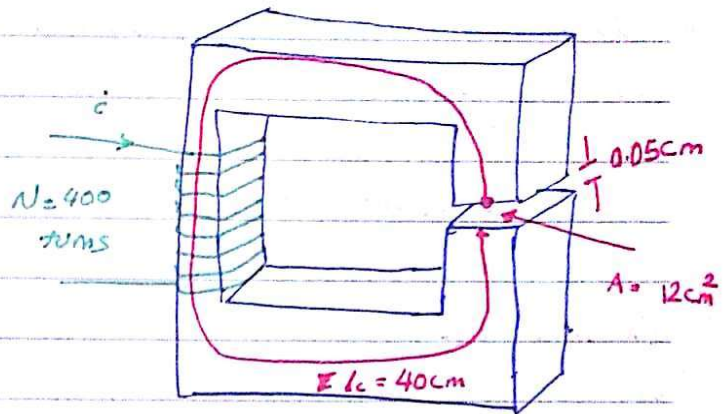


$$R = R_1 + R_2 = 41910.7968$$

$$\phi = \frac{1 \times 200}{41910.7968} = 4.772 \times 10^{-3} \text{ WP}$$

### Example 1-2:

mean path length 40cm, there are a small gap of 0.05cm. The cross sectional Area of the core is  $12 \text{ cm}^2$ , the relative permeability is 4000 and the coil of wire has turn 400.



Assume that the fringing in the air gap increases the effective cross sectional area of the air gap by 5 percent.

a) total reluctance of the flux

b) the current to produce a flux density of 0.5T in the air gap.

Solution:

$$R = \frac{l}{\mu A} \quad \phi = \frac{Ni}{R}$$

$$R_{\text{core}} = \frac{0.4}{4000 \times 4\pi \times 10^{-7} \times 12 \times 10^{-4}} = 66314.55962 \text{ A.turns/Wp}$$

$$R_{\text{air}} = \frac{0.05 \times 10^{-2}}{4\pi \times 10^{-7} \times [A]} \quad A = \left[ 12 \times 10^{-4} \times \frac{5}{100} \right] + 12 \times 10^{-4} = 1.26 \times 10^{-3}$$

$$= 315783.6172 \text{ A.turns/Wp}$$

$$R = 382098.1769 \text{ A.turns/Wp}$$



No.

$$\phi = B \cdot A$$

$$\phi = \frac{N\dot{i}}{R} \qquad \frac{N\dot{i}}{N} = \frac{B \cdot A \cdot R}{N}$$

$$I = \frac{B \cdot A \cdot R}{N} = \frac{0.5 * 1.26 * 10^{-3} * 382098.1769}{400}$$

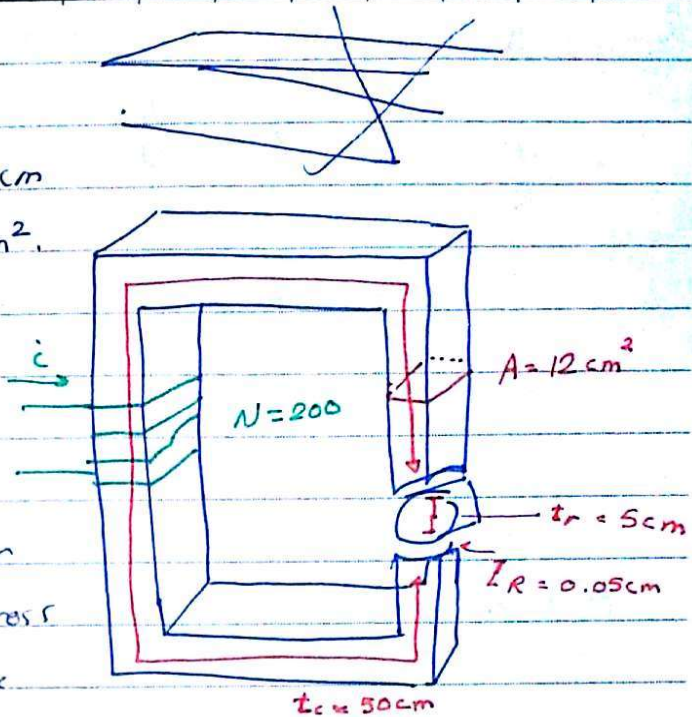
$$I = 0.6018 \text{ A.}$$

$$B = \frac{\mu N\dot{i}}{L}$$

$$\frac{0.5 * 0.05 * 10^{-2}}{400 * [9000 * 4\pi * 10^{-7}]} = I$$

Example 1-3:

the mean path of the stator is 50cm and cross sectional area is  $12 \text{ cm}^2$ .  
 the mean path of the rotor is 5cm, and its cross sectional area also may be assumed to be  $12 \text{ cm}^2$ . each air gap between the rotor and stator is 0.05cm wide and the cross sectional area is  $14 \text{ cm}^2$  at the air gap (including fringing)



$\mu = 2000$ ,  $N = 200$  turns,  $I = 1 \text{ A}$ ,  $\Phi$  flux density in the air gap will be ?? solution:

$$R_s = \frac{0.5}{12 \times 10^{-4} \times 2000 \times 4\pi \times 10^{-7}} = 165786.3991 \text{ A.turns/wb}$$

$$R_r = \frac{0.05}{12 \times 10^{-4} \times 2000 \times 4\pi \times 10^{-7}} = 16578.63991 \text{ A.turns/wb}$$

$$R_{\text{air}} = \frac{0.05 \times 10^{-2}}{4\pi \times 10^{-7} \times 14 \times 10^{-4}} = 284205.2555 \text{ A.turns/wb} \quad \left( \frac{\mu_0}{2} \right)$$

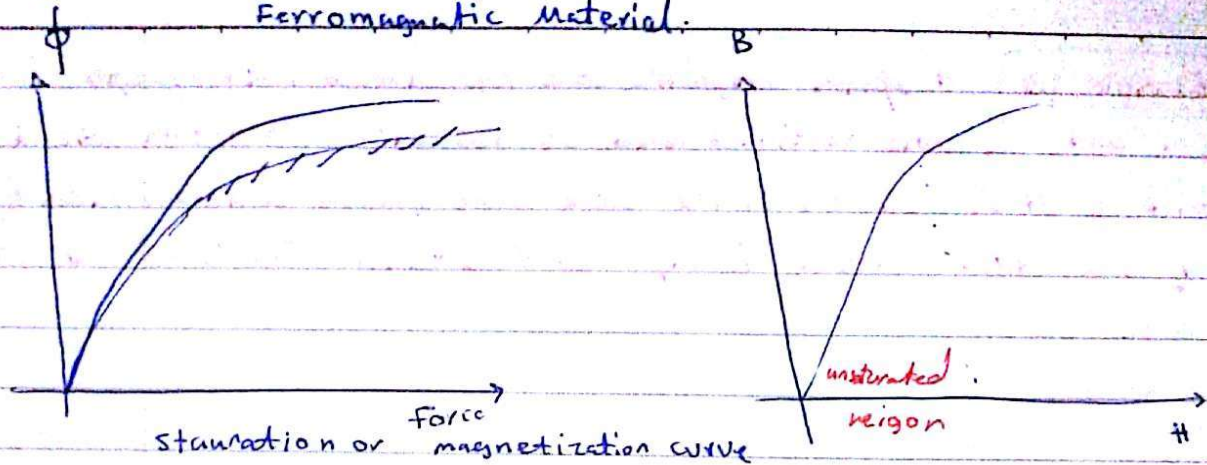
$$R = 466570.2945 + 750772.55$$

$$\Phi = B \cdot A$$

$$\frac{200(1)}{466570.2945 + 750772.55} = B \times 14 \times 10^{-2} = 1.9 \times 10^{-3} \quad 0.19$$



Magnetic behavior for No. Ferromagnetic material.



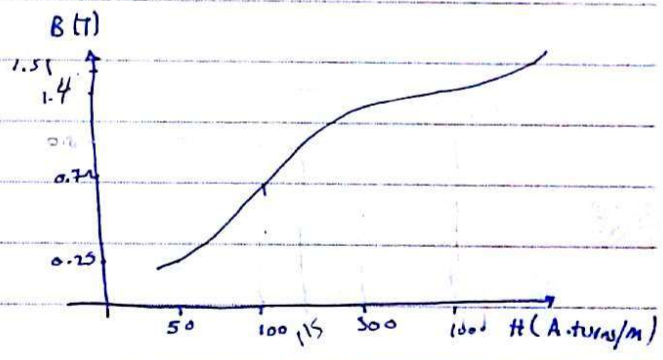
saturation or magnetization curve  
 $H$  proportional to  $\mathcal{F}$  (for air vs.  $\mu$  proportional to  $B$ )  
 (مغناطيسية)

في المنطقة غير المشبعة،  $B$  يتناسب طردياً مع  $H$  (نسبة  $\mu$  ثابتة)   
 وبما أن  $B = \mu H$  في المنطقة غير المشبعة،   
 saturated point -

in unsaturated region the permeability [slope] is constant

example:

Find Relative Permeability for  
 $H = 50, 500, 100, 1000 \text{ A.turns/m}$



$\frac{B}{H} = \mu$  50

$\mu = \frac{B}{H} \quad \mu_r = \frac{\mu}{\mu_0}$

$\mu = \frac{0.25}{50} = \frac{5 \times 10^{-3}}{4\pi \times 10^{-2}} = 3979 \text{ H/m}$  ~~constant~~

$\mu_r = \frac{0.7}{100 \times 4\pi \times 10^{-2}} \quad \mu_r = 5730 \text{ H/m}$   $\downarrow \mu$   $\uparrow B$   $\uparrow H$

$\mu_r = \frac{1.5}{500 \times 4\pi \times 10^{-2}} = 2228 \text{ H/m}$

$\mu_r = \frac{1.5}{1000 \times 4\pi \times 10^{-2}} = 12.02 \text{ H/m}$



Example 15 A square magnetic core has a mean path length of 55 cm and a cross sectional area of  $150 \text{ cm}^2$ .  $N=200$  turn coil of wire.  $\mu$  is shown in the curve below [in the previous example]:  
 a) how much current is required to produce  $0.012 \text{ Wb}$  of flux in the core

solution

$$\phi = \frac{Ni}{R}$$

curve  $B-H$

$$\phi = B \cdot A$$

$$0.012 = B \times 0.015$$

$$B = 0.8 \rightarrow \mu_r = 518$$

$$H = 115 \text{ A-turn/m}$$

$$B = \frac{\mu H}{\mu_r} \Rightarrow 6.956 \times 10^{-3} \text{ A/m}$$

$$\mu = \mu_r \cdot \mu_0$$

$$\phi = \frac{200 i}{0.55} \times 6.956 \times 10^{-3} \times 0.015 = 0.316$$

b) what is the core relative permeability at that current

$$\mu_r = \frac{6.956 \times 10^{-3}}{4\pi \times 10^{-7}} = 5535 \text{ H/m}$$

c) what is the reluctance of the core??

$$R = \frac{0.55}{6.956 \times 10^{-3} \times 0.015} = 5271.22 \text{ A-turns/Wb}$$





### 1.5 Faraday's law: [basis of transformers operation].

a time changing magnetic Flux produce an electro motive force.

$$emf = - \frac{d\phi}{dt} * N$$

القوة الحثية تعكس مجال الفيض المتغير

لنفس  
law

#### Example: 1-6

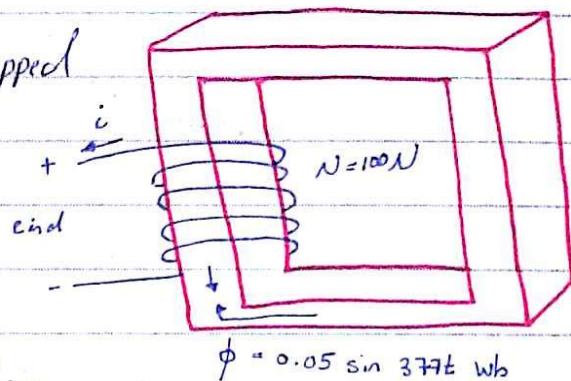
it shows a coil of wire wrapped around an iron core. the flux is given by the equation

$$\phi = 0.05 \sin 377t \text{ Wb}$$

$N = 100$  1 wind??

of what polarity is the voltage during

the time when flux is increasing in the reference direction shown in the figure? (assume that the flux leakage is zero)



solution:  $v_{ind} = N \frac{d\phi}{dt} = 100 \frac{d(0.05 \sin 377t)}{dt}$

$$100 \times 0.05 \cos 377t \times 377$$

$$v = 1885 \cos 377t \text{ V}$$

التيار الحثي في الملف هو  $v = 1885 \cos 377t$  فولت

$$[v \text{ في } t = 0.05]$$



1.6 production of induced force on a wire: [basis of motor action]

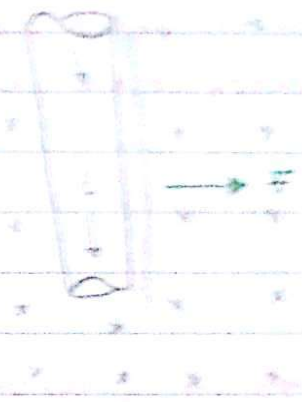
↑ قوة مغناطيسية  
 قوة لتيار في سلك  
 القوة المغناطيسية  
 سلك يمر فيه تيار ووضوح في مجال مغناطيسي متساو  
 يتأثر بقوة مغناطيسية

$$F = i (L \times B)$$

current.      length of wire.      magnetic flux density.

$$= i L B \sin \theta$$

↳ wire flux density vector



Example 1.7: The magnetic flux density is 0.25T directed into the page if the wire is 2.0m and carries 0.5A. in direction from the top to the bottom. Find direction and magnitude [1.16]

solution:

$$F = i L B \sin \theta$$

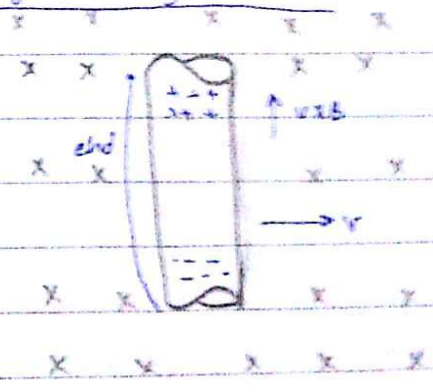
$$0.5 \times 2 \times 0.25 \sin 90 = 0.125 \text{ N to the right}$$

1.7 Induced voltage on a conductor Moving in a Magnetic Field:

awire with the proper orientation moving through magnetic field (voltage) is induced in it.

$$v_{ind} = (v \times B) \cdot L$$

velocity      density      length



[basis of generator action]



Example 1.8: Show a conductor moving  $v = 5 \text{ m/s}$  to the right in the presence of a magnetic field. The flux density  $0.5 \text{ T}$  into the page. Length of wire is  $1 \text{ m}$ . What are the magnitude and polarity of the resulting induced voltage??

Solution:

$$V = (v \times B) \cdot l$$

$$(5 \times 0.5 \sin 90) \cdot 1 = 2.5 \text{ V}$$

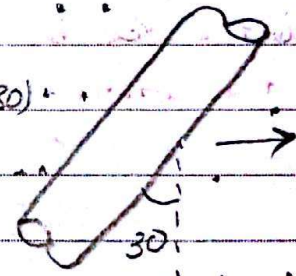
Example 1.9 conductor moving with velocity of  $10 \text{ m/s}$  to the right in a magnetic field. The flux density is  $0.5 \text{ T}$ , out of the page, and the wire is  $1 \text{ m}$  length, oriented as shown. What is the magnitude and polarity of induced voltage??

Solution:

$$V = (10 \times 0.5 \sin 90) \times 1 \cos(30)$$

$$= 4.33$$

direction of induced voltage

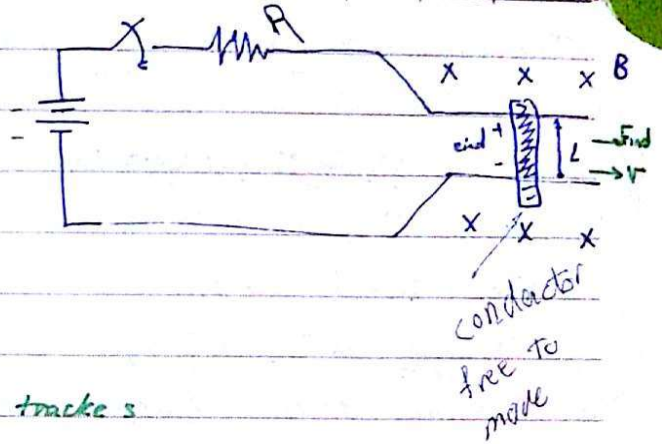


$v \times B$



1.8 the linear DC- ~~Motor~~ Machine-

1.  $F = i(l \times B)$
2.  $e_{ind} = (v \times B) \cdot l$
3. Kirchhoff's voltage law for this is:  
 $v_B = IR + v_{ind}$
4. Newton's law for bar across the tracks  
 $F_{net} = ma$



No loaded process:

\* close the switch:

$i = \frac{v_B - v_{ind}}{R}$        $v_{ind} = 0$        $i = \frac{v_B}{R}$  ← at starting

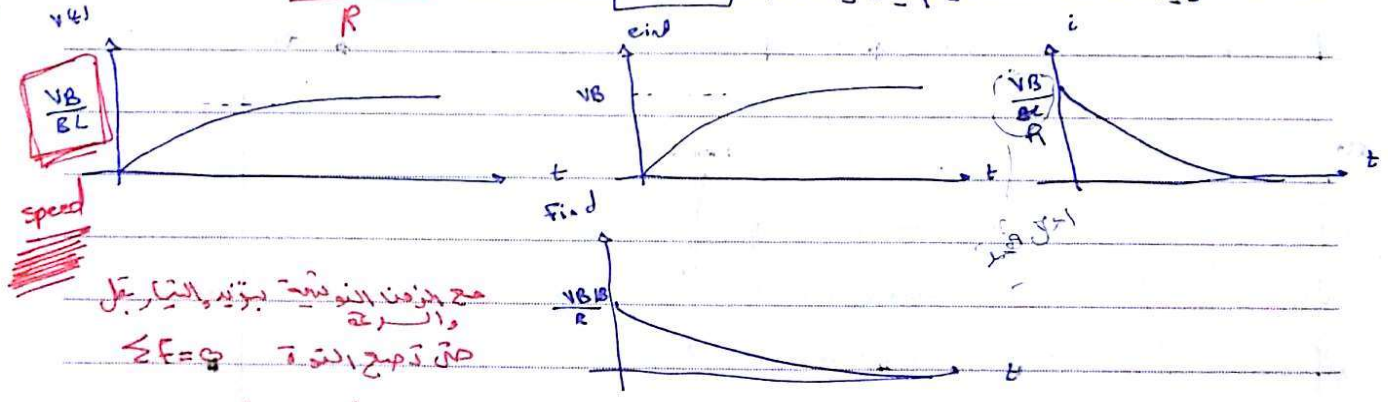
→ after moving

$F = i l B$  to the right       $e_{ind} = v B l$

$i = \frac{v_B - v_{ind}}{R}$

$\sum F = 0$

توازن القوى  $v_{ind}$  و  $v_B$  و  $i$



مع الزمن التوتيرة بتزيد والسرعة تبتعد عن الصفر  $\sum F = 0$

constant steady-state speed.

$i = \frac{v}{R}$        $v_{ind} = v B l$

$F = i l B \sin 90^\circ$        $v_{ind} = v B l$

$v_{ss} = \frac{v_B}{B l}$        $v_{ind} = v_B$

Force       $I = \frac{v - v_{ind}}{R}$        $v_{ind} = v B l$

$v_{ss} = \frac{v_B}{B l} = \frac{v_B}{B l}$        $F = 0$        $i = 0$        $e_{ind} = v_B$

$v_B = \frac{v B l}{B l}$







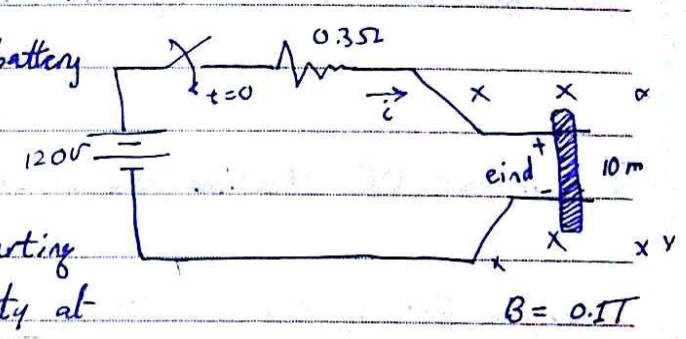


$e_{ind} > V_B \rightarrow$  act generator. [more rapidly]  
 $e_{ind} < V_B \rightarrow$  act motor. [more slowly]

بشروط بين الآتي ← motor or generator

generator ← انوار اقل او اقل بكون كثير وهدا بسبب مشاكل على انوار  
 add another resistance at standby

Example 1-10 a linear DC-Machine has a battery voltage 120V, an internal resistance 0.3Ω and a magnetic flux density at 0.1 T



1- What is the machine maximum starting current?? what is steady state velocity at no load??

