

# Data Dependencies

Not all loops can be parallelized. Before adding OpenMP directives need to check for any dependencies:

We categorize three types of dependencies:

- ◆ Flow dependence: Read after Write (RAW)
- ◆ Anti dependence: Write after Read (WAR)
- ◆ Output dependence (Write after Write (WAW))

## FLOW

*X = 21*  
*PRINT \*, X*

## ANTI

*PRINT \*, X*  
*X = 21*

## OUTPUT

*X = 21*  
*X = 21*

# Data Dependencies (2)

*For our purpose (openMP parallel loops) we only care about loop carried dependencies (dependencies between instructions in different iterations of the loop)*

Let's find the dependencies in the following loop?

```

S1: DO I=1,10
S2:   B(i) = temp
S3:   A(i+1) = B(i+1)
S4:   temp = A(i)
S5: ENDDO
    
```

# Data Dependencies (2)

*For our purpose (openMP parallel loops) we only care about loop carried dependencies (dependencies between instructions in different iterations of the loop)*

What are the dependencies in the following loop?

```
S1: DO I=1,10
S2:  B(i) = temp
S3:  A(i+1) = B(i+1)
S4:  temp = A(i)
S5: ENDDO
```




1: S3 → S2 anti (B)

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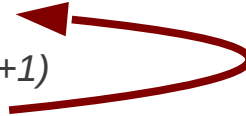
1: S3 → S2 anti (B) 2: S3 → S4 flow (A)
--

# Data Dependencies (2)

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- 1: S3 → S2 anti (B)
- 2: S3 → S4 flow (A)
- 3: S4 → S2 flow (temp)

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S4:  temp = A(i) ←
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```

- 1: S3 → S2 anti (B)
- 2: S3 → S4 flow (A)
- 3: S4 → S2 flow (temp)
- 4: S4 → S4 output (temp)

# Data Dependencies (2)

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What are the dependencies in the following loop?

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1: S3 → S2 anti (B)
2: S3 → S4 flow (A)
3: S4 → S2 flow (temp)
4: S4 → S4 output (temp)

*Sometimes it helps to "unroll" part of the loop to see loop carried dependencies more clear*

```
S2: B(1) = temp
S3: A(2) = B(2)
S4: temp = A(1)
```

```
S2: B(2) = temp
S3: A(3) = B(3)
S4: temp = A(2)
```

# Data Dependencies (2)

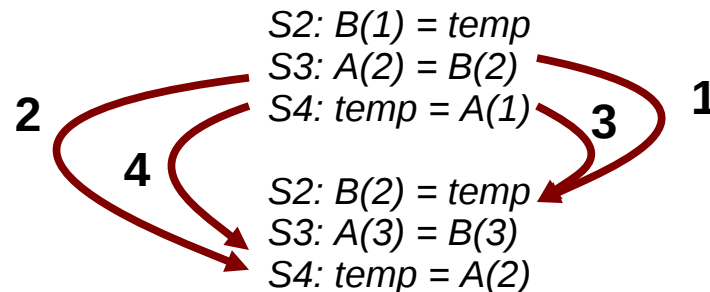
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```

- |                          |
|--------------------------|
| 1: S3 → S2 anti (B)      |
| 2: S3 → S4 flow (A)      |
| 3: S4 → S2 flow (temp)   |
| 4: S4 → S4 output (temp) |

Sometimes it helps to "unroll" part of the loop to see loop carried dependencies more clear



# Case Study: Jacobi

Implement a parallel version of the Jacobi algorithm using OpenMP. A sequential version is provided.

# Data Dependencies (3)

Loop carried anti- and output dependencies are not true dependencies (re-use of the same name) and in many cases can be resolved relatively easily.

Flow dependencies are true dependencies (there is a flow from definition to its use) and in many cases cannot be removed easily. Might require rewriting the algorithm (if possible)

# Resolving Anti/Output Deps

## Use PRIVATE clause:

Already saw this in example hello\_threads

## Rename variables (if possible):

Example: in-place left shift

```
DO i=1,n-1
  A(i)=A(i+1)  →  ANEW(i) = A(i+1)  →
ENDDO          ENDDO
```

```
!$OMP PARALLEL DO
DO i=1,n-1
  ANEW(i) = A(i+1)
ENDDO
!$OMP END PARALLEL DO
```

If has to be in-place can do it in two steps:

```
!$OMP PARALLEL
!$OMP DO
  T(i) = A(i+1)
!$OMP END DO
!$OMP DO
  A(i) = T(i)
!$OMP END DO
!$OMP END PARALLEL
```

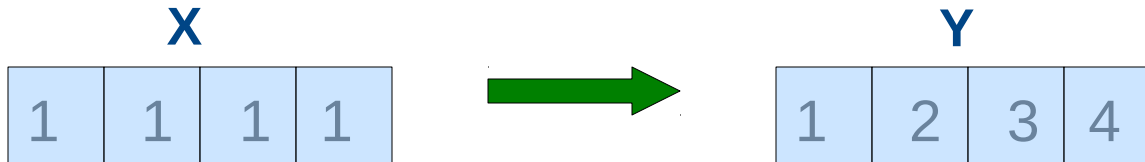
# More about shared/private vars

Besides the clauses described before OpenMP provides some additional datascope clauses that are very useful:

- ◆ **FIRSTPRIVATE ( *list* ):**  
Same as PRIVATE but every private copy of variable 'x' will be initialized with the original value (before the omp region started) of 'x'
- ◆ **LASTPRIVATE ( *list* ):**  
Same as PRIVATE but the private copies of the variables in list from the last work sharing will be copied to shared version. To be used with **!\$OMP DO** Directive.
- ◆ **DEFAULT (SHARED | PRIVATE | FIRSTPRIVATE | LASTPRIVATE ):**  
Specifies the default scope for all variables in omp region.

# Case Study: Removing Flow Deps

$$Y = \text{prefix}(X) \rightarrow Y(1) = X(1); Y(i) = Y(i-1) + X(i)$$

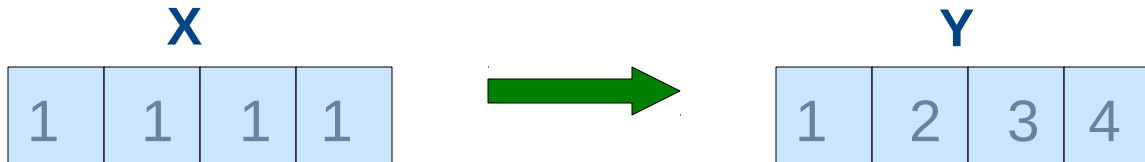


## SEQUENTIAL

```
Y[1] = X[1]
DO i=2,n,1
  Y[i] = Y[i-1] + X[i]
ENDDO
```

# Case Study: Removing Flow Deps

$Y = \text{prefix}(X) \rightarrow Y(1) = X(1); Y(i) = Y(i-1) + X(i)$



## SEQUENTIAL

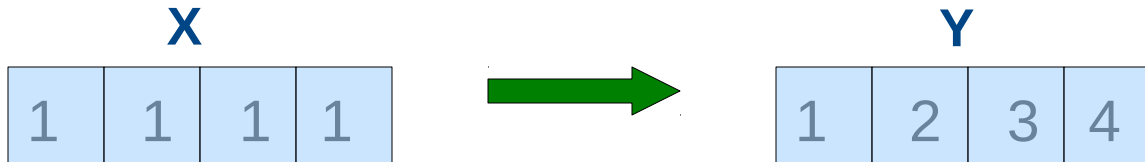
```
Y[1] = X[1]
DO i=2,n,1
  Y[i] = Y[i-1] + X[i]
ENDDO
```

## PARALLEL

```
Y[1] = X[1]
!$OMP PARALLEL DO
DO i=2,n,1
  Y[i] = Y[i-1] + X[i]
ENDDO
!$OMP END PARALLEL DO
```

# Case Study: Removing Flow Deps

$Y = \text{prefix}(X) \rightarrow Y(1) = X(1); Y(i) = Y(i-1) + X(i)$



## SEQUENTIAL

```
Y[1] = X[1]
DO i=2,n,1
  Y[i] = Y[i-1] + X[i]
ENDDO
```

## PARALLEL

```
Y[1] = X[1]
!$OMP PARALLEL DO
DO i=2,n,1
  Y[i] = Y[i-1] + X[i]
ENDDO
!$OMP END PARALLEL DO
```

**WHY?**

# Case Study: Removing Flow Deps

## REWRITE ALGORITHM

1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

STEP 1: split X among threads; every thread computes its own (partial) prefix sum

1	2	3	4
---	---	---	---

1	2	3	4
---	---	---	---

1	2	3	4
---	---	---	---

1	2	3	4
---	---	---	---

STEP 2: create array T  $\rightarrow T[1]=0$ ,  $T[i] = X[(\text{length}/\text{threads})*(i-1)]$ , perform simple prefix sum on T  
(will collect last element from every thread (except last) and perform simple prefix sum)

0	4	4	4
---	---	---	---

 $\rightarrow$ 

0	4	8	12
---	---	---	----

STEP 3: every thread adds T[threadid] to all its element

<div>+0</div>			
1	2	3	4

+4			
5	6	7	8

<div>+8</div>			
9	10	11	12

+12			
13	14	15	16

STEP 4: Finished; we rewrote prefix sum by removing dependencies.

# Prefix Sum Implementation

How to implement the algorithm on the previous slide?

- Three separate steps
- Steps 1 and 3 can be done in parallel
- Step 2 has to be done sequential
- Step 1 has to be performed before step 2
- Step 2 has to be performed before step 3

**NOTE: For illustration purposes we can assume array length is multiple of #threads**

NOTE: exercise prefix

# Case Study: Removing Flow Deps

This Case study showed an example of an algorithm with real (flow) dependencies

- Sometimes we can rewrite algorithm to run parallel
- Most of the time this is not trivial
- Speedup much less impressive (often)