KVL  $\rightarrow \frac{120}{0.3} = 400A$

~~think (v B l) = 120 m/s~~

steady state =  $v_{ss} = \frac{V_B}{Bl} = \frac{120}{0.1 \times 10} = 120 \text{ m/s}$

2- suppose 30N-force pointing to the right were applied to the bar.  $v_{ss}??$   
 How much Power would the bar be producing or consuming? How much Power would the battery be producing or consuming?

بشرط



$$e_{ind} = vBl$$

$$i = \frac{e_{ind} - vB}{R}$$

$$iR + vB = e_{ind} \rightarrow \boxed{iR + vB = vBl} \quad (1)$$

$$F_{app} = F_{ed} = iBl$$

$$30 = i \times 0.1 \times 10 \quad \boxed{i = 30A}$$

$$30 [0.3] + 120 = v^s \times 0.1 \times 10$$

$$v^s = 129 \text{ m/s}$$

The Bar is producing power  $p = Fv = 129 \times 30 = 3870 \text{ W}$

by doing this work generator is

the battery is consuming power  $p = v^s I = 120 \times 30 = 3600 \text{ W}$

[3] 30 N force pointing to the left were applied to the bar. Is generator or motor?? motor  $\Rightarrow$   $v^s$  is

at the steady state  $|F_{app}| = |F_{ed}| = lBi$

$$30 = 0.1 \times 10 \times i \quad \boxed{i = 30A}$$

$$e_{ind} = vBl$$

at steady state  $\frac{vB - e_{ind}}{R} = i$   $-e_{ind} = Ri + vB$

$$e_{ind} = -Ri + vB$$

$$120 - 30(0.3) = v^s \times 10 \times 0.1$$

$$v^s = 111 \text{ m/s}$$

4. Assume a force is pointing to the left is now applied to the bar. calculate the speed at 0N, 50N, 10N current

$\downarrow$                        $\downarrow$                        $\downarrow$   
 120                      150                      120

5. Assume the bar is unloaded and it suddenly runs into region where the magnetic field is weakened to 0.08 T. How fast will the bar go now?

$$v_{end} = \sqrt{0.08 \times 10}$$

$$F = iBL$$

$$0 = i = 0$$

$$i = \frac{vB - v_{end}}{R}$$

$$vB = v_{end}$$

$$120 = \sqrt{0.8}$$

$$v = 150 \text{ m/s}$$

no load, up, friction since 1st

$$\frac{\text{Friction}}{LB} = i$$



CHAPTER SEVEN:

DC MACHINERY  
FUNDAMENTAL.

7.1 A sample Rotating Loop between curved pole face:

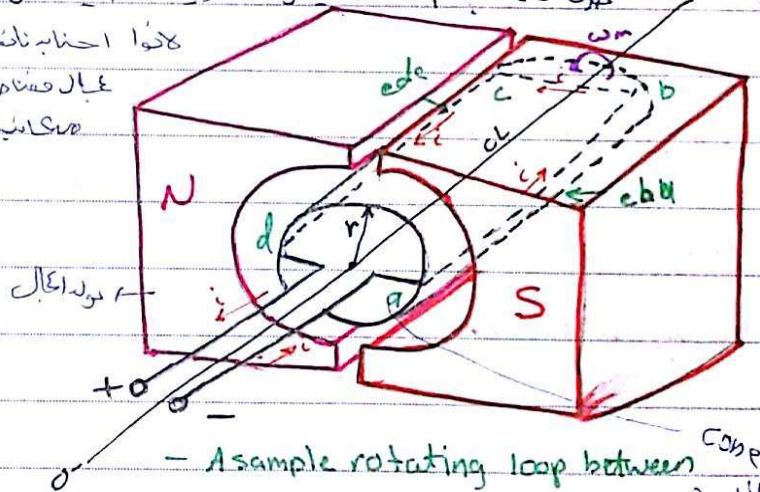
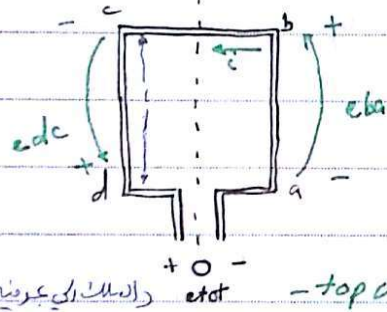
\* Real generator and motor do not move in straight line ~~is~~ they rotate.

→ The rotating part of motor called rotor. Armature عبارة عن املاك مترابطة

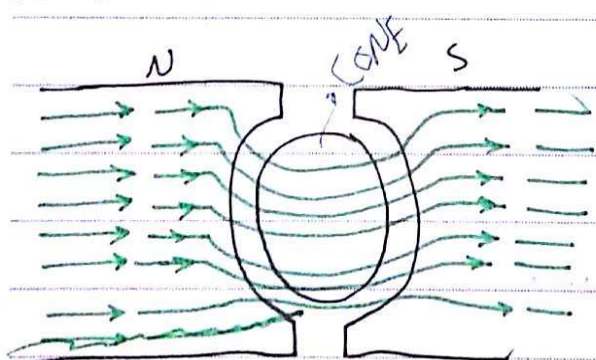
→ The stationary part of motor called stator OR, Field coil (يتبعين اقطاب) Magnetic poles. the magnetic field is supplied by the North and south poles.

طرق توليد اقطاب ايضا فوسه [ عن طريق مفتاحيس مثل بالرمسة او عن طريق سلك عن منبع تيار كهربائي ]

لانوا احكامه نالمنصفه انو اتسا بالمركبي سلك دائري  
عبار عن مفتاحيس تولد حركه  
سلك اسبوكه



- A sample rotating loop between curved pole face.



- view of field line -

\* عشان نيكو الاقطاب لازم سلك اقطر طرفين بالانوار  
نقطه اقطار  
بين ال pole وال rotor - ويتكون علودين كلنوع ال

[ Reluctance } Flux density ] rotor is uniform under the poles face

- ab cd plane of the page
- bc da parallel



look at the drawing in pre page: 00

The Voltage Induced in a Rotating Loop  $\rightarrow$  to determine the total voltage eor on the loop examine each segment of the loop separately and sum all resulting voltage. the voltage on each segment is  $e_{ind} = (v \times B) \cdot l$

1 segment ab :

$$e_{ba} = (v \times B) \cdot l = \begin{cases} vBl & + \text{ into the page under the pole face} \\ 0 & \text{beyond the pole edges} \end{cases}$$

2. segment bc :

$$e_{cb} = 0 \quad \cos 90^\circ = 0 \quad v \times B \text{ is } \perp \text{ to } l \text{ so } v \times B \cdot l = 0$$

3. segment cd :

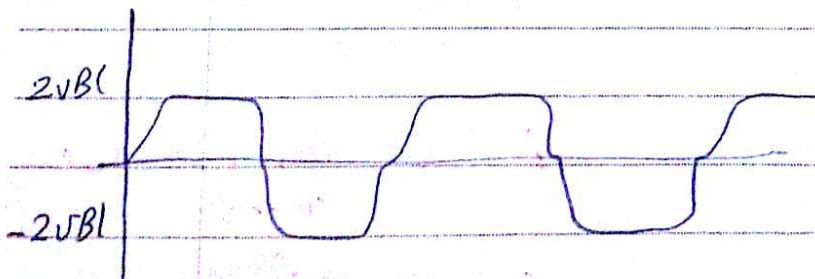
$$e_{dc} = \begin{cases} vBl & + \text{ out of the page under the pole face} \\ 0 & \text{beyond the pole edges} \end{cases}$$

4. segment da

$$e_{ad} = 0 \quad \text{bc is } \perp \text{ to } v \text{ and } v \times B$$

$$\text{TOTAL } e_{ind} = \begin{cases} 2vBl & \text{under pole face} \\ 0 & \text{beyond the pole edges} \end{cases}$$

The Output Voltage OF The Loop:





The final form of the voltage equation:

$$e_{ind} = \begin{cases} \frac{2}{\pi} \phi \omega n & \text{under the pole face.} \\ 0 & \text{beyond the pole edges.} \end{cases}$$

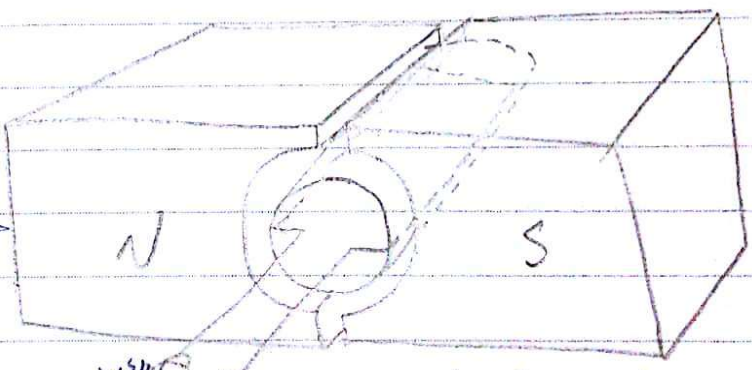
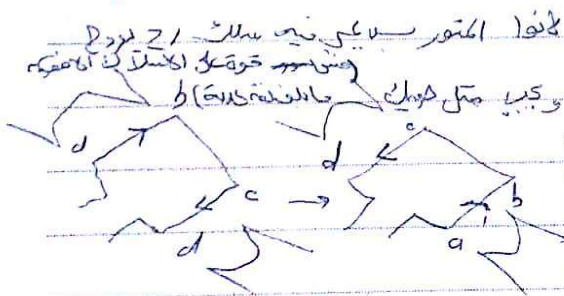
the voltage in any real machine will depend on the same three factors:

the flux, the speed of rotation, or a constant representing the construction of the machine.

Getting DC - voltage out of the rotating loop:

The loop give us alternately a constant negative and positive value how to get DC - voltage at it??

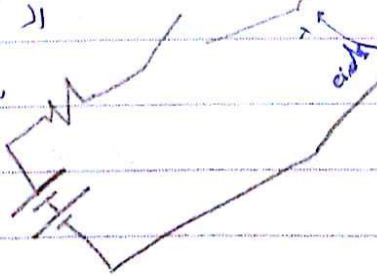
→ we add [commutator] at the end of the loop when the voltage change its direction the contact also switch connections so the output will build in the same way.



لأننا المتور سايحي فيه سلك 2 يورد  
 ويتحرك في اتجاه التيار الكهربائي  
 والنتيجة هي (التيار الكهربائي)  
 أو  
 صرح بتغير اتجاه التيار في ال pole, لو ادر  
 عن ان هيك يكون AC ما زيف  
 commutator

brushes  
 commutator (حلقات متحركة)  
 تسمى  
 بسبب الاحتكاك بينها يسبب شرارة (شرارة)  
 sparks

بأن التور انارة الى من الفولتج  
 وانتحرك به باتجاه التيار  
 فتتولد تيار في كل حلق  
 على اناصة.



No. \_\_\_\_\_

گنراتر اور generator یلف بالعمس بعمس اعمظاب اومعمس اعمظاب



No.

The Induced Torque in the Rotating loop.  $\phi = \phi_m \sin \theta$   
-  $\phi$  is  $\phi_m \sin \theta$   $\rightarrow$  switch  $\rightarrow$  sinusoidal torque  $\rightarrow$

$$F = (I \times B)l$$

under the poles surface  $\rightarrow$  is  $\phi_m \sin \theta$

$$T = Fr \sin \theta$$

$$T = 0 \text{ beyond the pole edges}$$

1. Segment ab:

$$F = i l B$$

$$T_{ab} = F(i l B) \text{ CCW}$$

2. segment bc:

$$F = 0 \quad \perp \parallel B$$

$$T_{bc} = 0$$

3. Segment cd:

$$F_{cd} = i l B$$

$$T_{cd} = r i l B \text{ CCW}$$

4. Segment da:

$$F_{da} = 0 \quad \perp \parallel B$$

$$T_{da} = 0$$

$$\text{Total: } |T_{ind}| = \begin{cases} 2rBiI & \text{under the poles surface} \\ 0 & \text{beyond the pole edges} \end{cases}$$
$$\phi = A_p B \quad A_p = \pi r l$$

$$\text{OR } T_{ind} = \begin{cases} \frac{2}{\pi} \phi i & \text{under the poles surface} \\ 0 & \text{beyond the pole edges} \end{cases}$$

the torque in Any Real machine depend on:

the flux, the current, A constant Represent the construction of the machine



Example 7-1. a simple rotating loop between curved pole faces connected to a battery and a resistor through a switch. the resistor shown models the total Resistance of the battery and the wire in the machine:

$$r = 0.5 \text{ m} \quad l = 1 \text{ m}$$

$$R = 0.3 \Omega \quad B = 0.25 \text{ T}$$

$$V_B = 120 \text{ V}$$

a) what happens when the switch closed??

solution a current is produced  $i = \frac{V_B}{R}$  (veind=0)

$i = 400 \text{ A} \rightarrow$  produced torque

$$F = 2(l \times B)$$

$$400 \times 1 \times 0.25$$

$$\tau = \frac{2}{\pi} \times 0.25 \times 400 = 63.66 \text{ N.m CCW}$$

u end  $\leftarrow$  angular acceleration  $\leftarrow$

$$\text{eind} = \frac{2}{\pi} \cdot \phi \cdot \omega n$$

veind =  $V_B \leftarrow \tau = 0$   $\rightarrow$  linear motor  $\rightarrow$   $\leftarrow$   $\rightarrow$   $\leftarrow$

b) What is the machine maximum current & angular velocity steady state at no load??

$$i = \frac{V_B}{R} = 400 \text{ A}$$

$$A = 2\pi r l$$

at no load  $\dots \underline{V_B = \text{veind}}$

$$120 = \frac{2}{\pi} \times 0.25 \times \omega n$$

$$\omega n = 480$$

$$\phi = \frac{\mu_0 N i M}{L} = \frac{B A}{L}$$

$$\frac{2}{\pi} \times B \cdot (2\pi r l) \cdot i$$



c) suppose a load is attached to the loop, and the resulting load torque is  $10 \text{ N.m}$ . What would the new  $v_{ss}$ ? power by battery power by the shaft.

solution:

$$\tau = \frac{2}{\pi} ABi$$

$$10 = \frac{2}{\pi} \cdot B \cdot \pi r L i \quad i = \frac{10}{2 \pi r L B} = \boxed{40 \text{ A}}$$

$$e_{ind} = \frac{2}{\pi} \phi \omega n$$

$$= \frac{2}{\pi} B \pi r L \omega n$$

$$e_{ind} = 2B r L \omega n$$

$$40 = \frac{V_B - e_{ind}}{R} \quad e_{ind} = 108$$

$$108 = 2(0.25) \cdot 0.5 \times 1 \times \omega n \quad \omega n = 432 \text{ rad/s}$$

$$P = V^2 I$$

$$= 120(40) = 4800$$

$$P = \tau \omega$$

$$\frac{10 \times 0.5}{\sin \theta} \times 432 = 4320$$

motor

d) suppose the machine is unloaded again, torque of 7.5 N.m in the direction of rotation.  $V_{ss}$ ? a machine or generator??

direction of motion  $\tau$  ↑ acc ↑ speed  $e_{ind}$  ↑ current opposite generator!!

$$\tau = \frac{2}{\pi} B \pi r L i \quad i = \frac{7.5}{2 \times 0.5 \times 0.25} = 30 \text{ A}$$

$$30 = \frac{e_{ind} - V_B}{R} \quad e_{ind} = 120 \text{ V}$$

$$120 = 2 B r L \omega n \quad \omega n = 516 \text{ rad/s}$$

e) suppose the machine running unloaded, what would the final steady state speed of rotor be if the flux density were reduce to 0.2 T.

$$e_{ind} = V_B$$

$$120 = 2 B r L \omega n$$

$$\omega n = \frac{120}{2 \times 0.2 \times 0.5 \times 1} = 600 \text{ rad/s}$$

$$\downarrow \phi = Ni \downarrow$$

$$i \downarrow \quad v \uparrow$$



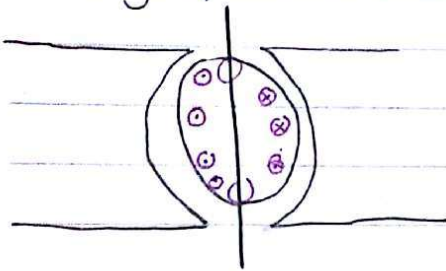
### 7.4 Problems With Commutation IN Real Machine:

#### 1 - Armature Reaction:

when a load is connected to the terminals of the machine a current will flow and produce a magnetic field of its own, which will distort the original magnetic field of the poles called armature reaction.

Armature Reaction caused two serious problems: magnetic neutral shift

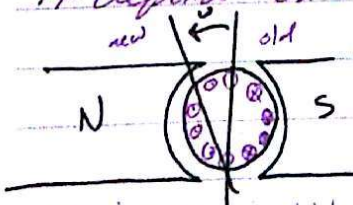
magnetic neutral plane: it's a plane of the machine where the velocity is parallel to flux density line,  $e_{ind} = 0$



- Flux distributed uniformly under the poles surface
- the voltage built out at the page under North pole
- the voltage built in the page under south poles
- Neutral plane is vertically

when a load is applied so the device is Generator.

the current will flow out of the page under the North poles and in the page under the south poles. this current will produce a magnetic field that will effect the original magnetic field which produce the voltage in the first place. (the plane will be shifted in the direction of motion and it depend on the amount of current)



High losses, voltage, sparks, commutator, brushes, and more armature reaction.

High losses, voltage, sparks, commutator, brushes, and more armature reaction.



it cause sparking and arcing in the brush <sup>lead</sup> to ~~reduce the commutator~~ <sup>to</sup> ~~like~~ increase maintenance, it can't be solved by replacing it (it may sparkle at no load)

high voltage will help to arc the arced it can be lead to flashover in commutator  $\rightarrow$  arc melt the <sup>cut above</sup> commutator surface.

2. the second major problem caused by Armature Reaction called flux weakening. saturated point

flux  $\rightarrow$  increase  $\rightarrow$  saturation point  $\rightarrow$  flux  $\rightarrow$  decrease

Flux weakening  $\rightarrow$  motors Flux  $\downarrow$  speed  $\uparrow$   $\rightarrow$  machine disconnected  $\rightarrow$  motor destroy it self  
 $\rightarrow$  generator Just reduce the voltage induced

$L \frac{di}{dt}$  voltages: happend in commutator segment called inductive kick.

high voltage  $\rightarrow$  sparking

when the segment shorted the current reverse fast, a very high voltage

$\frac{di}{dt} \rightarrow \frac{di}{dt} = v \rightarrow$  spark  $\rightarrow$  induced in the segment

سرعة انتقال التيار يكون عالية  $\rightarrow$  معدل انتقال التيار يكون سريع  $\rightarrow$  سبب

من المفترض ان يكون التيار يكون سريع





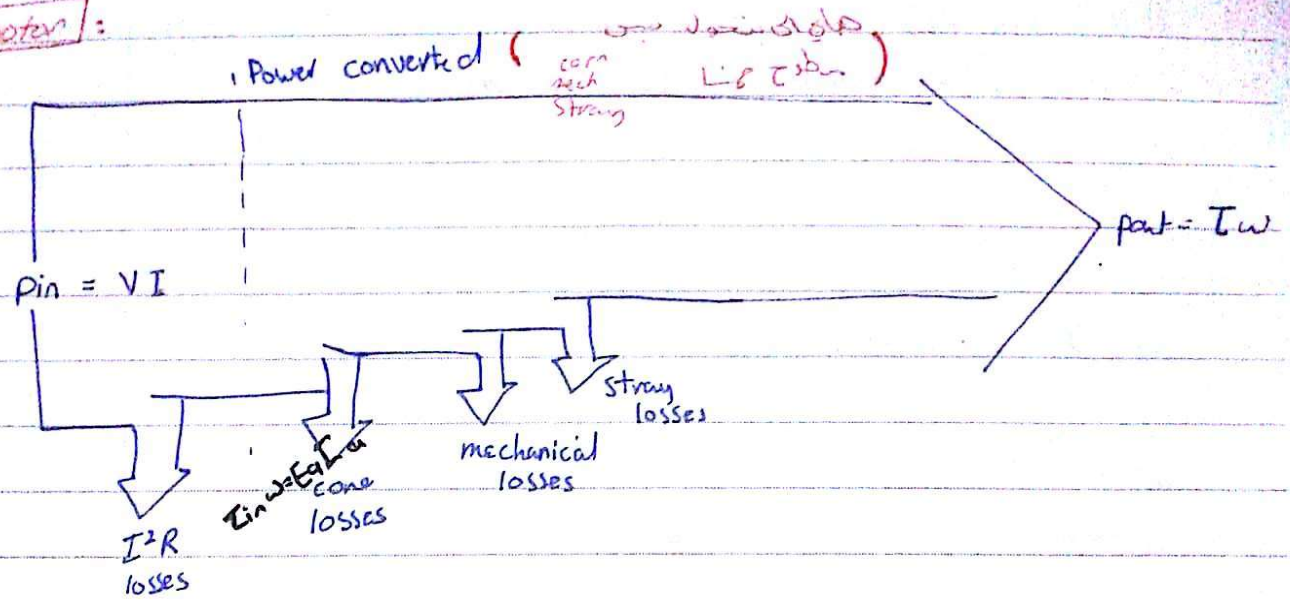




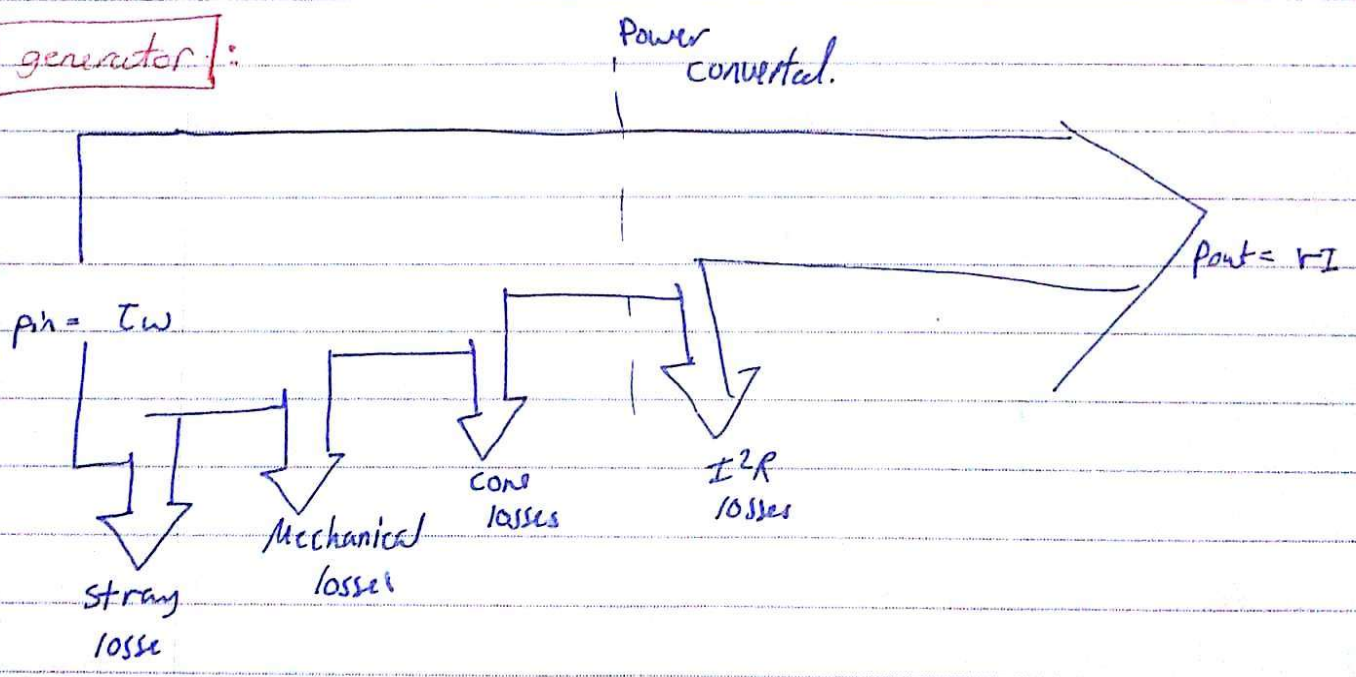


# The Power flow diagram:

**motor:**



**generator:**



example:

$$B = 0.4 \text{ T}, \quad V_B = 48 \text{ V}, \quad L = 0.5 \text{ m}$$

$$r = 0.25 \text{ m}, \quad R = 0.4 \Omega, \quad \omega = 500 \text{ rad/s.}$$

1] Is this operate as machine of generator, Explain?

$$V_{emf} \bar{E} = \frac{2}{\pi} * B * r * L * \omega$$

$$V_{emf} \bar{E} = 2 * (0.4) * (0.25) * 0.5 * 500 = 50 \text{ mV}$$

$V_{emf} > V_B$  generator.

2] What is the current ~~flow~~ flowing in to or out to the machine, power??

$$i = \frac{V_{emf} - V_B}{R} = 5 \text{ A}$$

$$P = 5 * 48 = 240 \text{ 'by battery}$$

$$P = \tau * \omega = 250 \text{ 'by shaft}$$

3] If the speed change to 550 rad / 450 rad find current (how?)

$$i = \frac{2(0.4)(0.25)(0.5)(550) - 48}{0.4} = 17.5$$

$$i = \frac{2(0.4)(0.25)(0.5)(450) - 48}{0.4} = -7.5 \text{ motor}$$



## Chapter 8: DC MOTORS AND GENERATORS:

### 8.1 INTRODUCTION TO DC MOTORS:

DC motor are often compared by their **speed Regulation (SR)** =

$$SR = \frac{\omega_{no\ load} - \omega_{full\ load}}{\omega_{full\ load}} \times 100\%$$

نسبة

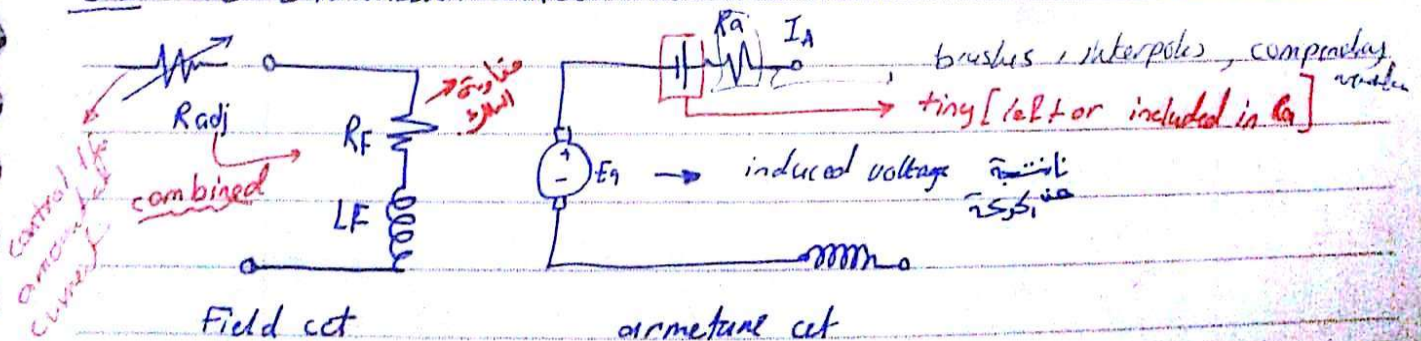
$$SR = \frac{n_{no\ load} - n_{full\ load}}{n_{full\ load}} \times 100\%$$

- (+) SR means that the motor speed drops with increasing loads
  - (-) SR means that the motor speed increase with increasing loads
- magnitude of (SR) = Slope of the torque - speed curve

\* there are five major types of dc motors in general use: -

1. The separated excited dc motor
2. The shunt dc motor
3. The permanent-magnet dc motor
4. The series dc motor
5. The compounded dc motor

### 8.2 THE EQUIVALENT CIRCUIT OF A DC MOTOR:



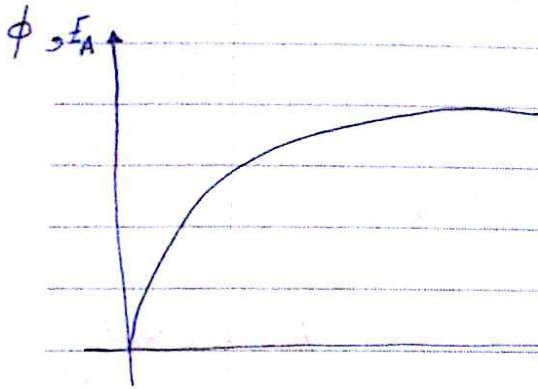
steady state  $\rightarrow$  Inductor  $\rightarrow \frac{di}{dt} = \text{zero}$



$E_A = K\phi\omega_m \rightarrow$  generated voltage

$T_{in} = K\phi I_A \rightarrow$  induced Torque

8.3 THE MAGNETIZATION CURVE OF A DC MACHINE:



$E_A$  is directly proportional to  $\omega_m$  and  $\phi$ .

$\phi$  with  $E_{ind}$  is shown because  $E_A$  is proportional to  $\phi$  so  $\phi$  with  $\omega_m$  is

$\frac{d\phi}{dI_f}$  A.turns

shown

most machine operates in the region near the saturation point?

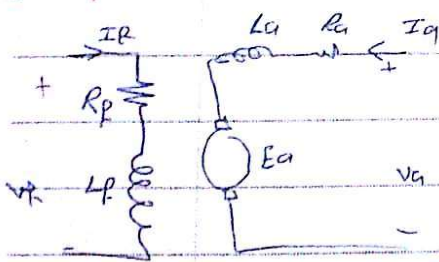
because huge increase in current will give us a little increase in  $E_A$  (voltage drop).

power supply



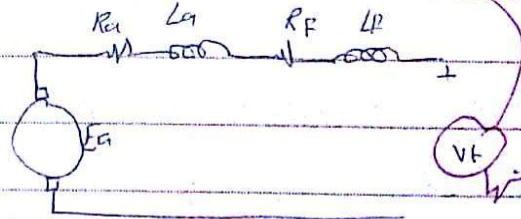
dc motors

① Separated excited DC-Motor:

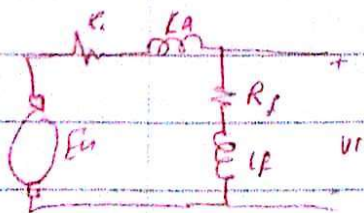


② series DC-MOTOR

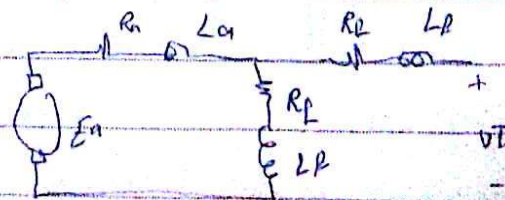
$\phi = \text{constant}$



③ Shunt DC-motor



④ compound dc motor













No. \_\_\_\_\_

power = 50 hp

$V = 250 \text{ V}$

at no load  $[Z=0] = 1200 \text{ r/min}$

compensating winding =  $\phi$  [constant]

$R_A = 0.06 \Omega$     $R_P = 50 \Omega$     $N = 1200$

at  $Z=0 \rightarrow I_a = 0$

$$I_{tot} = I_p = \frac{250}{50} = 5 \text{ A} \rightarrow \text{torque} = 0$$

a)  $100 - 5 = 95$

$$Z = k \phi 95$$

$$V_B = E_a + \frac{I_a R}{k \phi}$$

$$250 = E_a + \frac{k \phi 95 (0.06)}{k \phi} \quad E_a = 249.3 \text{ V}$$

$$249.3 = k \phi \omega$$

at no load  $250 = k \phi 1200$

$$\frac{249.3}{250} = \frac{\omega}{1200}$$

$$\rightarrow \text{torque} = 0$$

$$\omega = 1173 \text{ r/min}$$

b)  $I_p = 200 - 5 = 195 \text{ A}$

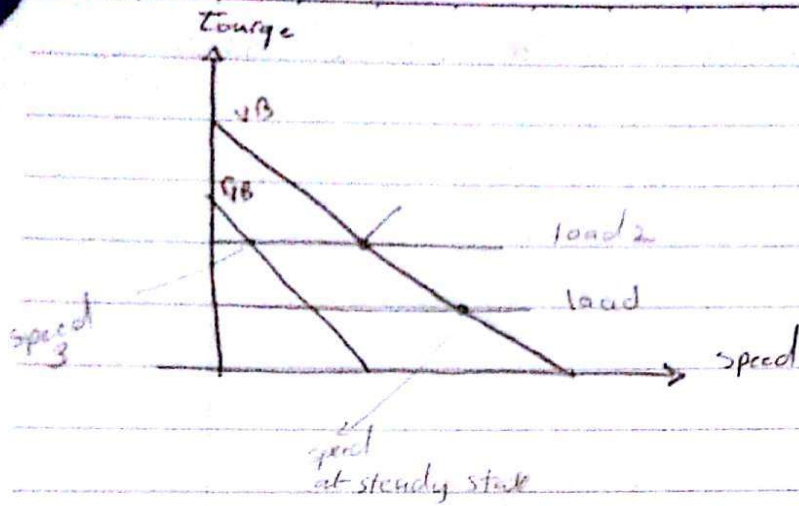
$$V_B = E_a + I_a R_A$$

$$250 = E_a + 195 (0.06) \quad E_a = 238.3 \text{ V}$$

$$238.3 = k \phi \omega$$

$$250 = k \phi 1200$$

$$\omega = 1144 \text{ r/min}$$



كل load اوسعة حصة >

مخازن اللول نقل السرعة <

وسب نقل الواقع على السرعة

speed  
=  $\omega$

[E]

$$I_A = 300 - 5 = 295 \uparrow \text{ wnt } \tau \uparrow$$

$$V_a = E_a + I_a R_a$$

$$250 = E_a + 295(0.06) \quad E_a = 232.3$$

$$232.3 = k\phi\omega$$

$$250 = k\phi 1200 \quad \omega = 1115 \text{ rad/s}$$

[d]

$$\tau = k\phi i \quad (E = k\phi\omega) \quad k\phi = \frac{E}{\omega}$$

$$\tau = \frac{E i}{\omega}$$

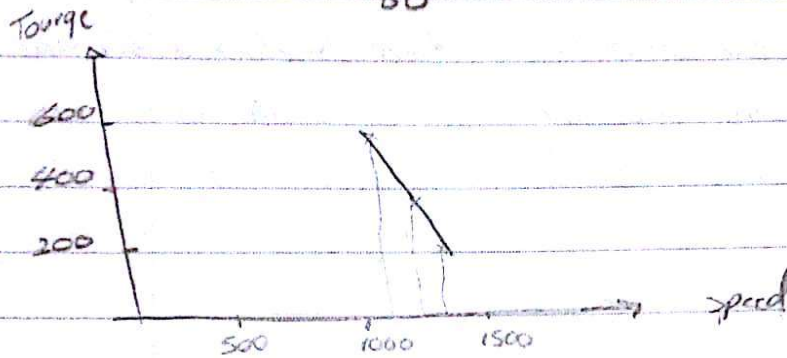
$$\tau = \frac{95 (244.3)}{1173 \frac{\text{r}}{\text{min}} \cdot \frac{1 \text{ min}}{60 \text{ s}} \cdot \frac{2\pi \text{ rad}}{\text{r}}} = \frac{95(244.3)}{122.83} = 190 \text{ Nm}$$



No. \_\_\_\_\_

$$T = \frac{E_c}{\omega} = \frac{238.3 (195)}{1144 \times \frac{2\pi}{60}} = \frac{238.3 (195)}{119.79} = 388 \text{ N.m}$$

$$T = \frac{232.3 (295)}{115 \times \frac{2\pi}{60}} = \frac{232.3 (295)}{116.76} = 587 \text{ N.m}$$



### Non-linear Analysis of shunt DC-motor

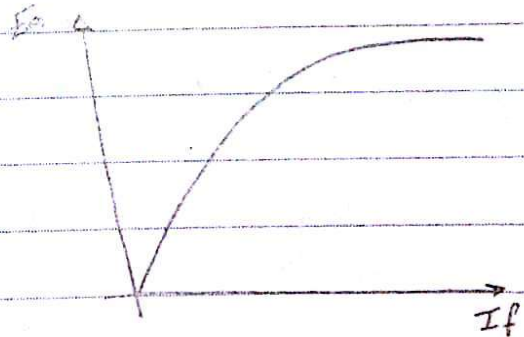
Flux  $\phi$  and  $E_a$  (internal voltage) is non-linear with the mmf

Example

to find  
BL

$$F_{net} = NF I_f - F_{AR}$$

$$I_f^* = I_f - \frac{F_{AR}}{NF}$$



Kirchhoff's law

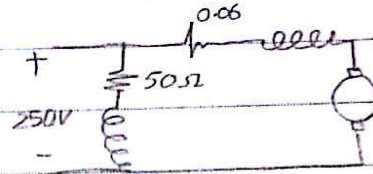
$$\frac{E_a}{E_{a0}} = \frac{N_m}{N_0}$$

initial references



Example 50hp, 250V, 1200 r/min dc shunt motor without compensating winding has an armature resistance (including the brushes and interpoles) of  $0.06 \Omega$ . Its field circuit has a total resistance  $R_f + R_{adj}$  of  $50 \Omega$ , which produce a no load speed of 1200 r/min, 1200 turns per pole on shunt field winding, and the armature reaction produce a demagnetizing mmf of ~~48~~ 840 A-turns at a load current of 200A, curve is shown  
a) find the speed of this motor when its input current is 200A?

Solution:



at no torque  $I_f = \frac{250}{50} = 5A$

$$I_A = I_L - I_f$$

$$200 - 5 = 195A$$

$$V_B = E_a + I_A R_a$$

$$250 = E_a + 195(0.06)$$

$$E_a = 238.3V$$

$$I_f^* = I_f - \frac{F_{AR}}{N}$$

$$5 - \frac{840}{1200} = 4.3A$$

$$4.3 \rightarrow \text{من اضعف}$$

$$4.3 \rightarrow 233V = E_0$$

$$\frac{E_a}{E_0} = \frac{n}{n_0}$$

$$\frac{238.3}{233} = \frac{n}{1200}$$

$$n = 1227 \text{ r/min}$$



d) How does its speed compare to that of the previous motor at a load current of 200A ??

$$n_m = 1194 \text{ r/min}$$

$$n_m = 1227 \text{ r/min} \rightarrow R.A \uparrow \uparrow I$$

e) Calculate and Plot the Torque speed for this reaction  
MATLAB

\*Control the speed of shunt dc-motor: (are the same for compounded DC-motor)

1. adjusting the field resistance.
2. " the terminal voltage applied to the armature.
3. Inserting a resistor in series with the armature ckt.

↳ Changing field resistance:

$$R_f \uparrow \quad I = \frac{V_T}{R_f} \text{ decrease } \rightarrow \phi \text{ decrease, } E_a = k\phi\omega_m \text{ decrease.}$$

$$I_A = \frac{V_T - E_a}{R_A} \text{ increase, } \tau = k\phi I_A \uparrow \text{ increase ??}$$

since  $\tau_{ind} > T_{load} \rightarrow \text{speed up}$

$E_a$  increases current to fall  $\rightarrow I_{ind}$  fall too  $T_{ind} = T_{load}$  at steady-state



A warning about lifted field resistance speed control:

the effect of increasing the field resistance is shown



$R \uparrow \Rightarrow I_f \downarrow \phi \downarrow$ , need no load increase  $\uparrow \frac{V_B}{R}$  slope become steeper

at a very low speed

$R_f \uparrow$  reject  $v \uparrow$  but actually speed decrease

[ torque equation  $\tau = k \phi I_a$  ]

[ back speed  $E_a = k \phi \omega$  ]

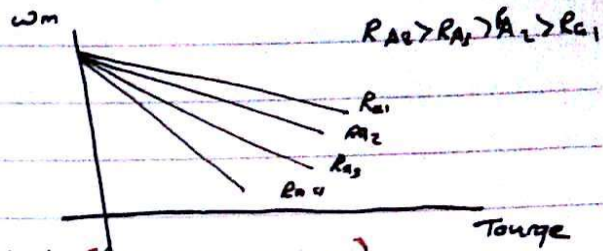
2. changing the armature voltage. [without change the voltage of the field] motor must be sep. excited to use voltage controller

- 1.) increase at  $V_a \rightarrow I = \frac{V_a - E_a}{R_a}$  increase
- 2.) current increase  $\tau = k \phi I \uparrow$  increase  $\rightarrow \tau_{ind} > \tau_{load}$  speed up
- 3.) speed increase  $E_a = k \phi \omega \uparrow$  increase
- 4.)  $E_a$  increase  $I = \frac{V_a - E_a}{R_a}$  decrease
- 5.)  $I$  decrease  $\tau$  decrease  $\tau_{ind} = \tau_{load}$



3. Inserting a Resistor in series with the armature act:

adding  $R_p$  in series will increase the slope, so the machine operate slowly



$I_f, I_b, E_b$  [its very wasteful (losses are very large)]

for speed] it's used in the expensive motor that we can't use a better way or motor operates all the time at full speed.

Field resistance control work with speed above the rate speed  
 armature voltage control work with speed less than the rate speed  
 [combine these two controller in the motor will give average 40 to 1 or more]

example: 100 hp, 250 V, 1200 r/min shunt dc motor with an armature resistance of  $0.03 \Omega$ ,  $R_p = 91.67 \Omega$  the motor has compensating winding AR ignored, mechanical and core losses are negligible, the motor assume to be driving a load with <sup>load</sup> current of  $126 \text{ A}$  and an initial speed of  $1103 \text{ r/min}$ . [assume the amount of armature current drawn by the motor remains constant]

Q curve 8-9, what is the motor speed if the field resistance is  $50 \Omega$ ?

solution  $I_A = I_{load} - I_f$

$$126 - \frac{120}{91.67} = 120 \text{ A}$$

$$V_B = E_a + 120(0.03) \quad E_a = 246.35 \text{ V}$$

$$\frac{E_a}{E_0} = \frac{n}{n_0} \rightarrow \frac{246.35}{250} = \frac{n}{1103}$$



No. \_\_\_\_\_

$$\frac{E_1}{E_2} = \frac{N_1}{N_2}$$

$$L = 200 \quad R_f = 50$$

$$I_A = 126 - \frac{250}{50} = 121$$

$$250 = E_g + 121(0.03) = 246.37 \text{ V}$$

$$\frac{E}{E} = \frac{k \Phi_1 n_1}{k \Phi_2 n_2}$$

$$n_2 = \frac{\Phi_1}{\Phi_2} n_1$$

$$\frac{\Phi_1}{\Phi_2} = \frac{268}{250} = 1.076$$

$$1.076 \times 1103 = 1187 \text{ r/min}$$



Example: [8-4] motor is sep. excited, the motor initially running with  $V_A = 250V$ ,  $I_A = 120A$  and  $n = 1103 \text{ r/min}$  while supplying a constant torque load, what will the speed of this motor be, if  $V_A$  is reduced to  $200V$ ?  $R_A = 0.03$

$$V_A = R_A I_A + E_a$$

$$250 = 0.03(120) + E_a \quad E_a = 246.4$$

$$200 = 0.03(120) + E_a \quad E_a = 196.4 \quad \left[ \begin{array}{l} \text{constant torque} \\ I \text{ constant} \\ \phi \text{ constant} \end{array} \right]$$

$$\frac{196.4}{246.4} = \frac{n}{1103} \quad n = 874.17 \text{ r/min}$$

### The Effect of an Open Field circuit

If the field circuit is open  $\phi$  decrease,  $E_a$  decrease, current  $A \uparrow$  so the Torque  $\uparrow$  and the motor will speed up

### 8.6 THE SERIES DC MOTOR: $V_t = E_a + I_a(R_a + R_p)$

Flux is proportional to  $T = k\phi i = k_c(I_a)^2$

armature current  $\rightarrow \phi = C I_a$

Torque is proportional to  $\left[ \begin{array}{l} \text{the square of } I_a \\ \text{the square of } I_a \end{array} \right]$

series motor give more torque



~~The terminal characteristic~~

The terminal characteristic of series DC motor:

$$V_T = E_a + I_a (R_a + R_p)$$

$$V_T = k \phi \omega_m + \sqrt{\frac{T_m}{k_c}} (R_a + R_p)$$

$$\phi = c I_a$$

$$T_a = \frac{\phi}{c}$$

$$T = k \phi I$$

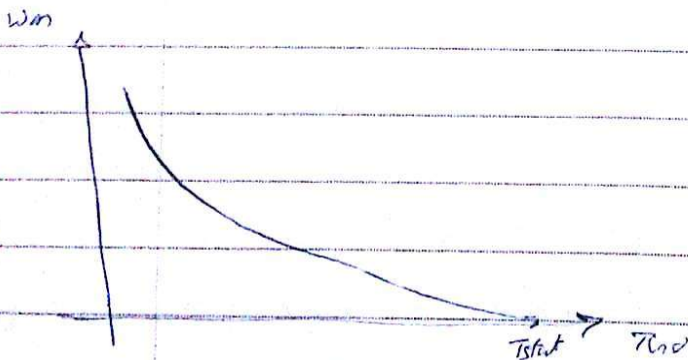
$$T = \frac{k \phi^2}{c}$$

$$\phi = \sqrt{\frac{c T}{k}}$$

$$V_T = k \sqrt{\frac{c T}{k}} \omega_m + \sqrt{\frac{T_m}{k_c}} (R_a + R_p)$$

$$\omega_m = \frac{V_T}{\sqrt{k c}} - \frac{I_a}{\sqrt{T_m}} - \frac{R_a + R_p}{k c}$$

when Torque goes to zero  $\rightarrow$  speed  $\infty$  [never completely unload series motor while running]





N.m =  $\frac{P}{\omega}$

No. \_\_\_\_\_

Example: 250 V series dc motor with compensating winding, and a total series resistance  $R_a + R_s$  of  $0.08 \Omega$ , 25 turns per pole, magnetization curve shown 8-22

1- find the speed and induced voltage torque when  $I_a = 50 A$ .

solution

$$V_B = E_a + I_a (R_{eq})$$

$$250 = E_a + 0.08 (I_a)$$

$$E_a = 246 \text{ V}$$

$$E_a = k \phi \omega_n$$

$$246 = k_c I_a \omega_n$$

$$246 = k_c \times 50 \omega_n$$

$$80 = k_c \times 50 \omega_n$$

$$80 = k_c \phi \omega_n$$

$$246 = k_c E \omega_n$$

$$F = NI = 25 \times 50 = 1250$$

$$E = 80$$

$$\omega_n = 1200$$

$$\omega_n = 3690$$

$$T = k \phi I = k_c (I_a)^2$$

$$T = k_c (50)^2$$

$$T = \frac{E I_a}{\omega_n}$$

$$E = k_c I_a \omega_n$$

$$k_c = \frac{E}{I_a \omega_n}$$

$$T = \frac{E I_a}{\omega_n} = \frac{80 \times 50}{1200 \frac{\text{V}}{\text{min}} \times \frac{\pi}{60}} = \boxed{81.83 \text{ N.m}}$$



## Speed control of series DC motor

insertion a resistor  
in series its wasteful

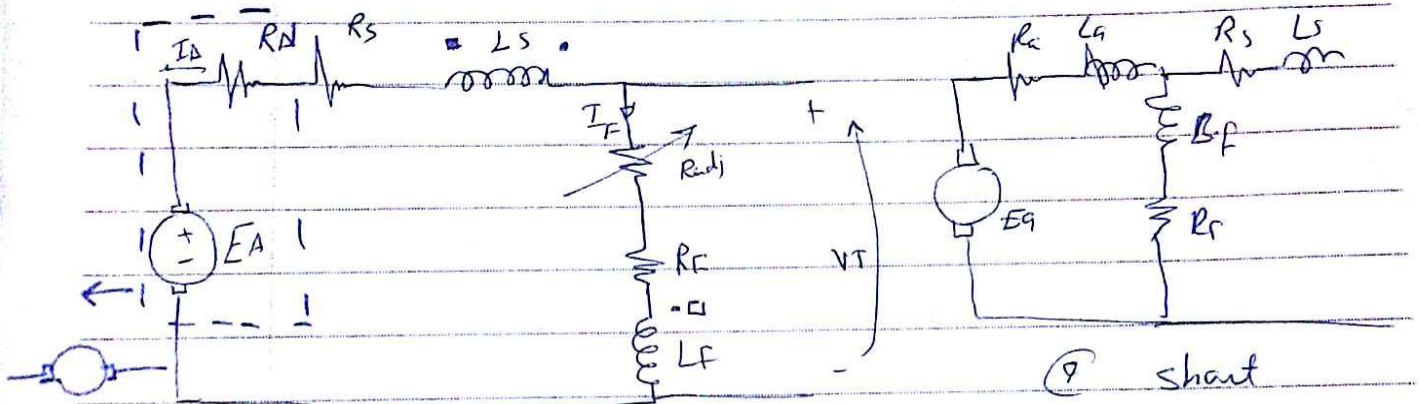
efficient way

change voltage terminals

$$v \uparrow \left( \frac{V_T}{R_c} \frac{1}{V_{end}} \right) \uparrow$$

voltage  $\uparrow$  speed  $\uparrow$

## 8.7 THE COMPOUNDED DC MOTOR: both shunt and series



lap 30

(3) long

① commutative compounding [the current into the dot in both coil (combine) (+)  $\times$  (+) (+)]

② differential compounding  $\ominus$ ,  $\ominus$   $\ominus$  - subtract when  $\ominus$   $\times$  (+)  $\ominus$

$$V_T = E_a + I_A [R_a + R_s]$$

$$I_A = I_L - I_F$$

$$I_F = \frac{V_A}{R_F}$$

$$I_{F_{net}} = I_F \pm I_{SE} - I_{AR}$$

$$I_F^* = I_F \pm \frac{N_S E_a}{N_F} I_A - \frac{I_{AR}}{N_F}$$



The torque - speed characteristic of cumulatively compounded DC-Motor

flux component  $\rightarrow$  constant

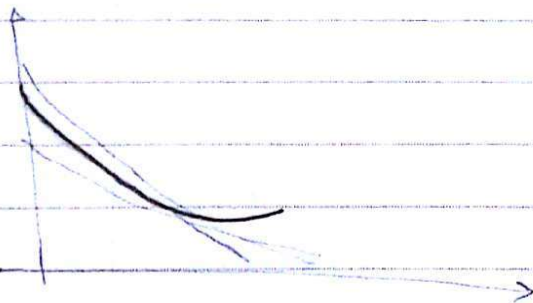
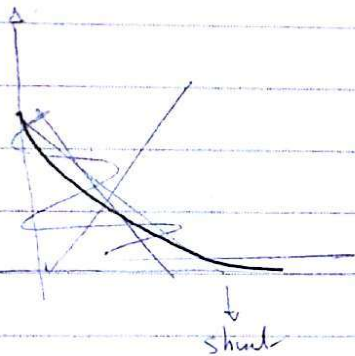
$\rightarrow$  proportional to its armature current [Z is stronger]

\* it has extra torque like series

\* it does not overload on speed at no load (like shunt motor)

at light load it operate like shunt

otherwise it operate as series.



The torque - speed characteristic of differentially compounded DC-Motor.

shunt - series  
mmf mmf

load increase,  $I_a$  increase,  $\phi$  decrease, speed increase,  $E_a$  increase,  $I_a$  decrease

, speed decrease [unstable system].

shunt like DC motor  $\rightarrow$



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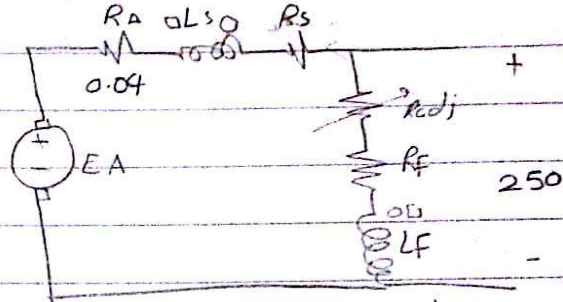
No. \_\_\_\_\_

example: A 100hp. 250V. compounded DC-motor with compensating winding internal resistance of  $0.04 \Omega$   $N=1000$  turns on shunt and 3 turns on series winding. [8-9] ← At no load field resistor has been adjusted to make the motor run at 1200 r/min [losses neglected]

a) what is shunt field current in this machine at no load?

at no load,  $I_a = 0$

$250 \text{ V}$   
 $J, 51 \rightarrow 5 \text{ A}$



b)  $I_a = 200 \text{ A}$ , find speed? cumulatively compounded

$$250 = E_a + 200(0.04)$$

$$E_a = 242$$

$$I_f^* = 5 + \frac{3}{1000}(200) = 5.6 \text{ A}$$

$$E = 252.5$$

$$\frac{242}{252} = \frac{n}{1200} \quad n = 1108 \text{ r/min}$$

c)  $I_a = 200 \text{ A}$ , diff comp find speed??

$$250 = E_a + 200(0.04) \quad E_a = 242 \quad n = ??$$

$$I_f^* = 5 - \frac{3}{1000}(200) + 0 = 4.4$$

$$E = 236 \quad n = 1200$$

$$n = 1230.5$$





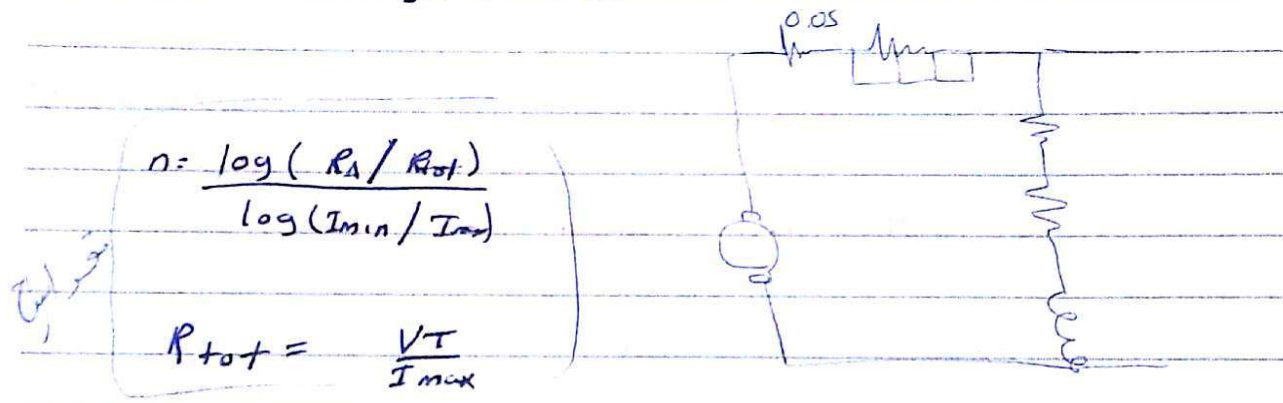


No. \_\_\_\_\_

example: 100hp, 250V, 350A shunt dc motor  $R_A = 0.05 \Omega$ .

We wish to design a starter circuit for this motor which will limit the maximum starting current to twice its rated value and will switch off section when current falls to its rated value.

1) how many stage of starting resistance i need to limit the current to range specified



$$R_{tot} = \frac{250}{I_{max}}$$

$$I_{max} = \frac{250}{0.05}$$

$$I_2 = 2I_1 \quad \frac{I_2}{I_1} = 2$$

$$\frac{I_2}{350} = 2 \quad I_2 = 700$$

$$R_{tot} = \frac{250}{700} = 0.357$$

$$n = 2.836 = 3 \text{ resistor}$$



b) what value of each segment of resistor be? At what voltage should each stage of the starting resistance be cutout??

$$I = \frac{V}{R_A + R_1 + R_2 + R_3}$$

$$700 = \frac{250}{R_A + R_1 + R_2 + R_3}$$

$$R_A + R_1 + R_2 + R_3 = 0.357$$

~~$$E_A$$~~ 
$$V_A = E_A + RI$$

$$250 - 0.357(350) = E_A$$

$$E_A = 125 \rightarrow I_A \text{ has fallen to } 350 \text{ A}$$

and it's the time to cut the ~~first~~ first

starting (current must jump to 700)

$$250 - ( \quad )(700) = 125$$

$$R = 0.1785 \Omega \} \text{ total } R \text{ in ckt to}$$

fall to 350 A

$E_A$  reaches

$$E_A = 250 - 350(0.1785) = 187.5$$

fall to 350 it's time

to cut the second one

$$187.5 = 250 - 700(R)$$

$$R = 0.0892 \Omega$$

$$E_A = 250 - 350(0.0892) = 218.75$$

time to cut the third one

$$R_3 = 0.0446 \Omega$$

$$E_A = 250 - 700(0.0446) = 219$$

~~$$E_A = 234.30$$~~



No. \_\_\_\_\_

$$I_a = \frac{VT - EA}{R_a} = 625 = \frac{250 - 218.75}{0.05}$$

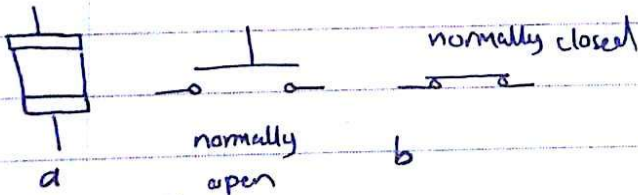
$$R_1 = R_{tot} - R_2 - R_3 - R_a = 0.357 - 0.1786 - 0.0393 - 0.05 = 0.1071$$

$$R_2 = R_{tot} - R_3 - R_a = 0.0893$$

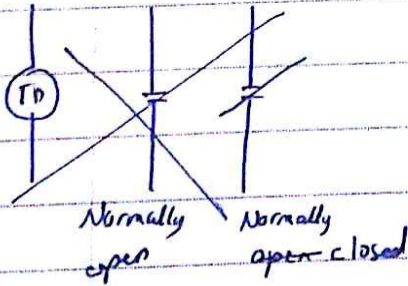
$$R_3 = R_{tot3} - R_a = 0.0893 - 0.05 = 0.0393$$

### DC Motor starting circuits:

fuses → to protect the ckt from short ckt. (طابعی فی شورن سیرکت بنجھونو مجزیہ) (سیرکت حقن طابعی برا اعلان)

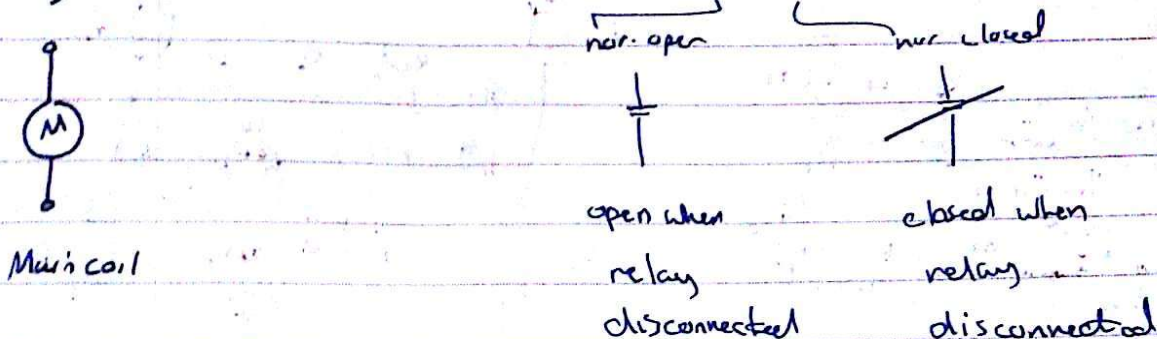


spring type → normally open → closed when the button pushed  
 → normally closed → open →



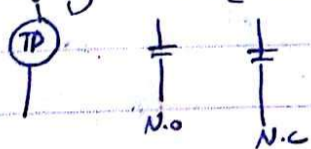


relay consist of Main coil and some contact



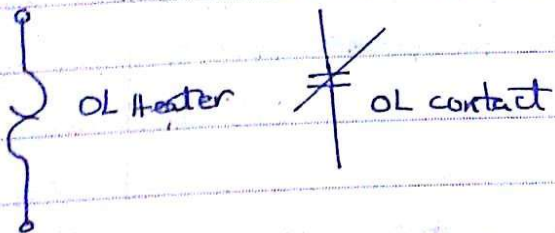
power → relay connect → switch st change.

Time delay relay [ ... ]

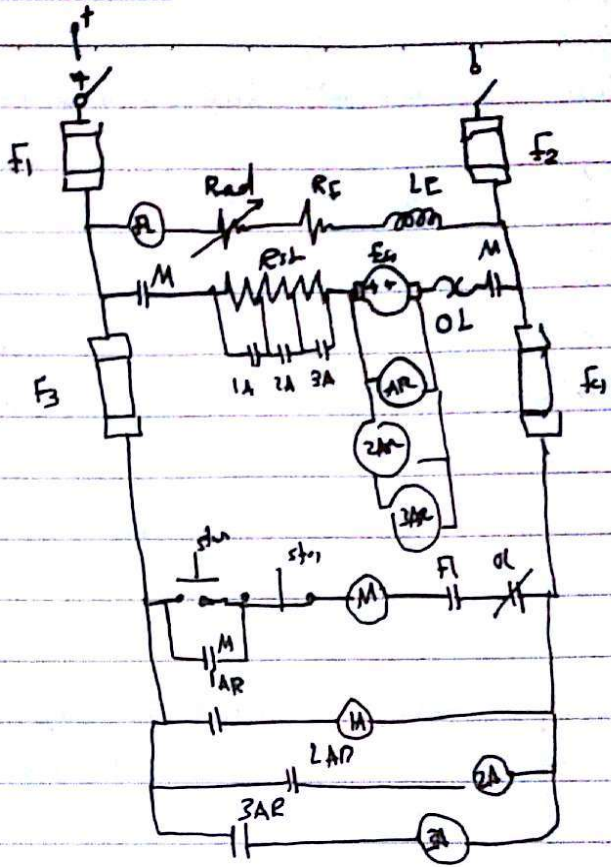
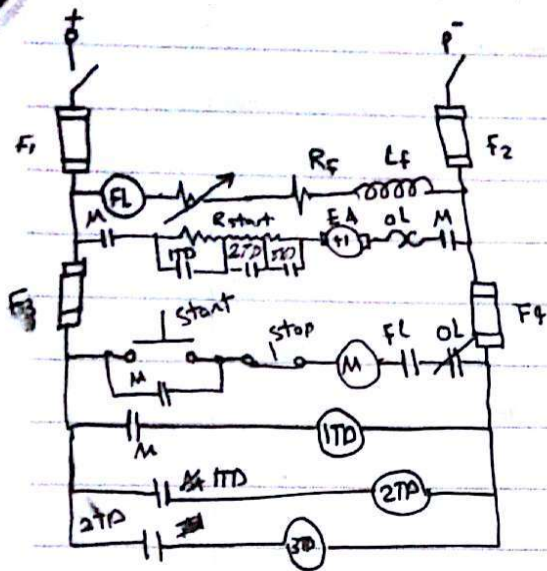


Overload [ consist of heater coil and some shut contacts ]

load etc → heater coil heat the coil heater up → shut contact







\* serial of Time relay  
 remove Resistance at the correct  
 time after the power applied  
 supply.

لقد كان الـ ITD يفتح الـ contact  
 ويستمر الـ جزئياً  
 resistor  
 الـ full load

its better than the previous

**FL** → Field loss relay.

إذا انقطع التيار ففقدت سبب من انه يناد على الـ field  
 ويستعمل الـ power supply ويستعمل الـ power supply  
 إذا الـ field current

الـ Heater ويستعمل الـ OL  
 الـ M relay ويستعمل الـ power supply  
 الـ load



## 8.10 DC MOTOR EFFICIENCY CALCULATION:

copper losses  $I^2R \rightarrow$ Resistance of stator  
rotor & Block loss  
 $\frac{\text{Voltage}}{\text{current}}$  of  $\mu\Omega$ 

Why the Resistance should be equal to full load? because it varies with temperature and full load will be near the operating temperature.

The resulting resistance are not accurate:

- 1- The cooling that normally occurs when the motor is spinning will not be present
- 2- there is an ac-voltage in rotor conductors during normal operation, they suffer from some amount of skin effect, which further raises armature resistance.

$$\text{Brush drop} = V_{BD} \cdot I_A$$

turn freely - no load  $\xrightarrow{\text{rated speed}}$  no output power

no load  $\rightarrow I_A$  small  $\rightarrow$  copper losses neg.



Example: A 50 HP, 250V, 1200 r/min shunt dc motor, has a rated armature current at **IA 170A** and a rated field current of 5A. When the rotor is blocked an armature voltage of 10.2V produce 170A of current flow, and field voltage of 250V produce a field current flow of 5A. voltage drop of brush is 2V. at no load with terminal voltage equal to 240V. the armature current is 13.2A. the field current is 4.8A. the motor speed is 1150 r/min

a) power is output at rated condition      2) efficiency.

$$R_A = \frac{V}{A} = \frac{10.2}{170} = 0.06 \Omega$$



$$R_F = \frac{V}{A} = \frac{250}{5} = 50 \Omega$$

$$\text{armature losses} = (170)^2 \times 0.06 = 1734 \text{ W}$$

$$\text{field losses} = (5)^2 \times 50 = 1250 \text{ W}$$

$$\text{Brush losses} = V_{bd} \times I_A = 2 \times 170 = 340 \text{ W}$$

$$P_{\text{tot}} = P_{\text{core}} + P_{\text{mech}} = 240 \times 13.2 = 3168 \text{ W}$$

a) power output =  $P_{\text{in}} - P_{\text{loss}}$

$$(240)(13.2) - P_{\text{core}} - P_{\text{mech}} - P_{\text{arm}} - P_{\text{field}} - P_{\text{brush}} = (0.6 \times 4.3750)$$

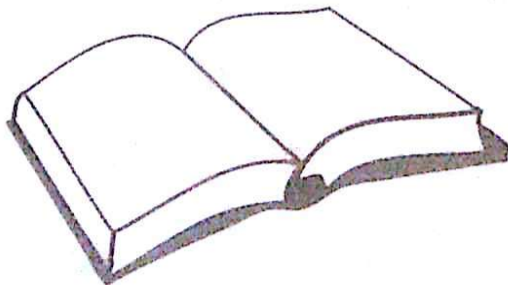
$$= 3682.05$$

②  $\eta = \frac{\text{output}}{\text{input}} = 29.23\%$





مَنْ لَمْ يَحْتَمِلْ ذُلَّ الْعِلْمِ سَاعَةً  
بَقِيَ فِي ذُلِّ الْجَهْلِ أَبَدًا



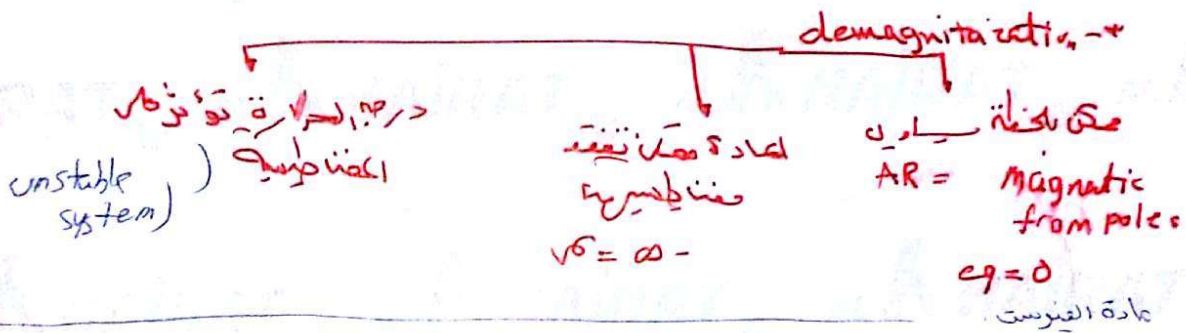


AC voltage apply on DC motor  
it will doesn't work

Permanent magnetic circuit:

اجابياتها  
مغناطيسية

- 1- لا يمكن ان يكون به احد طرفي حثا
- 2- الحثية مادة موصلة صلبة لا تتغير



## TRANSFORMER: "chapter two"

2.1 why transformer are important to modern life:

→ high current causes huge voltage drop in transmission line.

→ transformer step up voltage and decrease the current to keep the power constant (into equal out put device) so the electrical power can be generated over a long distance at very low losses (losses will not affect high voltage) then it step down for final usage.

$P$  proportional to  $I^2 R$  ← الخسائر

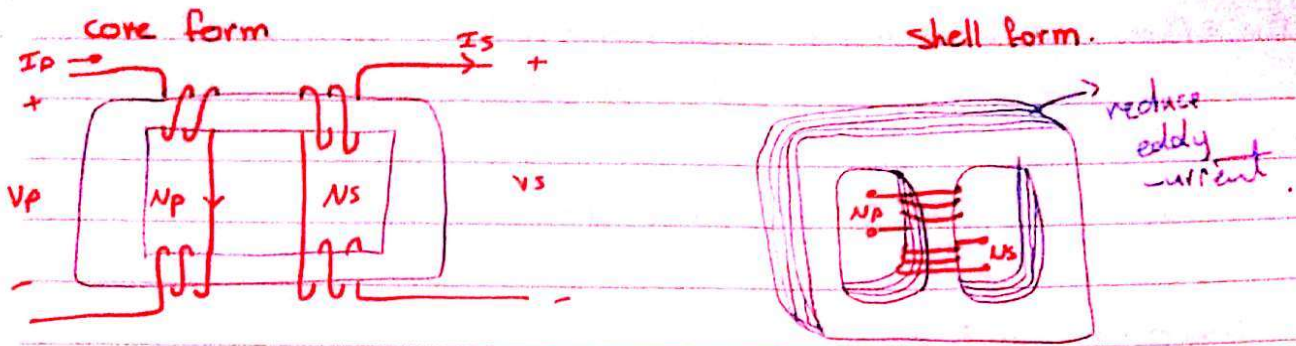
when the voltage increase and decrease the current the electric power will decrease twice.

step up range (110kwatt - 100k) → 120 V for safety usage  
step down (12 545kw)

AC voltage  
same frequency



## 2.2 type and construction of transformers



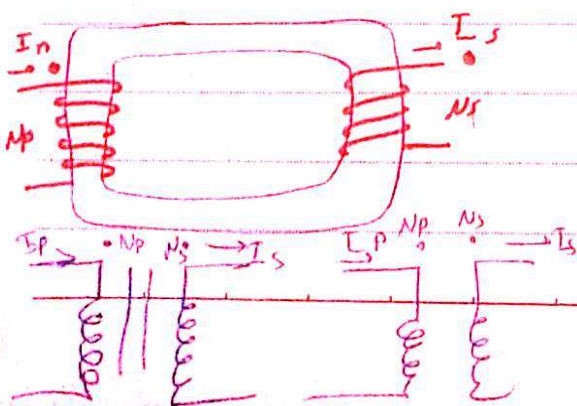
The primary and secondary winding is one on top of the other with low voltage :-

- ① to simplify the problem of insulating the high voltage winding from the core
- ② less leakage losses

name of transformer due to their usage :-

- ① auto (unit) transformer → step up voltage
- ② substation transformer → step down voltage
- ③ distribution transformer → take the distribution and step it down to 220, 110.
- ④ potential transformer → sample high voltage to low sec voltage [small current]
- ⑤ power transformer → also produce sec voltage proportional to prim voltage
- ⑥ current transformer → provide sec current smaller than prim current

## 2.3 the ideal transformer



relationship between the voltage  $V_p$  and  $V_s$

$$\frac{V_p}{V_s} = \frac{N_p}{N_s} = q \text{ (turns ratio)}$$

$$\frac{I_p}{I_s} = \frac{1}{q}$$



= (dot convention) polarity  $\rightarrow$   $\rightarrow$

- 1 - If the voltage is positive at the dotted end in primary side it will be positive at the dotted end of the secondary side
- 2 - If the current is flow in ~~total~~ to dotted side at primary, it will flow out of the dotted side at the secondary side.

Power in Ideal transformer :-

$$- \text{power} = \text{pin}$$

$$V_{pri} I_{pri} \cos \theta_p = V_{sec} I_{sec} \cos \theta_s$$

$$\theta_p = \theta_s = 0$$

$$\rightarrow V_p I_p = V_s I_s$$

total power  $\rightarrow$  Real power  $\rightarrow$  power factor  $(\cos \theta, \sin \theta)$

$$- S_{in} = S_{out}$$

$$V_p I_p \sin \theta_p = V_s I_s \sin \theta_s \rightarrow V_p I_p = V_s I_s$$

a  $\left\{ \begin{array}{l} > 1 \text{ step down} \\ < 1 \text{ step up} \end{array} \right.$

Impedance Transformation through Transformer

$$Z_L = \frac{V_p}{I_p} \text{ or } \frac{V_s}{I_s} \rightarrow \text{transformer change of voltage and current so}$$

$$Z'_L = a^2 Z_L \text{ [apparent impedance in primary]}$$

$$= a^2 \frac{V_p}{I_p}$$



## Analysis of circuit containing Ideal transformers:

replace the transformer with equivalent ckt,

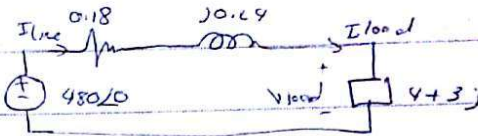
↳ reflecting → Replacing one side of transformer with its equivalent of other side's voltage level

How to do equivalent ckt??

$$\rightarrow \boxed{\frac{V_P}{V_S} = a} \quad \boxed{Z_L' = a^2 Z_L} \quad \text{polarity reversed direction}$$

Example 2.1: A single phase power system consists of 480-V 60Hz generator supplying a load  $Z_{load} = 4 + 3i \Omega$  through a transmission line of impedance  $Z_{line} = 0.18 + 0.24i \Omega$ .

a) what will the voltage at the load be?



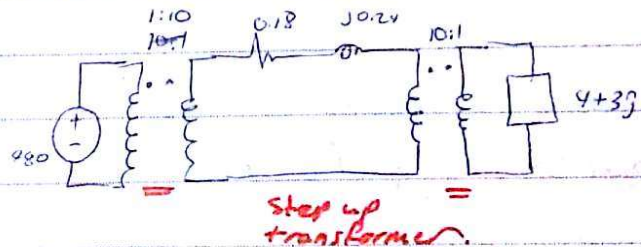
↳ what transmission losses be??

**solution**  $480 = [0.18 + 4 + 3j + 0.24i] I \quad I = 90.8 \angle -37.8^\circ \text{ A}$

$$V_{load} = I \times (4 + 3i) = 453.8 \angle 10.91^\circ \text{ V}$$

$$\text{transmission losses} = I^2 R = 1489.0352 \text{ watt}$$

b) what will the load voltage be, and transmission losses??



$$Z'_{load} = a^2 Z_L$$

$$\left(\frac{10}{1}\right)^2 (4 + 3i) = 400 + 300i$$

$$Z_{eq} = 400 + 0.18 + 300i + 0.24i = 500.3 \angle 36.87^\circ \Omega$$

$$Z'_{eq} = \frac{1}{a^2} (400.18 + i300.24) = 5.003 \angle 36.87^\circ \Omega$$

$$I_G = \frac{480}{Z'_{eq}} = 95.94 \angle -36.87^\circ \text{ A}$$

$$N_p I_G = N_s I_{line}$$

$$I_{line} = \frac{1}{10} (95.94 \angle -36.87^\circ \text{ A}) = 9.594 \angle -36.87^\circ \text{ A}$$







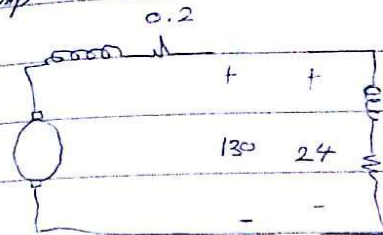
Example: Separately excited DC-motor is rotated at 1000 rpm. under no load condition

$I_f$	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8
$V_T$	0	30	60	85	102	115	124 122	130	134

$V_f = 24$ ,  $R_f$  is adjustable,  $R_a = 0.2$ ,  $V_a = 130$ .

1) field current at no load with 1000 rpm

at  $V_T = 130$   $I_f = 0.7A$



2) motor drives a load at 1200 rpm. Calculate the armature voltage at 1200 rpm if the field Resistance  $R_f = 60\Omega$

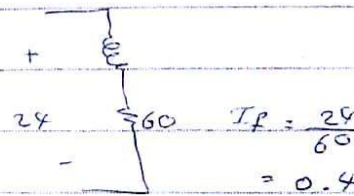
$$E_a = k\phi 1200$$

$$E_a = k\phi 1000$$

$$\frac{E_a}{102} = 1.2$$

$$E_a = 122.4$$

$$E_a = 102$$



3) torque for above condition

$$T = \frac{E_a I_a}{\omega} = \frac{122.4 \times I_a}{1200 \left(\frac{2\pi}{60}\right)} = 37 \text{ N.m}$$

$$122.4 = 130 - I_a(0.2)$$

$$I_a = 38 \text{ A}$$

4) Motor supplies Mechanical load of 4000W at 1450rpm the mechanical losses are 160W calculate efficiency

$$\frac{4000}{4000 + 160 + I_a^2 R_a + I_a I_f R_f}$$

power converted = 4000 + 160 = 4160

$$V T I_a = E_a I_a + I_a^2 R_a$$

$$0.3 I_a^2 + 130 I_a + 4160$$

$$I_a = 33.75$$

$$E_a = 123.25 \times 4160$$



No.

$$E_a = E_a$$

$$E_a = k\phi \omega n$$

$$\frac{123.25}{E_a} = \frac{1450}{1000}$$

$$E_a = 85.006$$

$$I_f = 0.3$$

$$P_{input} = (0.3) \times 24$$

$$\frac{24}{0.3} = \frac{0.3 R}{0.3} \quad R = 80$$

$$80(0.3)^2 + 0.2(33.74)^2 + 160 + 4000 = 4345$$

$$\frac{4000}{4345} \times 100\% = 91\%$$

A series DC motor has a combined armature and field resistance of  $R_A + R_S = 1.2 \Omega$ .  $V_T = 48V$ , torque develops  $1500 Nm$

(1) armature current and  $k_c$ .

(2) torque when speed is  $500 rpm$

(3) output power and efficiency when operating  $500 rpm$  (neglect mechanical losses)

$$(i) I = \frac{48}{1.2} = 40 A$$

$$T = k_c (I_a)^2 \quad k_c = 0.9375$$

(ii)

$$T = 0.9375(I)^2 \approx 0.764 N.m \quad E_a = \frac{k\phi}{0.9375(500)} = 468.75$$

$$468.75 = 48 - I_a(1.2)$$

$$\text{out put Power} = T\omega = 41.67$$

$$I_a = 0.9$$

power input

$$\eta = \frac{E_a I_a}{V_T I_a} = 49.08$$



Mechanical Power =  $E_a \cdot I_a$   
induced

No.

$$\frac{500 \times \pi}{60} = \frac{50 \pi}{3}$$

$$T = 0.9375 (I_a)^2$$

$$E_a = k \phi \omega_n \quad \phi = c I_a$$

$$E_a = k_c I_a \frac{50 \pi}{3}$$

$$E_a = 49.08 I_a$$

$$48 = 49.08 I_a + I_a (1.2) \quad I_a = 0.955 A$$

$$T = 0.854 \text{ N.m}$$

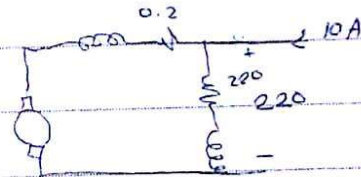
$$p = \frac{E_a I_a}{V T I_a} = \frac{49.08 (0.955)}{48} = 97.6\%$$

A 220 V shunt motor has armature and field resistance of 0.2  $\Omega$  and 220 respectively. The motor is driving a constant load torque and running at 1000 rpm drawing 10 A current from the supply. Calculate the new speed and armature current if an external armature resistance of 5  $\Omega$  is inserted. Neglect armature reaction.

Solution

$$I_f = \frac{220}{220} = 1 A$$

$$I_a = 9 A$$



$$220 = 5.2(9) + E_a \quad E_a = 173.2 \rightarrow \omega = ??$$

$$220 = 0.2(9) + E_a \quad E_a = 218.2 \quad 1000$$

$$n = 793.76 \text{ rpm}$$

220 V shunt motor has  $R_A = 0.2$   $R_f = 220$ . The motor is driving load torque  $T \propto \omega^2$  and running at 1000 rpm drawing 10 A from supply. Calculate torque when 5  $\Omega$  is inserted in armature ckt.

$$I_a = 10 - \frac{220}{220} = 9 A$$

$$220 = 0.2(9) + E_a \quad E_a = 218.2$$





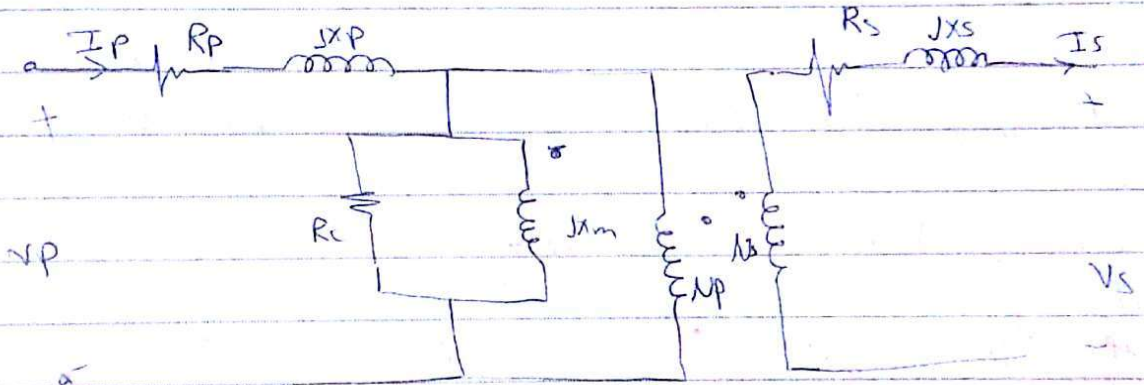
$$e_{Lp}(t) = L_p \frac{di_p}{dt} \quad e_{Ls}(t) = L_s \frac{di_s}{dt}$$

$L_p = N_p^2 \Phi$  → leakage inductance in primary

$I_m$  (magnetization current) proportional to  $V$  and lagging it by  $90^\circ$

so we can represent it by  $X_m$  in primary voltage.   
 (voltage in the core) connected across

(hysteresis and eddy current)  $I_{h+c}$  proportional to  $V$  and in phase with it   
 so it modeled as  $R_c$  connected across the p.p. voltage.

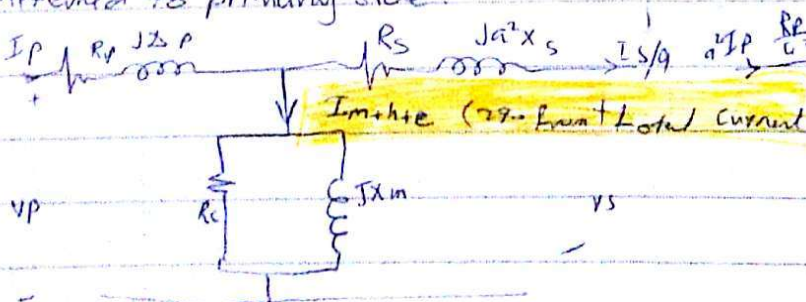


$x_p = \omega L_p$        $x_s = \omega L_s$   
 reactance due to primary      reactance due to secondary

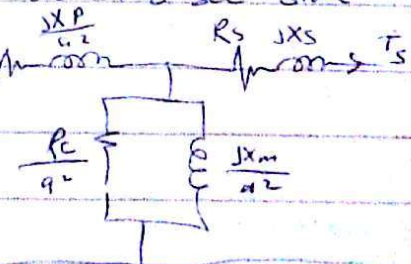
$$\left( \frac{V_p}{V_s} = a \right)$$

Red Box

Referred to primary side:



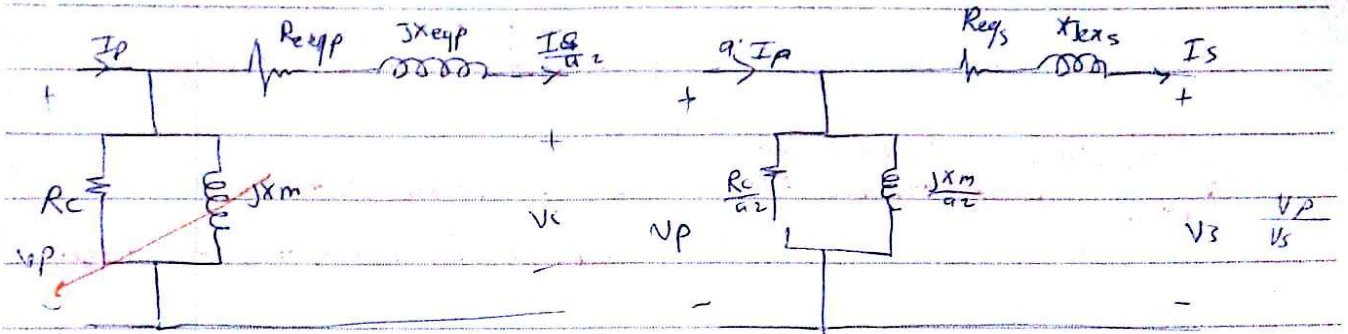
Referred to sec side





Approximate Equivalent ckt of a Transformer:

because excitation current ( $I_m$  or  $I_w$ ) is 2-3% of total current ckt. can be simplified.

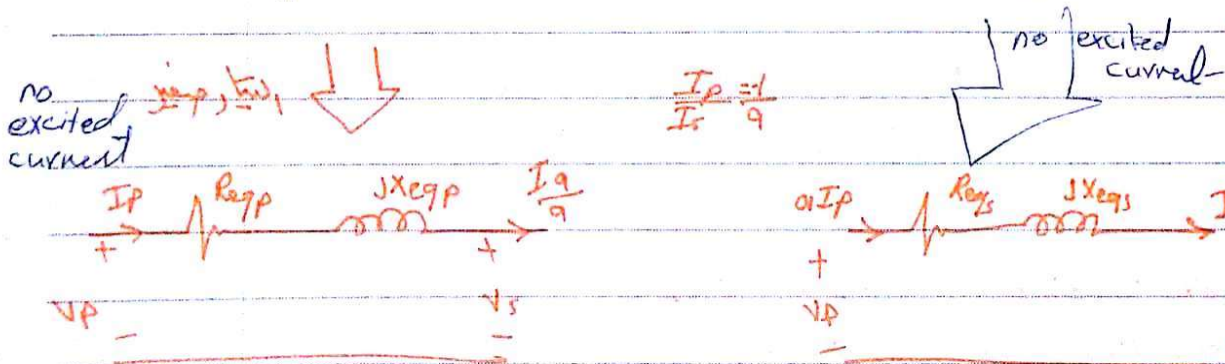


$$R_{eqp} = a^2 R_s + R_p$$

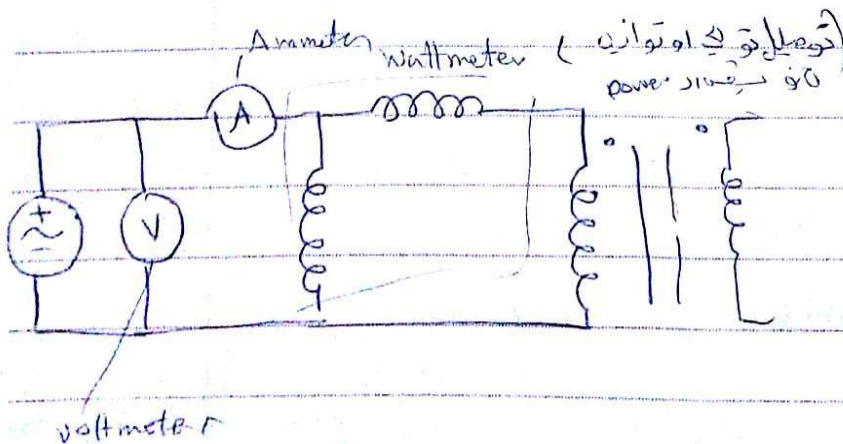
$$jX_{eqp} = a^2 jX_s + jX_p$$

$$R_{eqs} = \frac{R_p}{a^2} + R_s$$

$$jX_{eqs} = \frac{jX_p}{a^2} + jX_s$$



Determine the value of components in transformer models:





$I_{zero}$   $V_{maximum}$  No.

[1] Open ckt test [low voltage side]  
 Rated low voltage

auto Rapp. lkt excitation  $I_{exc}$ ,  $V_{exc}$  [to High voltage side]  $I_{exc}$ ,  $V_{exc}$  Full line voltage  
 P<sub>exc</sub> Branch  
 [P<sub>exc</sub> on primary]  
 magnitude for excitation Power factor  
 Impedance

$$G_c = \frac{1}{R_c} \quad B_m = \frac{1}{X_m}$$

$V_{rated} = V_{open}$   
 ckt.

$$G_c = \frac{I_{0.c} \cos \phi}{V_{0.c}} \quad B_m = \frac{I_{0.c} \sin \phi}{V_{0.c}}$$

(2)  $\phi = \cos^{-1} \frac{P_{0.c}}{V_{0.c} I_{0.c}}$

(1)  $I_{0.c}$   
 $P_{0.c}$   
 $V_{0.c}$

Referred to low Voltage side [  $I_{exc}$  ]

$a^2 >$   $V_{exc}$  primary side

[2] Short ckt test [to High voltage side]  $V_{sc}$ ,  $I_{sc}$   
 $V_{sc} = 0$   $I_{maximum}$  rated low voltage value

low voltage wt transformer is shorted

elements  $I_{sc}$  losses  $V_{sc}$ ,  $I_{sc}$  excitation Branch

$$|Z_{sc}| = \frac{V_{sc}}{I_{sc}} \cos \phi$$

$I_{rated} = I_{short}$   
 ckt

$$\phi = \cos^{-1} \frac{P_{sc}}{V_{sc} I_{sc}}$$

$$R_{eq} = Z_{sc} \cos \phi$$

$$X_{m eq} = Z_{sc} \sin \phi$$

Referred to high voltage side



Example 2-2: The equivalent circuit impedances of a 20 kVA, 8000/240 V, 60 Hz transformer are to be determined. The open circuit test was performed on the secondary side of transformer, and short circuit test were performed on the primary side.

Open circuit test

$$V_{oc} = 240 \text{ V}$$

$$I_{op} = 7.133 \text{ A}$$

$$W_{oc} = 400 \text{ W}$$

Short circuit test

$$V_{sc} = 489 \text{ V}$$

$$I_{sc} = 2.5 \text{ A}$$

$$P_{sc} = 240 \text{ W}$$

Find the impedances of

the approximate equivalent circuit referred to the primary side, and sketch the circuit.

Solution:

Open ckt [low voltage source]

$$\phi = \cos^{-1} \frac{400}{240 \cdot 7.133} = 76.48^\circ$$

$$Y_E = \frac{7.133}{240} = 0.0297 \angle -76.5^\circ \rightarrow 6.933 \times 10^{-3} - 0.028879j$$

$$R_c = \frac{1}{0.0297}$$

$$R_c = \frac{1}{6.933 \times 10^{-3}} = 144.23 \Omega \rightarrow (33.33)^2 \cdot 144.23 = 159.9 \text{ k}\Omega$$

$$X_m = \frac{1}{0.02887} = 34.63 \Omega \quad (33.33)^2 \times 34.63 = 38.97 \text{ k}\Omega$$

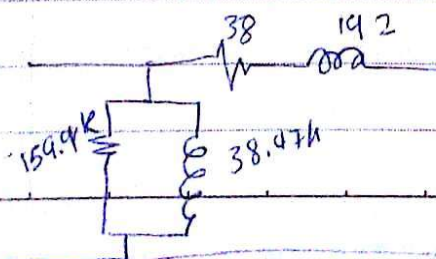
PF = Shorted

$$PF = \frac{240}{489 \cdot 2.5}$$

$$\phi = 78.67^\circ$$

$$Z_{eq} = \frac{489}{2.5} \angle \cos^{-1} \phi = 38.42 + j191.78 \Omega$$

$\downarrow$                        $\downarrow$   
 $R_{SE}$                        $X_{SE}$





### 2.7 transformer voltage regulation and efficiency:

output voltage dependent on the load impedance even if input voltage is constant

$$\text{Voltage regulation} \rightarrow \frac{V_{s \text{ no load}} - V_{s \text{ full load}}}{V_{s \text{ full load}}} \times 100\% \quad \frac{V_p}{V_s}$$

$$\frac{V_p}{V_s} = \frac{V_{s \text{ full load}}}{V_{s \text{ full load}}} \times 100\%$$

high VR and Impedance reduce the fault current in ct.

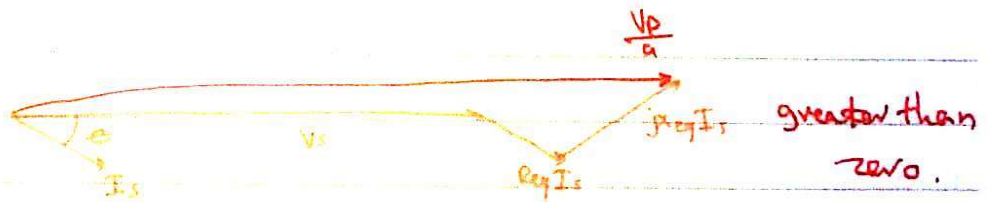
how to determine voltage regulation

it depends on the impedances and the angle of current flow in the transformer

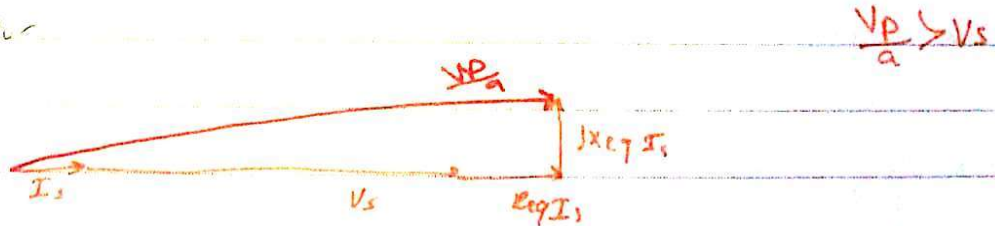
by drawing phasor diagram.  $\phi = \text{angle } 0^\circ$  and all element compare with it

$$\frac{V_p}{V_s} = V_s + R_{eq} I_s + jX_{eq} I_s$$

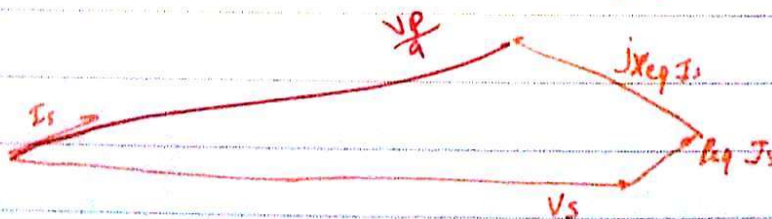
with lagging PF



unity power factor



leading PF





Transformer Efficiency → transformer also compared by their efficiency

$$P = \frac{P_{out}}{P_{in}} \times 100\%$$

} copper losses  
 } eddy current losses  
 } hysteresis losses

$$\eta = \frac{V_s I_s \cos \phi}{P_{cu} + P_{core} + V_s I_s \cos \phi} \times 100\%$$

Example: A 5KVA, 2300/230V transformer is to be tested to determine the excitation branch component, its series impedances, and its voltage regulation

Open circuit test  
(low voltage side)

$V_{oc} = 230V$   
 $I_{oc} = 2.1 A$   
 $W_{oc} = 50W$

short circuit test  
(high voltage side)

$V_{sc} = 87V$   
 $I_{sc} = 6 A$   
 $W_{sc} = 160W$

a) Find the equivalent circuit referred to high voltage side

short ckt

$$\phi = \cos^{-1} \frac{160}{230 \times 2.1} = 55.43$$

open ckt

$$\phi = \frac{50}{230 \times 2.1} = 84.05$$

$$Z_{eq} = \frac{87}{6}$$

$$= \frac{4.94 + j6.45}{R_{sc} \quad X_{sc}}$$

$$Y_{eq} = 9.95 \times 10^{-4} + j9.08 \times 10^{-3}$$

$$R_c = 105.82 \quad \uparrow \quad Y_m = 110.13$$

$$R_{sc} \text{ referred to HV} = \left( \frac{2300}{230} \right)^2 105.82$$

$$Y_m = 110.13$$



b) Find the equivalent ct due to low voltage side

$$R_{SE} = \frac{4.95}{100} = 0.0495$$

$$X_{SE} = \frac{6.45}{100} = 0.0645$$

c) calculate the full load voltage regulation at 0.8 lagging PF, 1 pf and 0.8 leading PF using the exact equations for  $V_P$

$$VR = \frac{V_s \text{ no load} - V_s \text{ full load}}{V_s \text{ full load}} \times 100\%$$

$$I_s = \frac{P_s}{R_s V_s} = \frac{15000}{230} = 65.2$$

$$\frac{V_P}{a} = V_s + R_{eq} I_s + X_{eq} I_s$$

$$230 + 0.0495 \cdot 65.2 / 36.86 + j0.0645 / 56.86 - 0.8 = 0 - j0$$

$$\frac{V_P}{a} = 229.85 \quad 230.85 / 0.90V \quad VR = 2.1\%$$

$$\frac{V_P}{a} = 230 + 0.0495 (65.2 / 0) + j0.0645 / 65.2 \quad 1 = 0 - \phi$$

$$= 232.93 / 1.03$$

$$VR = \frac{232.93 - 230}{230} = 1.3\%$$

$$\frac{V_P}{a} = 230 + 0.0495 (65.2 / 36.86) + j0.0645 (65.2 / 36.86)$$

$$\frac{V_P}{a} = 229.85 / 1.2$$

$$VR = \frac{229.85 - 230}{230} = -0.065\%$$

d) efficiency at the transformer at full load with PF = 0.8 lagging

$$\eta = \frac{V_s I_s \cos \phi}{V_s I_s + P_{cu} + P_{core}}$$

$$V_s I_s + P_{cu} + P_{core}$$



$$P_{cu} = (I_s)^2 R_{eq}$$

$$0.0445 \times \left( \frac{15000}{230} \right)^2 = 189W$$

$$P_{core} = \frac{(V_P/4)^2}{R_C} = \frac{(234.85)^2}{1050} = 52.52$$

$$V_P = 230 + 0.0445 \left( \frac{15000}{230} \right)^2 \times 0.0643 \left( \frac{15000}{230} \right)^2 \cos^{-1} 0.8$$

$$V_s I_s \cos \phi = 230 \times 656.2 \times 0.8 = 11998.35$$

$$\frac{11998.35}{11998.35 + 52.52 + 189} = 98\%$$

## 2.8 TRANSFORMER TAPS AND VOLTAGE REGULATION

Distribution transformer [2.5% - +5%]

example 500 kVA, 13200 / 480 V distribution transformer has four 2.5 percent taps on its primary winding. what is voltage ratio for the transformer per tap setting

5%  $13860 / 480 V$

2.5%  $13530 / 480 V$

norm  $13200 / 480 V$

-2.5%  $12870 / 480 V$

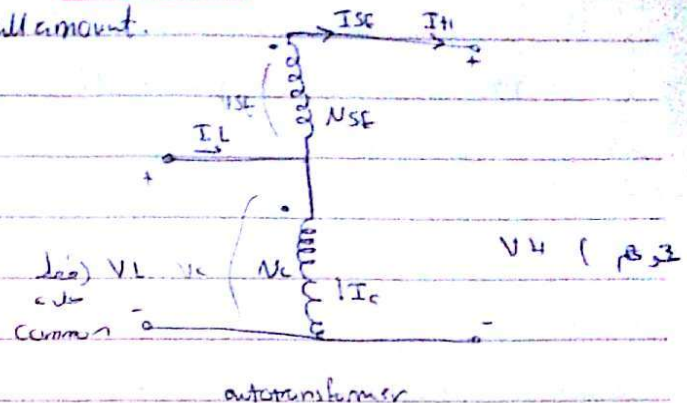
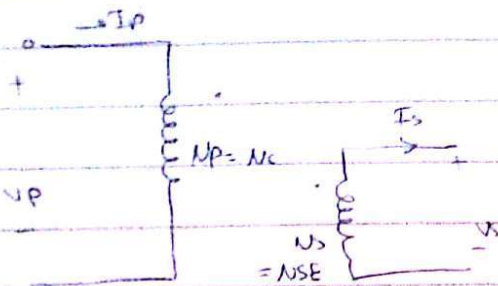
-5%  $12540 / 480 V$



## 2.9 THE AUTOTRANSFORMER:

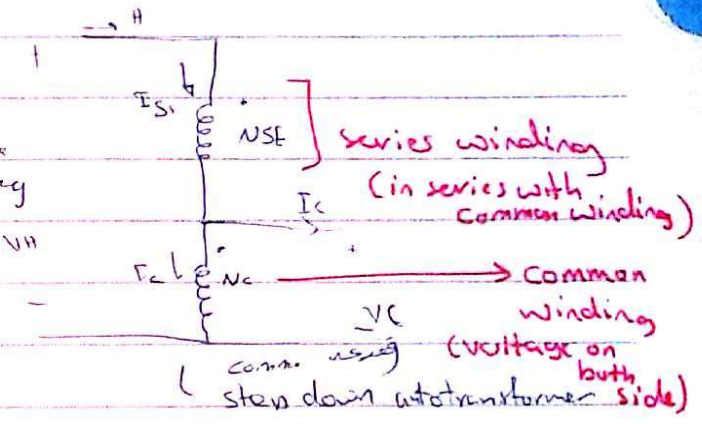
self-study.

Use to change voltage level by a small amount.



connected in the conventional manner

total voltage =  $V_{on \text{ first winding}} + V_{on \text{ sec winding}}$   
 output input



Primary side where the power into it

depending on it step up or down

$I_L = I_{SE} + I_C$

$V_H = V_C + V_{SE}$

$I_H = I_{SE}$

$V_L = V_C$

$I_C N_C = I_{SE} N_{SE}$

$\frac{V_C}{V_{SE}} = \frac{N_C}{N_{SE}}$

$\frac{V_L}{V_H} = \frac{N_C}{N_{SE} + N_C}$

$\frac{I_L}{I_H} = \frac{N_{SE} + N_C}{N_C}$



**Apparent Power in transformer:** [Not all power travelling in the winding]

$$P_L = \frac{S_{10}}{S_w} = \frac{N_E S + N_C}{N_E S}$$

power  
enter prim  
leave sec

power  
travelling  
in winding

Example: 100 VA, 120/12-V transformer is to be connected so as to form a step up autotransformer  $V_p = 120$  is applied to transformer.

D) secondary voltage

E) maximum volt amp rating in this mode of operation

F) rating advantage of autotransformer connection over the transformer rating conventional at 120/12-V operation.

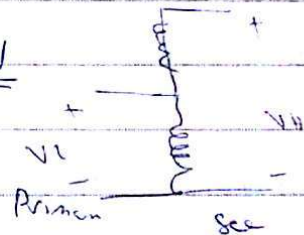
Solution:

$$\frac{I_H}{V_H} = \frac{N_C}{N_E S + N_C}$$

$$V_H = \frac{12 + 120}{12} \times 120$$

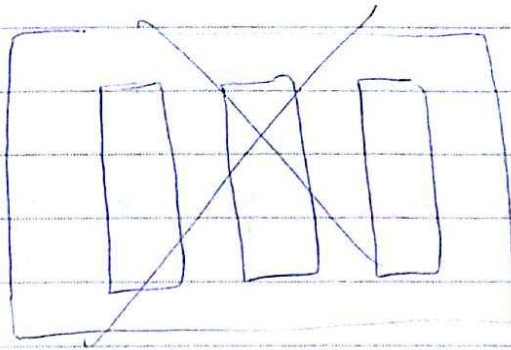
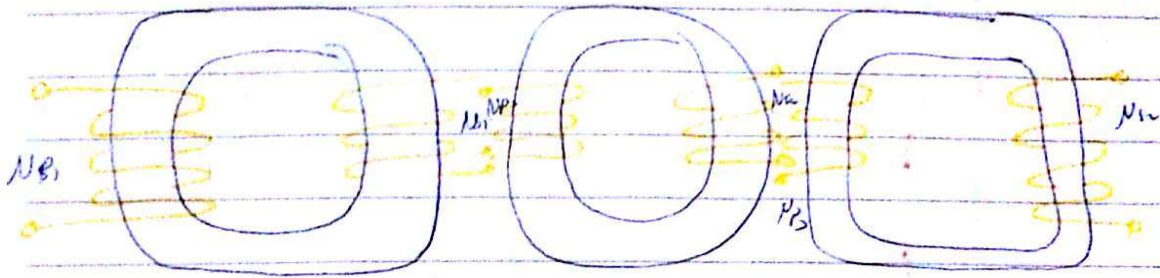
$$\underline{V_H = 132 \text{ V}}$$

$$I = \frac{P_{max}}{V} = \frac{100}{12} = 8.33$$

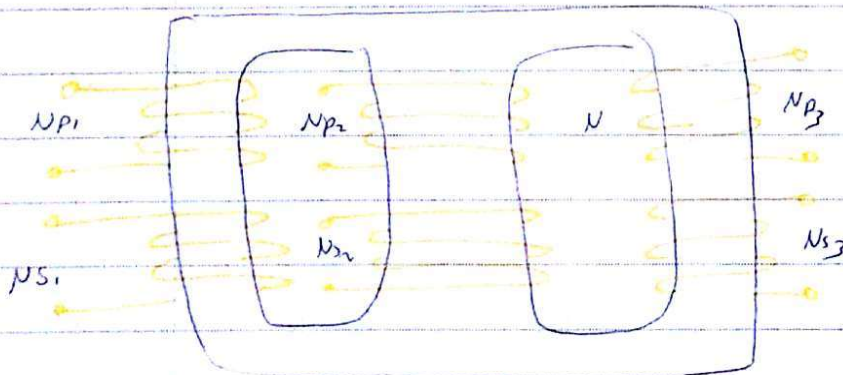




# THREE PHASE TRANSFORMER:



each unit can be replaced if sth trouble happens



Smaller  
lighter  
Cheaper  
more efficiency

single three leg

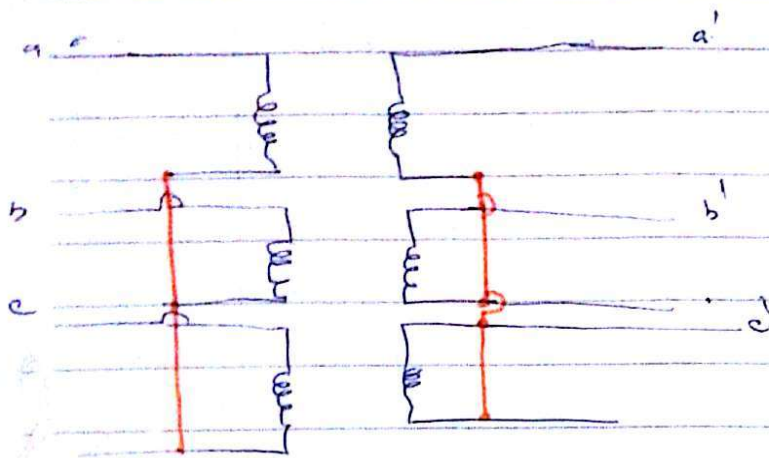
Connection

- YY
- YA
- ΔY
- ΔΔ

[  $\Delta/\Delta/\Delta/\Delta/\Delta/\Delta$  ]  
[  $\Delta/\Delta/\Delta$  ]



WYE - WYE connection:-



$$V_P = \frac{1}{\sqrt{3}} V_{SE}$$

$$\frac{V_P}{V_S} = \frac{V_P}{\sqrt{3} V_P}$$

$$V_{\phi P} = \frac{1}{\sqrt{3}} V_{LP}$$

$$V_{\phi S} = \sqrt{3} V_{\phi S}$$

$V_P$  120 apart in any other voltage

$$\frac{V_P}{V_S} = \frac{\sqrt{3} V_{\phi P}}{\sqrt{3} V_{\phi S}} = \alpha$$

(1)  $\Delta$   $\Delta$

- (i) if load unbalanced voltage phase can become unbalanced
- (ii) third harmonic can be large (noise)

(2)  $\Delta$   $\Delta$

- (i) grounded the neutral line (provides a return path for any current imbalanced the load)
- (ii) add a third winding connection a  $\Delta$

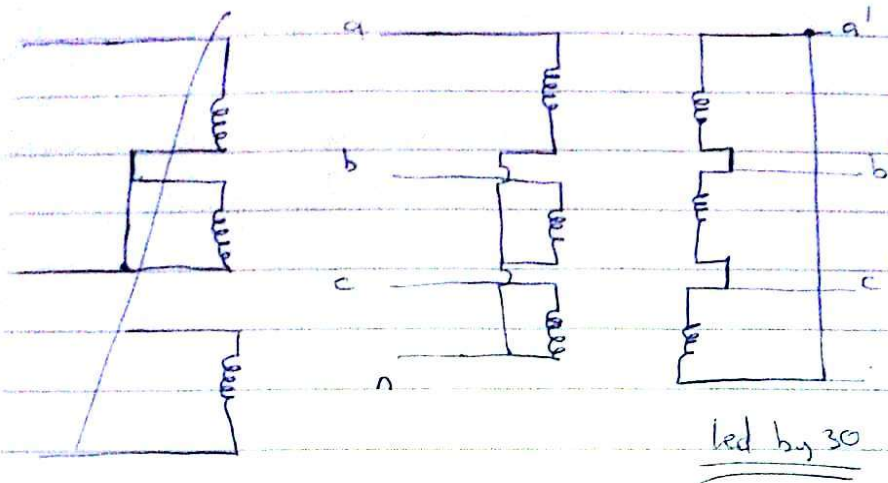
WYE DELTA CONNECTIONS

$$V_{LP} = \sqrt{3} V_{\phi P}$$

$$V_{LS} = V_{\phi S}$$

$$\frac{V_{LP}}{V_{LS}} = \sqrt{3} \alpha$$





- its has no harmonic problem because of  $\Delta$  connection
- secondary connection shifted  $30^\circ$  relative to Primary, can cause problem in parallel connection

DELTA WYE CONNECTION

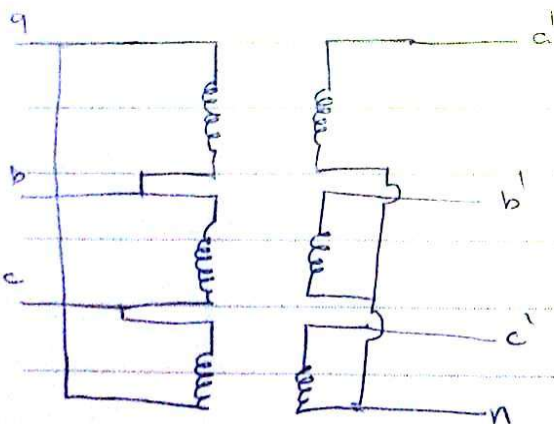
$V_{LP} = V_{\phi p}$

$V_{LS} = \sqrt{3} V_{\phi p}$

$\frac{V_{LP}}{L_S} = \frac{L}{\sqrt{3}} a$

Y- $\Delta$  connection

but lag by  $30^\circ$



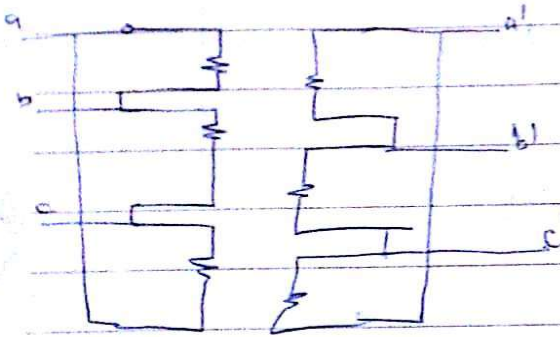


### DELTA DELTA CONNECTION

$$V_{LP} = V_{PP} \quad V_{Ls} = V_{Ps}$$

$$\frac{V_{LP}}{V_{Ls}} = a$$

has no problem with harmonics  
or Phase shift



2.9. A 5000 kVA, 230/13.8 kV single phase power transformer has open circuit resistance of 1 percent and reactance of 5 percent. The open circuit performed on low voltage side of the transformer

$$V_{o.c} = 13.8 \text{ k} \quad I_{o.c} = 21.1 \quad P_{o.c} = 40.8 \text{ k}$$

a) Find the equivalent circuit referred to the low voltage side of the transformer.

$$a = \frac{230}{13.8} = 16.66$$

$$\phi = \cos^{-1} \frac{40.8 \text{ k}}{21.1 \times 13.8 \text{ k}} = 71.99^\circ$$

$$Y = 1.528 \times 10^{-3}$$

$$R_c = (1.528 \times 10^{-3} \cos^{-1} 71.99) = \frac{2.24 \text{ V}}{4664.6371 \text{ } \Omega} = 8.08$$

$$X_m = (1.528 \times 10^{-3} \sin 71.99)^{-1} = \frac{660.97 \text{ } \Omega}{737} = 2.65$$

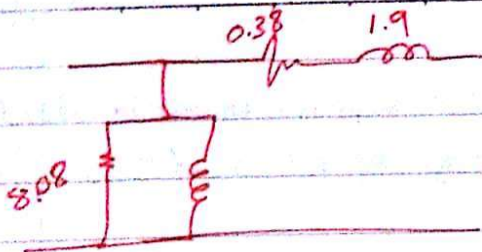
$$Z_{base} = \frac{V_{base}}{I_{base}}$$

$$Z_{base} = \frac{V_{base}}{I_{base}} = \frac{13.8 \text{ k}}{\frac{5000}{13.8 \text{ k}}} = 38.088$$

$$R_{eq} = (0.01) (38.088) = 0.38088$$

$$X_{eq} = (0.05) (38.088) = 1.9044$$





b) the voltage on the secondary side is 13.8kV and the power is 4000 kW at 0.8 PF lagging. Find VR & efficiency?

$$\frac{V_P}{S} = 13.8 + \frac{I_S \cos^{-1} 0.8}{\frac{4000 \text{ kW}}{13.8 \text{ kV}}} [0.38 + 1.9j]$$

$$I_S = \frac{4000 \text{ kW}}{13.8 \text{ kV}} \cos^{-1} 0.8$$

$$\frac{362.3}{289.85} \angle -36.87^\circ$$

$$\frac{V_P}{S} = 14330 \angle 1.5^\circ$$

$$V_R = \frac{14330}{13800} - 13800 = 3.89\%$$

$$\text{Efficiency} = \frac{4000 \text{ kW}}{4000 \text{ kW} + \frac{19330^2}{225 \text{ V}} + (362.3)^2 (0.38)} = 96\%$$



A 13.8 kV single phase generator supplies power to a load through a transmission line.  $Z_{load} = 50 \angle 36.87^\circ$  and  $Z_{line} = 60 \angle 60^\circ$

1] if the generator is directly connected to the load (without transformer) what is the ratio of the load voltage to the generated voltage? what is the transmission losses of the system??

$$I = \frac{13800}{50 \angle 36.87^\circ + 60 \angle 60^\circ} = 24.83 \angle -39.3^\circ$$

$$\text{Voltage line} = 24.83 \angle -39.3^\circ (50 \angle 36.87^\circ) = 1247.28 \angle -29.3^\circ$$

$$\text{ratio} = \frac{12.4728 \text{ k}}{13.8 \text{ k}} = 0.89$$

$$\text{Losses} = 30 (24.83)^2 = 36999.739 \text{ watt}$$

$$\text{2] efficiency: } \frac{246611.56}{265107.927} = 93$$



Resistance [ المقاومة ] → صفة مقاومة من حيث المادة لمحدد التيار الكهربائي فيها



$$V = I R \quad R [\Omega]$$

Inductance [ المحاثة ]

DC short ckt - (تخزن الطاقة لفترة)

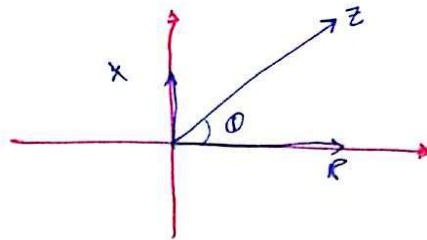
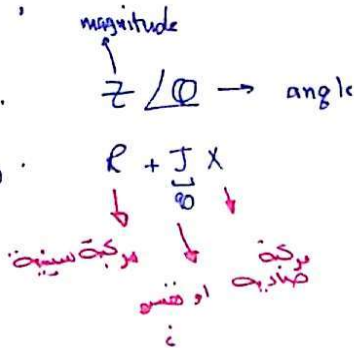


$$AC \quad X = \omega L [\Omega]$$

Impedance [ Z ] :

polar form .

Rectangular form .



power

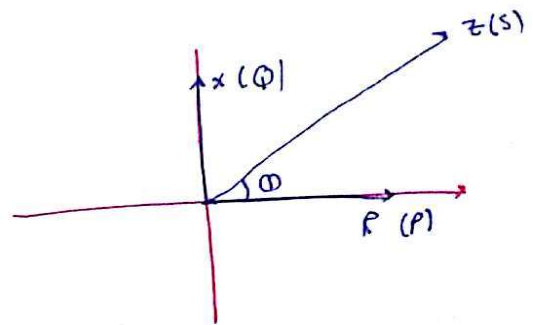
$$DC \rightarrow P = VI \quad , \quad I^2 R \quad , \quad \frac{V^2}{R}$$

AC →

[1] Apperant Power (S) = VI [VA] .  
 (القدرة الظاهرية)

[2] Active power (P) = VI cos theta [Watt] .  
 Average , Real

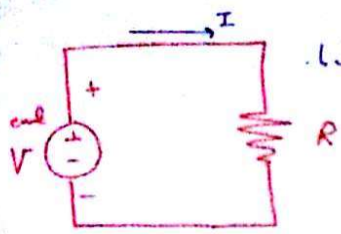
[3] Reactive Power (Q) = VI sin theta [VAR] .





# Type of machines:

## 1) Electrical circuits:



electromotive force

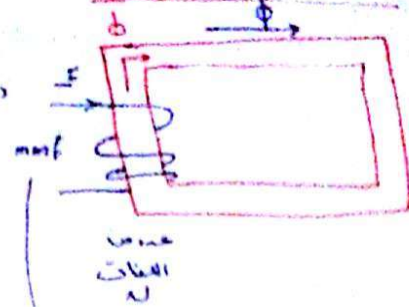
دائرة كهربية (Electrical circuit)

$$I = \frac{V}{R}$$

$$R = \frac{L}{\sigma A}$$

length  
conductivity

## 2) magnetic circuits



magnetic motive force

$$mmf = NI$$

دائرة كهربية مغناطيسية (Magnetic circuit)  
مقاومة كهربية (Electrical resistance)  $\rightarrow$  مقاومة مغناطيسية (Magnetic reluctance)

$$\phi = \frac{mmf}{R}$$

reluctance

$$R = \frac{L}{\mu A}$$

length  
Area

## Magnetic Field Intensity (strength) H

$$H = \frac{mmf}{L} = \frac{NI}{L} \quad [A/m]$$

## Magnetic Flux density (B):

$$B = \mu H \quad [T]$$

$$\mu = \mu_r \cdot \mu_0$$

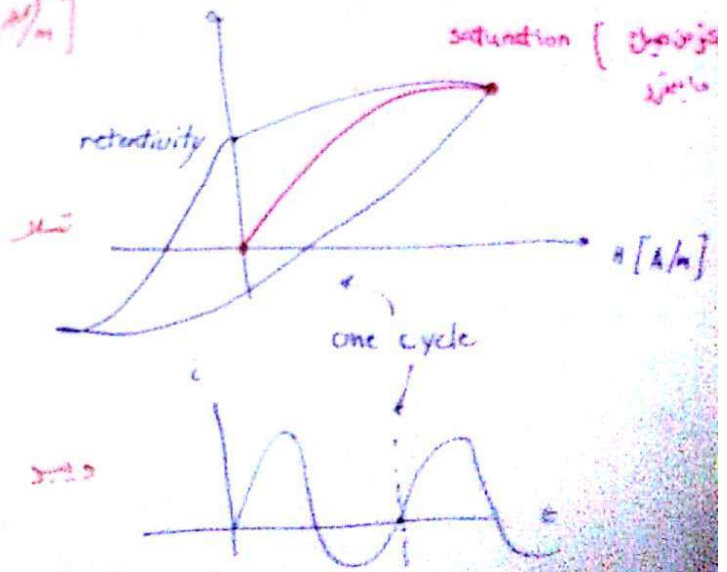
relative  
 $\mu_0$  air [ $4\pi \times 10^{-7}$ ]

$$\text{Flux} = A \cdot B \quad [Wb]$$

area  
Magnetic Flux density

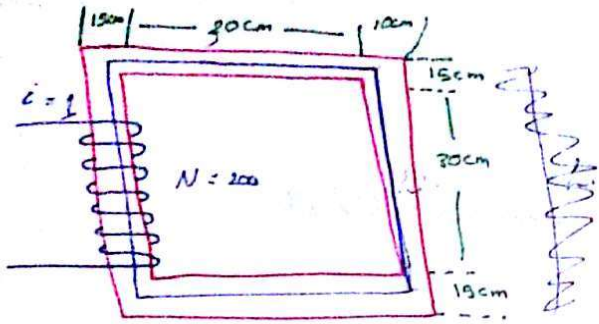
$$A \cdot \mu \frac{NI}{L} = \frac{mmf}{R} = \frac{mmf}{L/\mu A}$$

B [T]





Example 1-1:



the depth of core = 10 cm,

$\mu_r = 2500$ , Flux??

solution:

$$\phi = \frac{E E \mu}{R} = \frac{N i}{L} \cdot A \cdot \mu$$

$$= \frac{200 \times 1}{2 \pi 0} \times 2500 \times 4 \pi \times 10^{-7}$$

مناظر اینس لایه  
 حسب اینس منطقی کل دار خطه  
 بتستی اینس

\*\*\*

$$R = \frac{L}{\mu A}$$

$$10 \text{ core } L_1 = \frac{15}{2} + 30 + \frac{15}{2} = 45 \times 10^{-2} \text{ m.}$$

$$A_1 = 10 \times 10 = 0.01 \text{ m}^2$$

$$R_1 = \frac{0.45}{(2500 \times 4 \pi \times 10^{-7}) \times 0.01} = 14300 \text{ A.turns/wb}$$

$$L_2 = \frac{10}{2} + 30 + \frac{15}{2} = 1.25 \text{ m}$$

$$A_2 = 15 \times 10 = 0.015 \text{ m}^2$$

$$R_2 = \frac{1.25}{2500 \times 4 \pi \times 10^{-7} \times 0.015} = 26525 \text{ A.turns/wb}$$

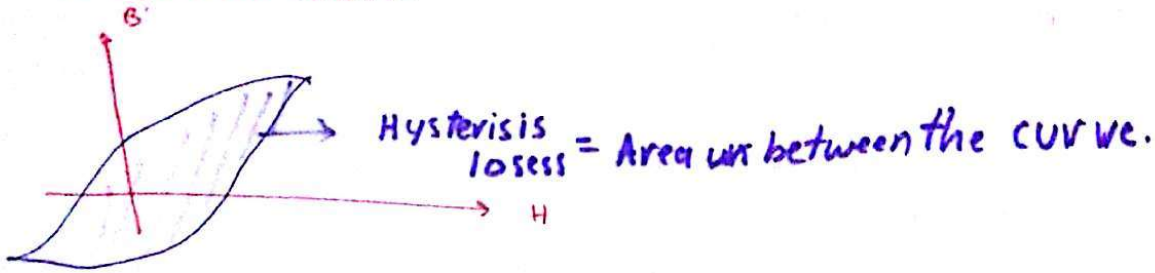
$$R = R_1 + R_2 = 14300 + 26525 = 40825 \text{ A.turns/wb}$$

$$\phi = \frac{200 \times 1}{40825} = \boxed{4.89 \times 10^{-3} \text{ wb}}$$



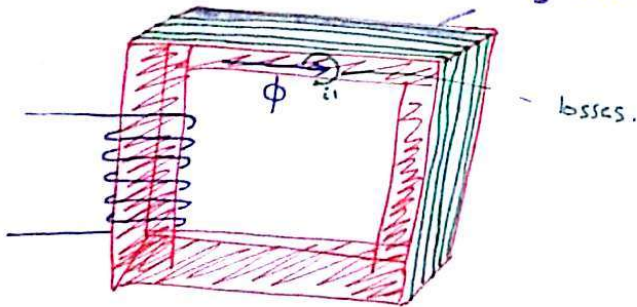
Magnetic losses:

[1] Hysteresis losses :-



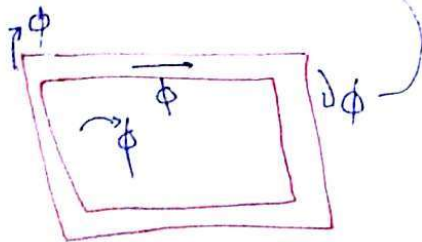
[2] Eddy current losses

مادة عازلة



نتيجة لتعدد سلك  
بعض تيارات هيزرة لولبية  
تنتج صدمة هذه الصدمة مثل  
هذه الصدمة على شكل صدمات خالصة ما يمر  
سبب الحثك بوجود حثبات

[3] Leakage flux

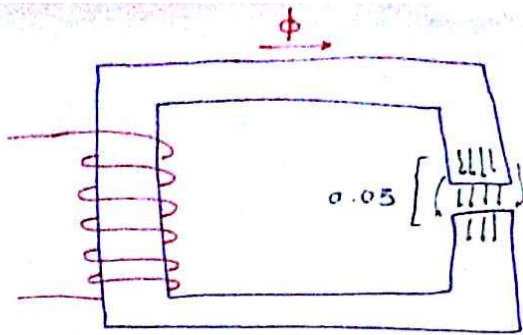


Flux غير الحثبات

لانها ال



Example 1-2



$l_c = 40\text{cm}$ , air gap =  $0.05\text{cm}$   
 $A_c = 12\text{cm}^2$   
 $\mu_r = 2000$   
 Air gap =  $105\%$   $A_c$   
 Find  $I$ ??

solution

الفروع  $\rightarrow A \uparrow \rightarrow \mu_0$   
 الجلب  $\rightarrow AL \rightarrow \mu_r \mu_0$

$$R_{\text{core}} = \frac{l_{\text{core}}}{\mu_r \mu_0 A_{\text{core}}} = \frac{0.4}{4000 \times 4\pi \times 10^{-7} \times 0.12 \times 10^{-2}} = 66314.55962 \text{ A.turns/wp}$$

$$R_{\text{air}} = \frac{0.05\text{cm}}{4\pi \times 10^{-7} \times 1.05 \times 0.0012} = 31578361 \text{ A.turns/wp}$$

$$I = R_{\text{air}} + R_{\text{core}} = 31644676.28 \text{ A.turns/wp}$$

Four electromagnetic Principles:

[1] A current carrying wire produce a magnetic field  $\vec{M}$

[2] a time changing magnetic flux produce an emf

$$\text{emf} = - \frac{d\phi}{dt}$$

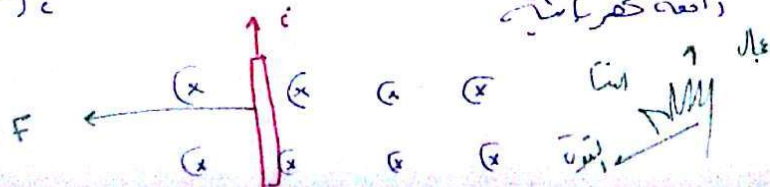
لأننا القوة تعاكس  
الحقل المغناطيسي

تحديد مجال حثية قاعدة اليد اليمنى  
مجال التيار  $\vec{M}$   
شدة المجال المغناطيسي

[3] Motor Action

$$\vec{F} = (\vec{I} \times \vec{B})$$

مبدأ عرفية تيار جومر داخل مجال مغناطيسي يتقاربت توك  
داقعة كهربائية



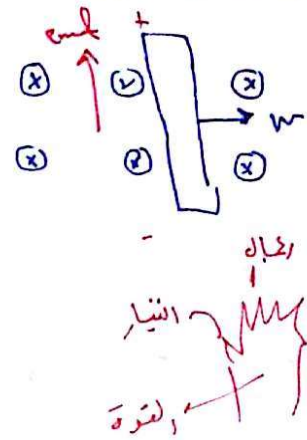


4 Generator Action

$$\vec{E} = (\vec{v} \times \vec{B}) l$$

سلك بدافنحرکو بحال مضامیسی

بنشأ میخ تیار



بهمین استجارت منسوب القادمان، المغاغلان، لقرات

Q.1

Example: A 500 V, 50 h.p (37.3 kW), 1000 rpm DC motor has no full load efficiency of 90%. The armature resistance is 0.29 Ω and there is a total voltage drop of 2V at the brushes. The field current is 1.8 A.

- (1) Full-load line current (2) Full load torque in N.m (3) total resistance in motor. starter to limit the starting current to 1.5 times the full load.

Solution:

$$\frac{P_{out}}{P_{in}} = 90\%$$

$$P_{out} = 90\% \times 37.3 \times 10^3 = 33.57 \text{ kW}$$

$$\frac{373000}{90\%} = 414444 \text{ W}$$

total current  $P = V \times I$

$$414444 = 500 \times I$$

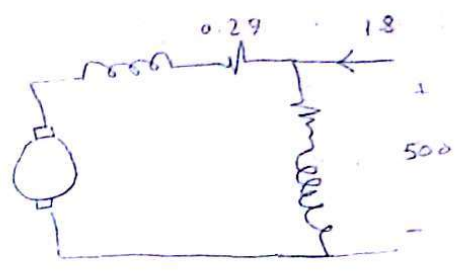
$$(i) I = 82.8 \approx 83 \text{ A}$$

$$I_L = 83 - 1.8 = 81 \text{ A}$$

$$(iii) 500 = 2 + (0.29 + R) (81 \times 1.5 - 1.8)$$

$$498 = 121.95 + R \times 121.95$$

$$R = 3.8436 \Omega$$



$$(ii) \tau = k\phi$$

$$\tau = \frac{E_a i_a}{\omega} = 35618 \text{ N.m}$$

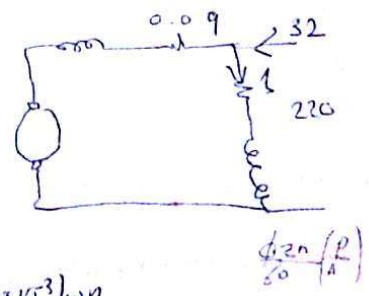
Example: A 4 pole, 220V shunt motor has 540 lap-wound conductors. It takes 32A from main supply and develops 7.5 h.p (5.595 kW). The field winding takes 1A. The armature resistance is 0.04 Ω and the flux per pole is 30 mWb.

- (1) speed (2) torque.

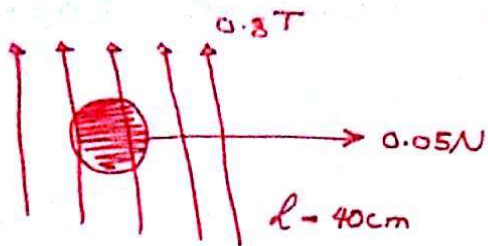
$$I_L = 31 \text{ A at starting. } \phi = 30 \times 10^{-3}$$

$$E_a = k\phi\omega$$

$$220 = 31(0.04) + E_a \quad E_a = 217.21 = k(30 \times 10^{-3})\omega$$







Find  $i$  ?

$$0.05 = i(40 \times 0.4 \times 0.8 \sin 90)$$

16 mA out of the page

Torque

$$130 = 122.4 + 0.2 I_a$$

$$I_a = 33$$

$$T = 37 \text{ N.m}$$

Example: Separately excited dc motor is rotated at 1000 rpm.

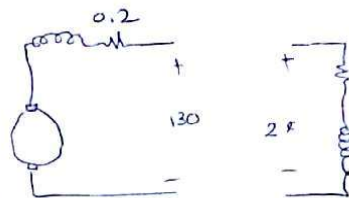
$I_f$	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8
$V_T$	0	30	60	85	102	115	124	130	134

$R_A = 0.2 \quad V_A = 130$

$V_{\text{field}} = 24 \text{ V}$   
 $R_f$  is adjustable.

1) field current at no load with 1000 rpm.

at  $V_T = 130 \quad I_f = 0.7 \text{ A}$



2) The motor drives a load at 1200 rpm. calculate the armature voltage at 1200 rpm if the field resistance  $R_f = 60 \Omega$ .

$$I_f = \frac{24}{60} = 0.4$$

$$E_a = k\phi \frac{1200}{1000} = k\phi \frac{1200}{1000}$$

$$102 - 0.2 = k\phi \frac{1200}{1000}$$

$$E = E_{1000} \frac{1200}{1000}$$

$$E_a = 122.4$$

$$E_a = k\phi \omega$$

$$\frac{E_a}{102} = \frac{k\phi \cdot 1200}{k\phi \cdot 1000}$$

$$E_a = 122.4 \quad V_T = 122.4 + 0.2 I_a$$

$$122.4 = k\phi + 1200 \times \frac{2\pi}{60}$$

$$k\phi = \frac{102}{0.974}$$

3) torque for above condition

$$E_a = 122.4$$

$$\frac{122.4}{1200} = \frac{122.4}{1000}$$

$$T = 122.4$$

4) motor supplies mechanical load at 4000 W at 1450 rpm the mechanical losses are 160 W calculate the efficiency

$$P_{\text{con}} = 4000 + 160 = 4160$$

$$\frac{4000}{4160} = 96\%$$

$$\frac{4000}{4000 + 160}$$

$$(V_T - E_a + I_a R) I_a$$

$$V_T I_a = 4160 + I_a^2 R$$

$$I_a = 33.74$$

$$130 = 0.2(33.74) + E_a \quad E_a = 123.25$$

A 230 V, 10 hp dc shunt motor delivers power to a load at 1200 r/min.

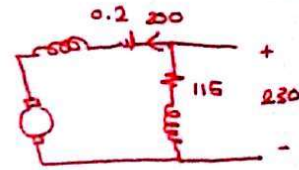
$I_a = 200$  A,  $R_a = 0.2 \Omega$   $R_p = 115 \Omega$  rotational losses are 500 W, torque??

Solution

~~$T = k\phi i$~~

~~$T = k\phi \times 200$~~

~~$k\phi = \frac{E_a}{\omega} = \frac{230 - 0.2(200)}{1200}$~~



~~$P = 7,460 \text{ kWatt}$~~

$230 = E_a + 40$   $E_a = 190$

$P = 190 \times 200 = 38000 - 500$

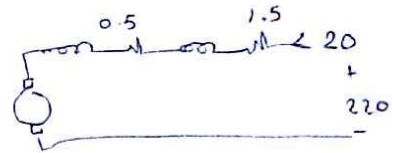
$P = 37500$

$T = \frac{37500}{\frac{1200 \times (2\pi)}{60}} = 298.41$

series-connected DC motor has an  $R_a = 0.5 \Omega$   $R_p = 1.5 \Omega$  driving a constant load at 1200 rpm, the current drawn by the motor is 20 A from the voltage source 220 V. The rotational losses is 150 W. find efficiency.

$220 = 20(1.5 + 0.5) + E_a$

$E_a = 180$



$P = 180 \times 20 = 3600$

$P = \frac{3600 - 150}{3600} = 95.8\% \quad 78.404$



5 hp, 1800 rpm, 230 V<sub>oc</sub>, shunt excited motor with circuit model resistances  
 $R_f = 209 \Omega$   $R_a = 1.5 \Omega$  (P<sub>mech</sub> losses = 0W).

1) rated torque

$$\tau = k\phi i$$

$$= \frac{E_a i}{\omega} = \frac{5 \times 746}{1800} = 19.8 \text{ N.m}$$

2) terminal current 14.3A while supply with rated voltage but driving less than the rated load. determine the mechanical power in hp and operational efficiency.

$$P = \tau \omega$$

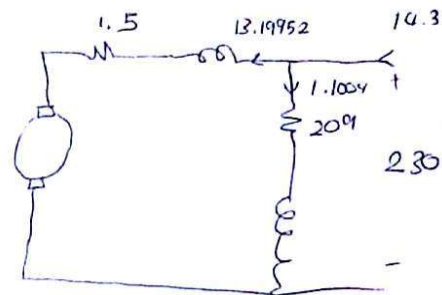
$$k\phi i \times 1800$$

$$\frac{E_a i}{\omega} \times \omega$$

$$13.19952 (230 - 1.5(13.19952))$$

$$2,774 \text{ kW out}$$

$$\frac{P_{out}}{P_{input}} = \frac{2774}{5 \times 746} = 74.36\%$$



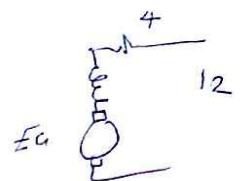
500 V, 37.3 kW, 1000 rpm DC shunt motor has an full load efficiency of 90%  
 $R_A = 0.28 \Omega$  voltage drop 2  $I_f = 1.8$ .

12V permanent DC-Motor with  $R_a = 4 \Omega$ , speed = 2700 rpm  
 $I_c = 300 \text{ mA}$  rated voltage

1) torque  $\tau = \frac{E_a i}{\omega}$

$$\frac{10.8 \times 0.3}{2700}$$

$$11.45 \times 10^{-3}$$



$$12 = 4 \times 0.3 + E_a$$

$$E_a = 10.8$$

1-21

P 63

□ initial Force  $e$  / initial current

$$\rightarrow \text{initial current} = \frac{VB}{R} = \frac{100}{0.25} = 400 \text{ A.}$$

$$\text{initial Force} = l(i \times B)$$

$$l(400 \times 0.5 \sin 90) = 200 \text{ N} \rightarrow \text{to the right.}$$

$$\boxed{2} \quad e_{\text{ind}} = vBl \quad \text{no load } v_{\text{ind}} = vB$$

$$100 = v \times 0.5 \quad v = 200 \text{ m/s}$$

 $\boxed{3}$  opposite direction  $\rightarrow$  motor

$$F = 25 \text{ N}$$

$$25 = i * B \quad \boxed{i = 50 \text{ A}}$$

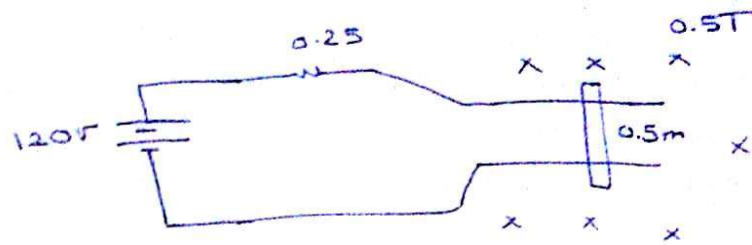
$$50 = \frac{vB - e_{\text{ind}}}{0.25} \quad v_{\text{ind}} = 87.5$$

$$e_{\text{ind}} = vBl$$

$$87.5 = v \times 0.5 \quad v = 175 \text{ m/s}$$

$$\eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{25 \times 175}{50 \times 100} = \frac{4375}{5000} = 87.5$$





1] opposite  $\rightarrow$  motor

$F = 20$

$$\frac{120 - v_{ind}}{0.25} = i \quad \leftarrow \quad \begin{aligned} 20 &= i \times 0.5 \times 0.5 \\ i &= 80 \end{aligned}$$

$$\frac{120 - v_{ind}}{0.25} = 80$$

$$v_{ind} = 100 - \sqrt{v} \times 0.5 \times 0.5$$

$\sqrt{v} = 400 \text{ m/s}$

2]  $B = 0.45$

$F = 0.45 \downarrow \quad \sqrt{v} \downarrow \quad v_{ss} = \frac{120}{0.45 \times 0.5} = 533.33 \text{ m/s}$

3]  $v_B = 100 \quad v_{ss} = \frac{100}{0.45 \times 0.5} = 444.44 \text{ m/s}$

4] by decreasing or increase the voltage and Flux density.

[1]

[2]

$F = 30 \text{ N}$

$B = 0.3$

$0.5$

$0.05$

$30 = i \cdot 0.3 \cdot 0.5$

$i = 200 \text{ A}$

$200 = \frac{120 - e_{\text{ind}}}{0.25}$

$e_{\text{ind}} = 70$

$70 = v \cdot 0.5 \cdot 0.3$

$v = 466.66 \text{ m/s}$

$30 = 0.5 \times 0.5 i$

$i = 120$

$120 = \frac{120 - e_{\text{ind}}}{0.25}$

$e_{\text{ind}} = 90$

$90 = v \cdot 0.5 \cdot 0.5$

$v = 360 \text{ m/s}$

$30 = 0.5 \times 0.05 i$

$i = 1200$

$1200 = \frac{120 - e_{\text{ind}}}{0.25}$

$e_{\text{ind}} = 180$

$-180 = v \cdot 0.05 \cdot 0.5$

$v = -7200$

no-load

$B = 0.5$

 $v$ 

$120 = 0.5 \times 0.5 v$

$v = 480 \text{ m/s}$

$30 = i \times 0.5 \times 0.5$

$i = 120$

$v = 360 \text{ m/s}$

$120 = B \times 0.5 \times 360$

$B = 0.66 \text{ T}$





The Hashemite University  
Faculty of Engineering  
Course Syllabus

**Course Title:** Electrical Machines      **Course Number:** 110405323  
**Department:** Department of Mechatronics      **Designation:** Compulsory  
**Prerequisite(s):** 110409203  
**Instructor:** Eng. Fadwa Momani      **Instructor's Office:** E3115  
**Instructor's e-mail:** [Fadwamomani@yahoo.com](mailto:Fadwamomani@yahoo.com), Engfadwa Momani (facebook account)  
**Office Hours:** Announced on the office door  
**Time:** 10:40 -11:50 (Sun→ Thu)      **Class Room:** E2023

**Course description:** This course introduces the basic principles of electrical machines and energy conversion. Principles and operation of Single and three phase transformers are also introduced. The principles, operation, key characteristics, and application of DC motors (e.g., bush types, brushless type, and servo type), AC motors (e.g., single and three phase), and special purposes motors (e.g., stepper motors) are also presented.

**Textbook(s):** Stephen Chapman: "Electric Machinery Fundamentals", 5th edition, McGraw Hill, 2012.

**Other required material:**

1. George Mcpherson, "An Introduction to Electrical Machines and Transformers," Wiley: New York, 1981/1990.
2. Charles Hubert, "Electric Machines: Theory, Operation, Applications, Adjustment, and Control," Pearson Education: Delhi, 2nd Ed, 2002.
3. Smarajit Ghosh, "Electric Machines," Pearson Education: Delhi, 2005.
4. Sayed Naser, "Handbook of Electrical Machines," McGraw-Hill: New York, 1987.
5. Sayed Naser, "Electrical Machines and Electromechanics," Schaum's outline series , 2<sup>nd</sup> Ed, 1998.

**Course objectives:** *The student shall be able to:*

1. Obtain mathematical models, estimate, and analyze the performance characteristics of transformers and motors
2. Identify the best electrical motor for the desired application
3. Comprehend the impact of state-of-the-art electric machines in solving industrial problems

**Topics covered:**

1. Introduction to Machinery Principles (Chapter 1)
2. DC Machinery Fundamentals (Chapter 7)
3. DC Motors and Generators (Chapter 8)
4. Transformers (Chapter 2)
5. AC Machinery Fundamentals (Chapter 3)
6. Induction Motors (Chapter 6)
7. Single-Phase and Special-Purpose Motors (Chapter 9)

**Class/laboratory schedule:** 3 class sessions each week; 50 minutes each  
**Grading Plan:**

First Exam	(30 Points)	wed 8/6/2016
Second Exam	(30 Points)	Tus 21/6/2016
Final Exam	(40 Points)	To be announced by the registrar

**General Notes:** Attendance is mandatory

**Prepared by:** Eng. Fadwa Momani      **Date:** 24/5/2016

# Electrical Machines Course Contents

**Textbook:** *Electric Machinery Fundamentals* by Stephen J. Chapman, McGraw Hill.

The contents covered in this course are presented during the semester as follows:

1. Introduction to Machinery Principles
2. DC Machinery Fundamentals
3. DC Motors and Generators
4. Transformers
5. AC Machinery Fundamentals
6. Induction Motors
7. Single-Phase and Special-Purpose Motors

In each required chapter, the sections covered are as follows during the semester:

Chapter	Sections		Excluded Titles
	4 <sup>th</sup> Version	5 <sup>th</sup> Version	
Introduction	1.1 – 1.8, 1.10	1.1 – 1.8, 1.10	
DC Motors	8.1, 8.4, 8.7, 8.8	7.1, 7.4, 7.7, 7.8	
	9.1 – 9.4, 9.6 – 9.7, 9.10, 9.17	8.1 – 8.7, 8.10, 8.17	
AC Circuits Review	1.9, 1.10, Appendix A	1.9, 1.10, Appendix A	
Transformers	2.1 – 2.3, 2.5, 2.7, 2.8, 2.10, 2.13, 2.14	2.1 – 2.3, 2.5, 2.7, 2.8, 2.10, 2.13, 2.14	<ul style="list-style-type: none"> <li>▪ The Per-Unit System for Three-Phase Transformers</li> <li>▪ The Transformer Phasor Diagram</li> </ul>
AC Induction Motors	4.6 – 4.9	3.6 – 3.9	
	7.1 – 7.5, 7.9, 7.11, 7.13, 7.14	6.1 – 6.5, 6.11, 6.13, 6.14	
Single-Phase and Special-Purpose Motors	10.1 – 10.4, 10.6, 10.7	9.1 – 9.4, 9.6, 9.7	<ul style="list-style-type: none"> <li>▪ The Double-Revolving-Field Theory of Single-Phase Induction Motors</li> <li>▪ The Cross-Field Theory of Single-Phase Induction Motors</li> <li>▪ Reluctance Motors</li> <li>▪ Hysteresis Motors</li> </ul>